

---

**Formal Specification of Software**

# **UML State Machines**

**Bernhard Beckert**



**UNIVERSITÄT KOBLENZ-LANDAU**

# UML State Machines

---

**Important type of UML diagrams**

**For modelling behaviour**

- **Lifecycle of objects**
- **Behaviour of operations**

**History**

- **Invented by D. Harel (State Charts)**
- **Made popular by J. Rumbaugh (OMT)**

# Notions Related to State Machines

---

- **State**
- **Transition**
- **Event**
- **Action, Activity**
- **Guards**
- **Sending messages**
- **Nesting**
- **Concurrency**
- **History states**

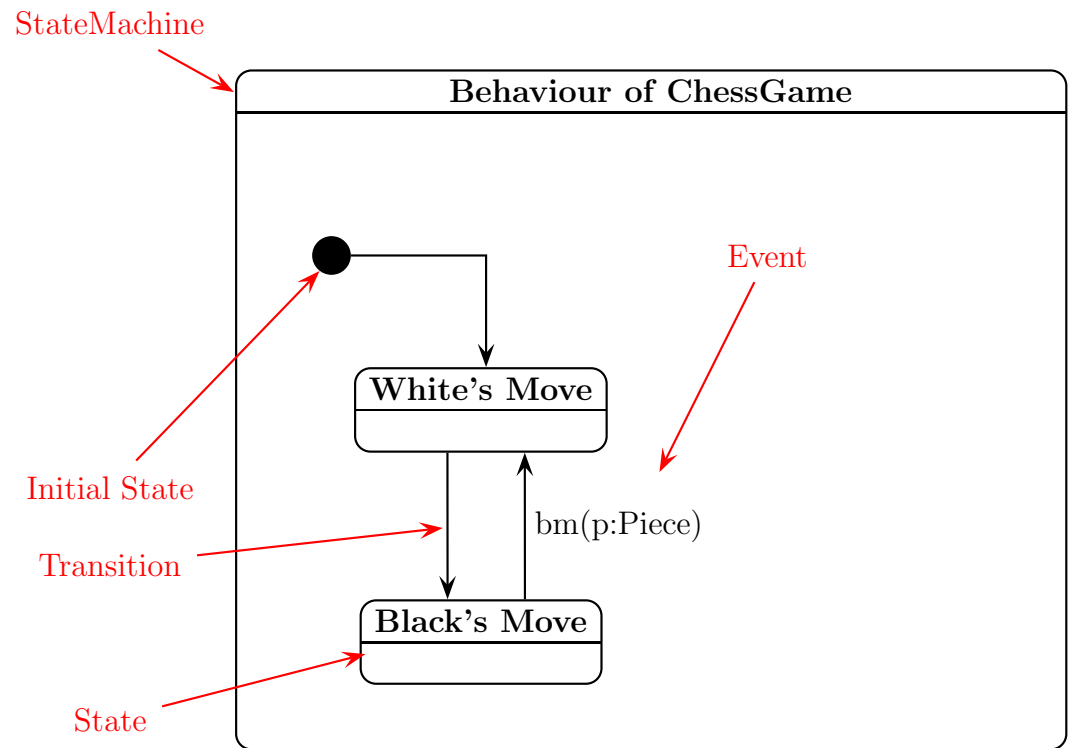
# Example: Chess

---

A chess game consists  
of alternate moves of  
Black and White. White  
moves first.

