Formal Specification and Verification Reasoning about Java Programs

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Based on a lecture by Wolfgang Ahrendt and Reiner Hähnle at Chalmers University, Göteborg

Java Type Hierarchy



Each class referenced in API and target program is in signature with appropriate partial order

Modeling instance attributes

Person		
int int	age id	
int int	<pre>setAge(int i) getId()</pre>	

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Attribute Access

Signature $FSym_{nr}$: int age(Person); Person p;

Java/JML expression p.age >= 0

Typed FOL age(p)>=0

KeY postfix notation p.age >= 0

Navigation expressions in typed FOL look exactly as in JAVA/JML

Modeling Attributes in FOL Cont'd

Properties of attributes

- When not initialized, $\mathcal{I}(\mathbf{a}) = \mathbf{null}$
- Overloading can be resolved by qualifying with class path: Person::p.age

Changing the value of attributes

How to translate assignment to attribute p.age=17;?

assign
$$\frac{\Gamma \Longrightarrow \{1 := t\} \langle \texttt{rest} \rangle \phi, \Delta}{\Gamma \Longrightarrow \langle \texttt{l} = \texttt{t}; \texttt{rest} \rangle \phi, \Delta}$$

Admit on left-hand side of update program location expressions

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KeY applies rules automatically, you don't need to worry about details

Modeling class (static) attributes

For each class C with static attribute a of type T: FSym_{nr} declares non-rigid constant T a;

- Value of a is $\mathcal{I}(a)$ for all instances of C
- If necessary, qualify with class (path): byte java.lang.Byte.MAX_VALUE
- Standard values are predefined in KeY:
 \$\mathcal{I}\$ (byte java.lang.Byte.MAX_VALUE) = 127

Modeling reference this to the receiving object

Special name for the object whose JAVA code is currently executed:

in JML: Object self;

in Java: Object this;

in KeY: Object self;

Default assumption in JML-KeY translation: !(self = null)

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Constant Domain Assumption

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Realizing Constant Domain Assumption

- Non-rigid function boolean <created>(Object);
- Equal to true iff argument object has been created
- Initialized as $\mathcal{I}(< \texttt{created}>)(o) = F$ for all $o \in \mathcal{D}$
- Object creation modeled as {o.<created> := true} for next "free" o

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- Problem: difficult to exploit for update simplification



Definition (Quantified Update)

For T well-ordered type (no ∞ descending chains): quantified update:

{\for T x; \if P; l := r}

- For all objects d in D^T such that β^d_x ⊨ P perform the updates {1 := r} under β^d_x in parallel
- ▶ If there are several 1 with conflicting *d* then choose *T*-minimal one

Quantified Updates Cont'd

- The conditional expression is optional
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Example (Integer types are well-ordered in KeY— Demo)

\exists int n; ({**\for int** i; l := i}(l = n))

▶ Is valid both for JAVA int and \mathbb{Z} ($n \doteq 0$ non-standard order)

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Example (Initialization of field a for all objects in class C)

{\for T o; o.a := 0}

Extending Dynamic Logic to Java

Any syntactically correct Java with some extensions

- Needs not be compilable unit
- Permit externally declared, non-initialized variables
- Referenced class definitions loaded in background

And some limitations ...

- No concurrency
- No generics
- No Strings
- ► No I/O
- No floats
- No dynamic class loading or reflexion
- API method calls: need either JML contract or implementation



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- KeY implements update application and simplification rules for array locations

Java Features in Dynamic Logic: Complex Expressions

Complex expressions with side effects

- ▶ JAVA expressions may contain assignment operator with side effect
- FOL terms have no side effect on the state
- JAVA expressions can be complex and nested

Example (Complex expression with side effects in Java) int i = 0; if ((i=2)>= 2) i++; value of i ?

Complex Expressions Cont'd

Decomposition of complex terms by symbolic execution Follow the rules laid down in JAVA Language Specification

Local code transformations

$$\begin{array}{l} \text{evalOrderlteratedAssgnmt} & \frac{\Gamma \Longrightarrow \langle \texttt{y}\texttt{ = t; x = y; rest} \rangle \phi, \Delta}{\Gamma \Longrightarrow \langle \texttt{x = y = t; rest} \rangle \phi, \Delta} \quad \texttt{t simple} \end{array}$$

Temporary variables store result of evaluating subexpression

$$\label{eq:Field} \begin{array}{c} \Gamma \Longrightarrow \langle {\bf boolean \ v0; \ v0 \ = \ b; \ if \ (v0) \ p; \ r\rangle \phi, \Delta} \\ \hline \Gamma \Longrightarrow \langle {\bf if \ (b) \ p; \ r\rangle \phi, \Delta} \end{array} \quad {\rm b \ complex} \end{array}$$

Guards of conditionals/loops always evaluated (hence: side effect-free) before conditional/unwind rules applied

Java Features in Dynamic Logic: Abrupt Termination

Abrupt Termination: Exceptions and Jumps

Redirection of control flow via return, break, continue, exceptions

 $\langle \pi \operatorname{try} \xi p \operatorname{catch}(e) q \operatorname{finally} r; \omega \rangle \phi$

Rules ignore inactive prefix, work on active statement, leave postfix

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Rule tryThrow matches try-catch in pre-/postfix and active throw