# Example: Chess

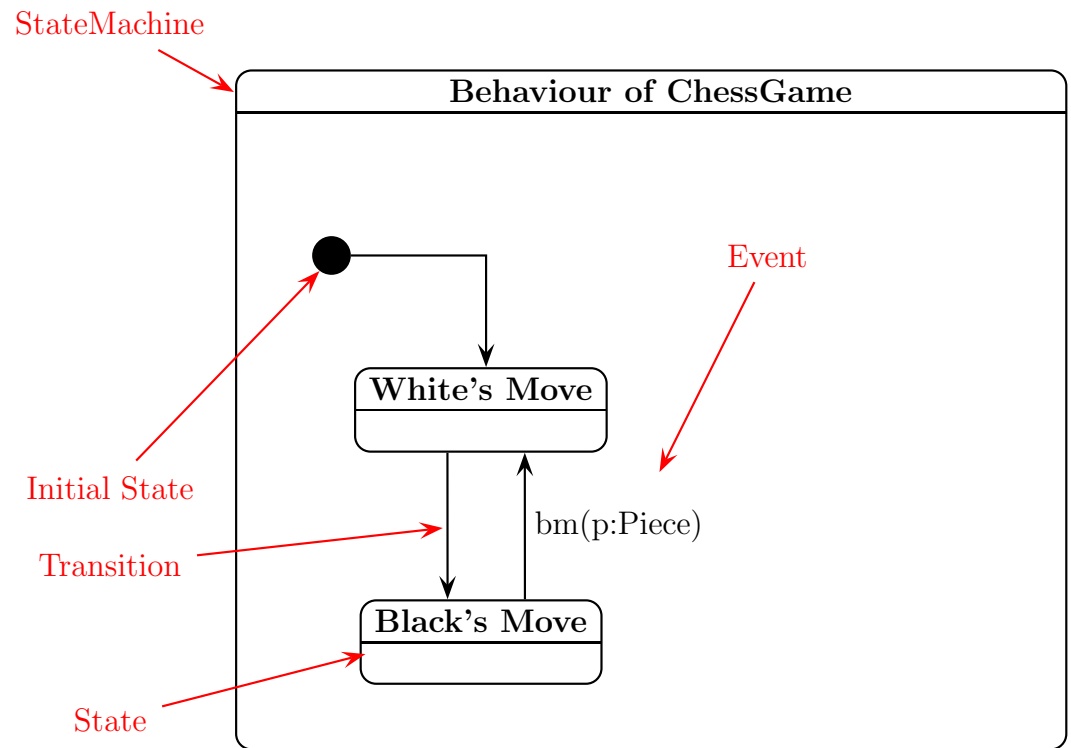
A chess game consists of alternate moves of Black and White. White moves first.



# Example: Chess

A chess game consists of alternate moves of Black and White. White moves first.

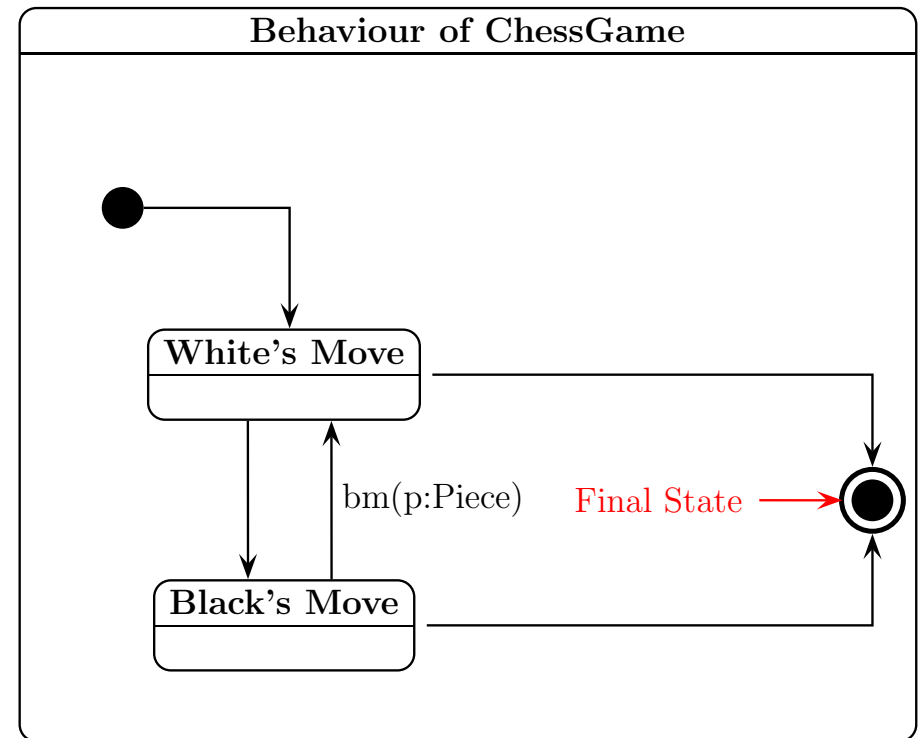
The game can end both when it is White's and when it is Black's turn.



# Example: Chess

A chess game consists of alternate moves of Black and White. White moves first.

The game can end both when it is White's and when it is Black's turn.

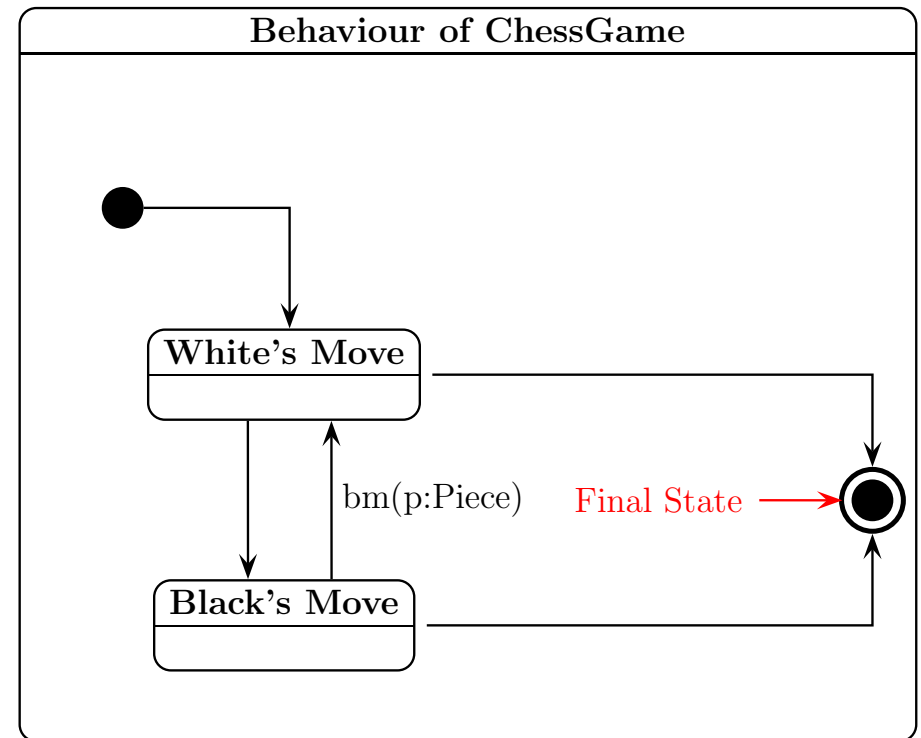


# Example: Chess

A chess game consists of alternate moves of Black and White. White moves first.

The game can end both when it is White's and when it is Black's turn.