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Demo

lect13/exc2.key

Formal Specification and Verification: Java DL

Java Features in Dynamic Logic: Aliasing

Reference Aliasing

Naive alias resolution causes proof split (on $o \doteq u$) at each access

$$\Rightarrow$$
 o.age \doteq 1 \rightarrow \langle u.age = 2; $angle$ o.age \doteq u.age

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Unnecessary case analyses

$$\Rightarrow o.age \doteq 1 \implies \langle u.age = 2; o.age = 2; \rangle o.age \doteq u.age$$
$$\Rightarrow o.age \doteq 1 \implies \langle u.age = 2; \rangle u.age \doteq 2$$

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Updates avoid case analyses— Demo lect13/alias2.key

- Delayed state computation until clear what is required
- Eager simplification of updates

Aliasing Cont'd

Form of Java program locations

- Program variable x
- Attribute access o.a
- Array access ar[i]

Assignment rule for arbitrary Java locations

assign
$$\frac{\Gamma \Longrightarrow \mathcal{U}\{1 := t\} \langle \pi \ \omega \rangle \phi, \Delta}{\Gamma \Longrightarrow \mathcal{U} \langle \pi 1 = t; \ \omega \rangle \phi, \Delta}$$

Updates in front of program formula (= current state) carried over

- Rules for applying updates complex for reference types
- Aliasing analysis causes case split: delayed using conditional terms

$$\{o.a := t\}u.a \rightsquigarrow \setminus if(\{o.a := t\}u \doteq o) \setminus then(t) \setminus else(\{o.a := t\}u).a$$

Java Features in Dynamic Logic: Method Calls

Method Call with actual parameters arg_0, \ldots, arg_n

$$\{\operatorname{arg}_0 := t_0 || \cdots || \operatorname{arg}_n := t_n || c := t_c\} \langle c.m(\operatorname{arg}_0, \ldots, \operatorname{arg}_n); \rangle \phi$$

where m declared as void $m(T_0 p_0, \ldots, T_n p_n)$

Actions of rule methodCall

- (type conformance of arg_i to T_i guaranteed by JAVA compiler)
- ▶ for each formal parameter p_i of m: declare & initialize new local variable T_i p#i =arg_i;
- look up implementation class C of m and split proof if implementation cannot be uniquely determined
- ▶ create method invocation c.m(p#0,...,p#n)@C

Method Body Expand

- 1. Execute code that binds actual to formal parameters $T_i p \# i = arg_i$;
- 2. Call rule methodBodyExpand

$$\begin{split} \Gamma &\Rightarrow \langle \pi \text{ method-frame(source=C, this=c)} \{ \text{ body } \} \; \omega \rangle \phi, \Delta \\ \Gamma &\Rightarrow \langle \pi \text{ c.m}(p \# 0, \dots, p \# n) @C; \; \omega \rangle \phi, \Delta \end{split}$$

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Symbolic Execution Only static information available, proof splitting

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Symbolic Execution Runtime infrastructure required in calculus

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Demo

lect13/method2.key

Localisation of Fields and Method Implementation

JAVA has complex rules for localisation of attributes and method implementations

- Polymorphism
- Late binding
- Scoping (class vs. instance)
- Context (static vs. runtime)
- Visibility (private, protected, public)

Use information from semantic analysis of compiler framework Proof split into cases when implementation not statically determined

Null pointer exceptions

There are no "exceptions" in FOL: \mathcal{I} total on FSym Need to model possibility that $o \doteq null$ in o.a

- ▶ KeY creates PO for $! \circ \doteq null$ upon each field access
- Can be switched off with option nullPointerPolicy

Object initialization

 $\ensuremath{\mathrm{JAVA}}$ has complex rules for object initialization

- Chain of constructor calls until Object
- Implicit calls to super()
- Visbility issues
- Initialization sequence

Coding of initialization rules in methods <createObject>(), <init>(),... which are then symbolically executed

A Round Tour of Java Features in DL Cont'd

Formal specification of Java API

How to perform symbolic execution when JAVA API method is called?

1. API method has reference implementation in JAVA Call method and execute symbolically

Problem Reference implementation not always available **Problem** Too expensive

- 2. Use JML contract of API method:
 - 2.1 Show that requires clause is satisfied
 - 2.2 Obtain postcondition from ensures clause
 - 2.3 Delete updates with modifiable locations from symbolic state

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Java Card API in JML or DL

DL version available in KeY, JML work in progress See W. Mostowski

www.cs.ru.nl/~woj/software/software.html

- Most JAVA features covered in KeY
- Several of remaining features available in experimental version
 - Simplified multi-threaded JMM
 - Floats
- Degree of automation for loop-free programs is high
- Proving loops requires user to provide invariant
 - Automatic invariant generation sometimes possible
- Symbolic execution paradigm lets you use KeY w/o understanding details of logic

Essential

KeY Book Verification of Object-Oriented Software (see course web page), Chapter 3: Dynamic Logic, Sections 3.6.1, 3.6.2, 3.6.5, 3.6.7

Recommended

KeY Book Verification of Object-Oriented Software (see course web page), Chapter 3: Dynamic Logic, Section 3.9