The moving player can end the game: winning (checkmate),



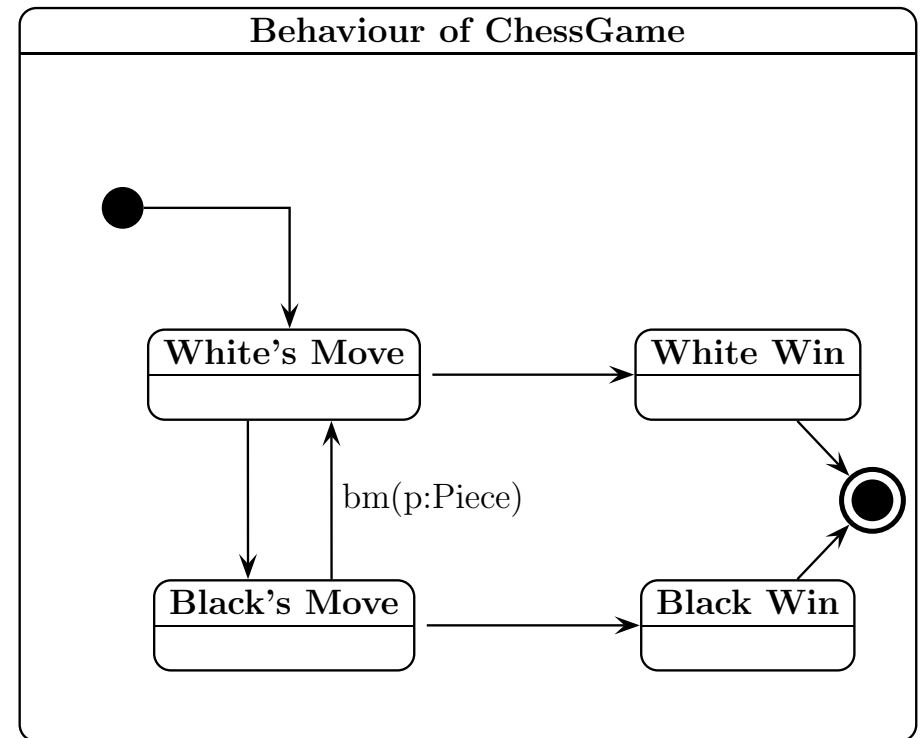


# Example: Chess

A chess game consists of alternate moves of Black and White. White moves first.

The game can end both when it is White's and when it is Black's turn.

The moving player can end the game: winning (checkmate),



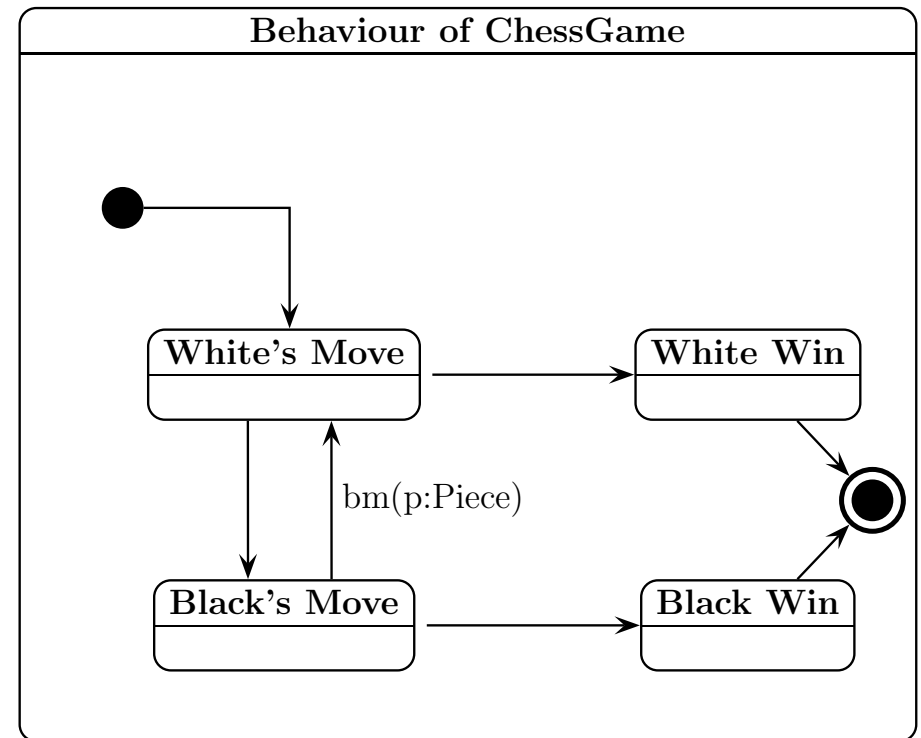
# Example: Chess

A chess game consists of alternate moves of Black and White. White moves first.

The game can end both when it is White's and when it is Black's turn.

The moving player can end the game: winning (checkmate),

loosing (resign),

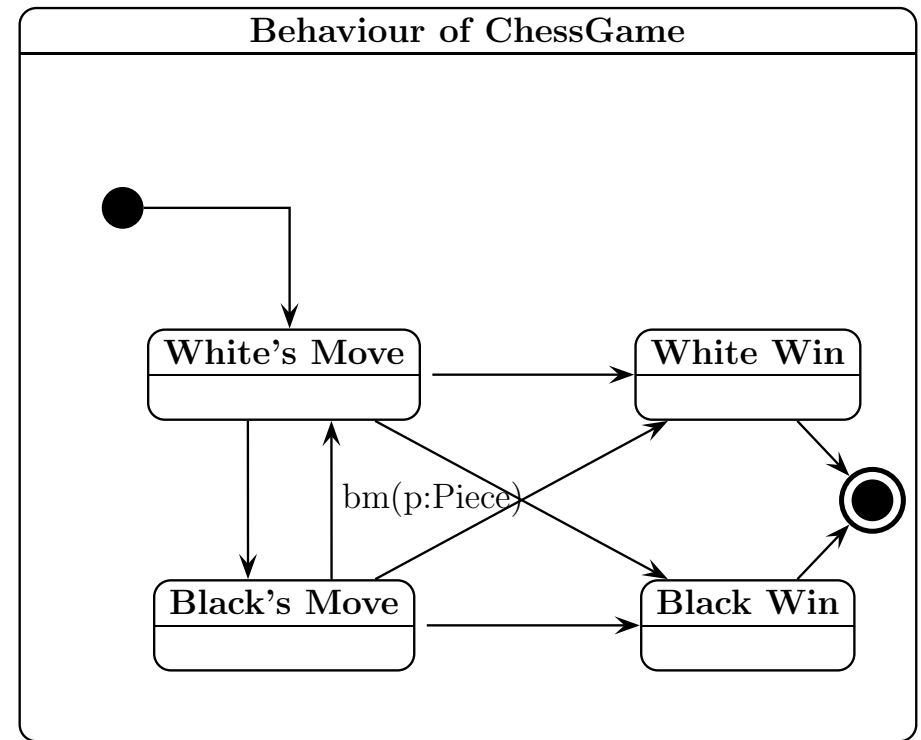


# Example: Chess

A chess game consists of alternate moves of Black and White. White moves first.

The game can end both when it is White's and when it is Black's turn.

The moving player can end the game: winning (checkmate), loosing (resign),



# Example: Chess

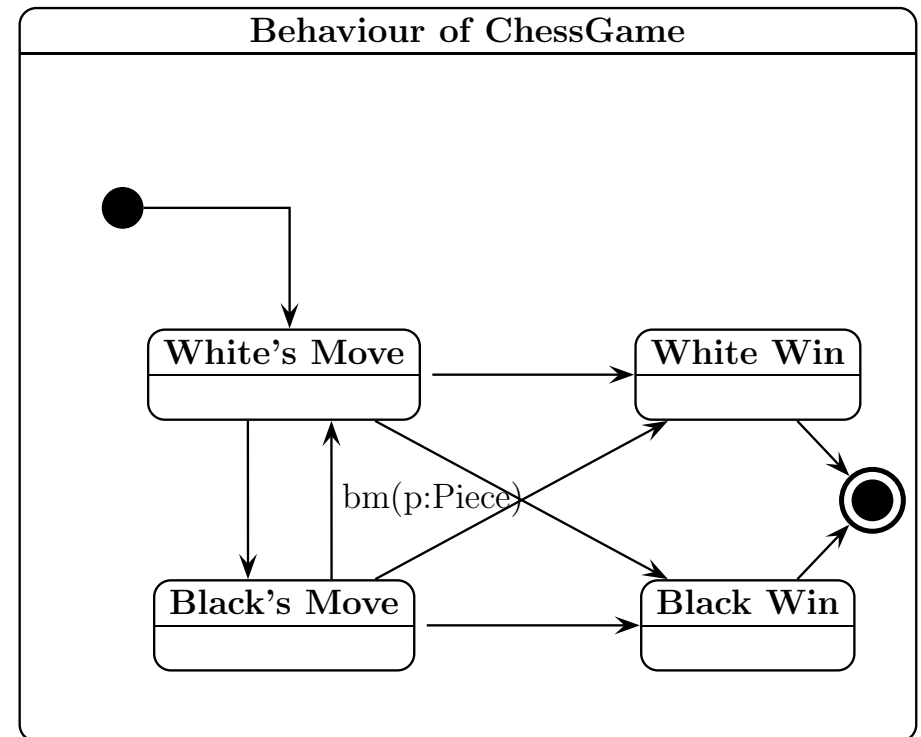
A chess game consists of alternate moves of Black and White. White moves first.

The game can end both when it is White's and when it is Black's turn.

The moving player can end the game: winning (checkmate),

loosing (resign),

or with a draw.



# Example: Chess

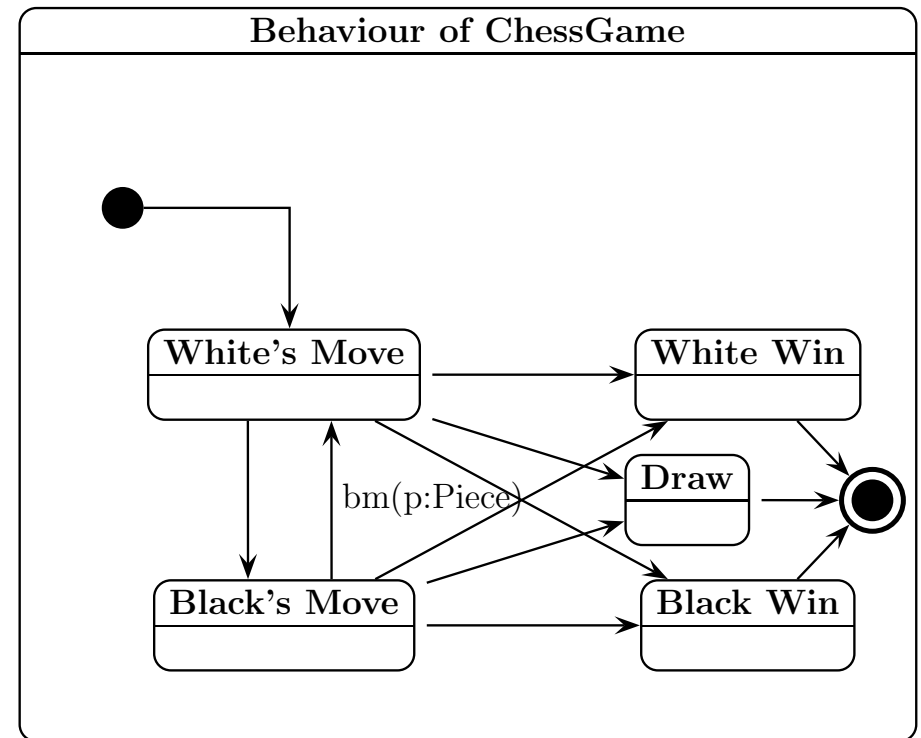
A chess game consists of alternate moves of Black and White. White moves first.

The game can end both when it is White's and when it is Black's turn.

The moving player can end the game: winning (checkmate),

loosing (resign),

or with a draw.



# State Machines

---

## State Machine

**Labelled, finite graph (cycles possible)**

# State Machines

---

## State Machine

**Labelled, finite graph (cycles possible)**

## States

**Nodes of the graph**

**Labelled with: name, do-, entry-, exit-action, ...**

**Initial and final states have special shapes**

# State Machines

---

## State Machine

Labelled, finite graph (cycles possible)

## States

Nodes of the graph

Labelled with: name, do-, entry-, exit-action, ...

Initial and final states have special shapes

## Transitions

Edges of the graph

Labelled with: event, guard, action, ...



# When to Use State Machines

---

## Use State Machines ...

- at an early stage of software development
- when behaviour of an object (lifecycle) or operation is not well understood yet

# When to Use State Machines

---

## Use State Machines ...

- at an early stage of software development
- when behaviour of an object (lifecycle) or operation is not well understood yet

## Do **NOT** use State Machines ...

- when several objects are involved (interaction diagrams are better)

# State

---

## Abstract view

- the same response to the same stimuli
- the same active behaviour

# State

---

## Abstract view

- the same response to the same stimuli
- the same active behaviour

## Implementation view

- certain attributes have certain values

# Event

---

## Properties

- **observable in the environment of the current object**
- **takes place at certain point in time (has no duration)**
- **has possibly parameters**

# Event

---

## Properties

- **observable in the environment of the current object**
- **takes place at certain point in time (has no duration)**
- **has possibly parameters**

## Role in diagram

- **triggers a transition**
- **is “consumed” when transition is executed**
- **can be saved under certain circumstances**

# Types of Events

---

## Signal event

**An object that is dispatched (thrown) and received (caught)**

## Call event

**Represents the dispatch of an operation**

## Time event

**Represents the passage of a certain amount of time**

## Change event

**Represents the fact that a Boolean expression is changed to `true`**

**The expression is checked continuously (polling)**

# Transition

---

## Properties

- describes change from one state to another state
- without duration when executed



# Transition

---

## Properties

- describes change from one state to another state
- without duration when executed

## Role in diagram

- triggering controlled by events, guards, state exit conditions
- execution can cause actions

# Example: ATM

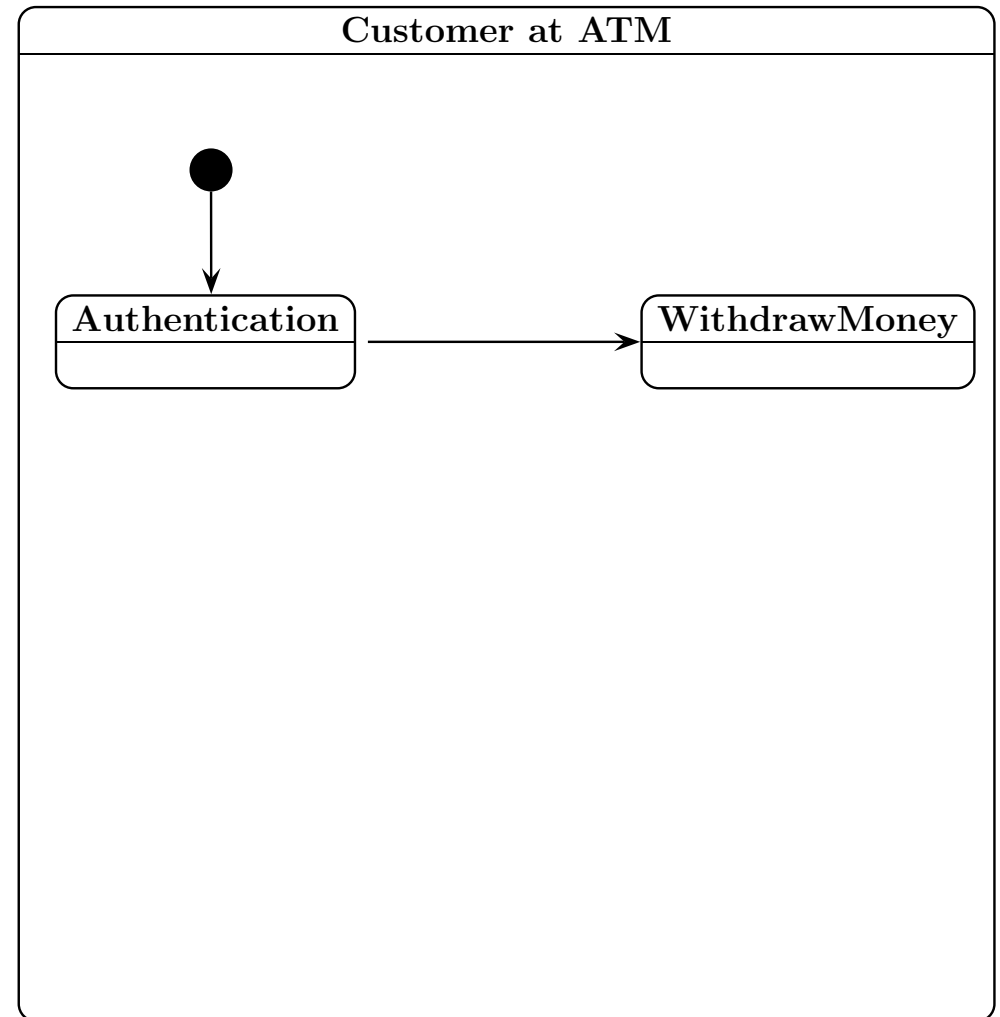
---

The customer must pass authentication before withdrawing money.

# Example: ATM

---

The customer must pass authentication before withdrawing money.

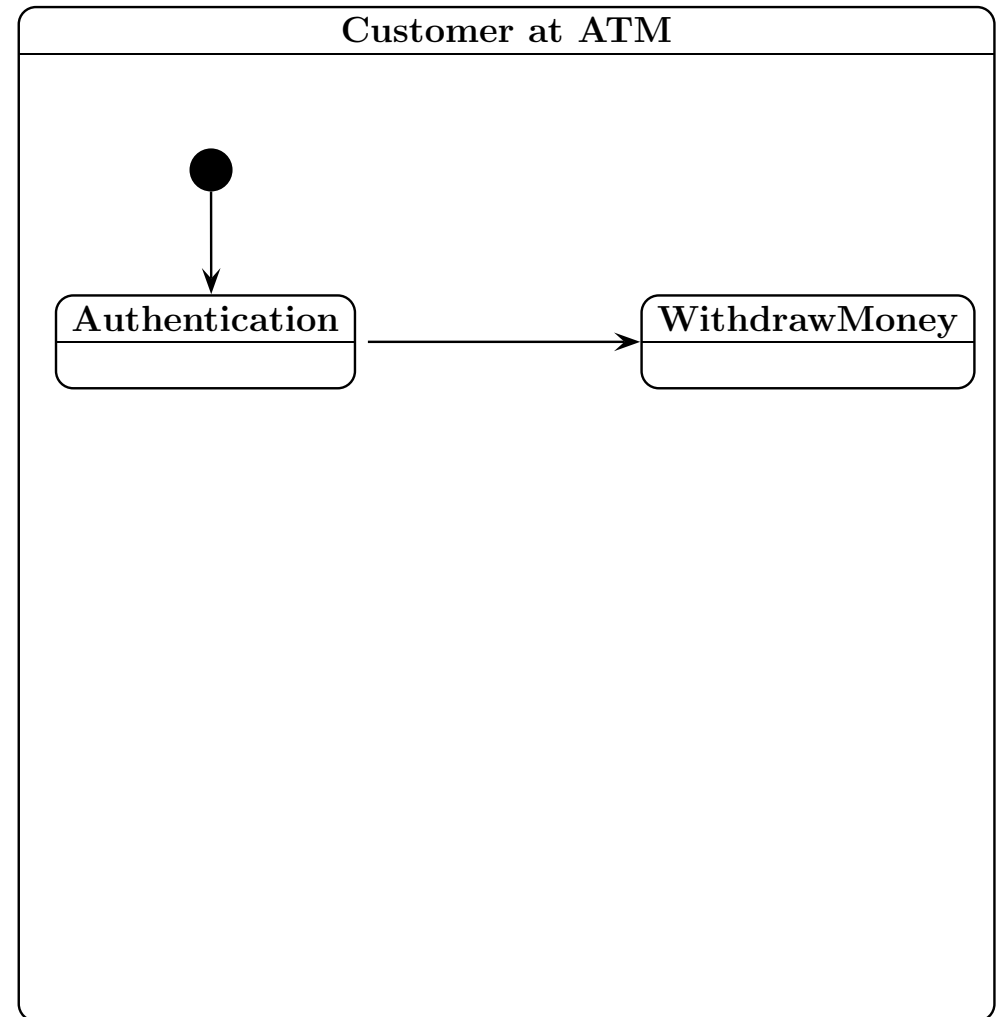


# Example: ATM

---

The customer must pass authentication before withdrawing money.

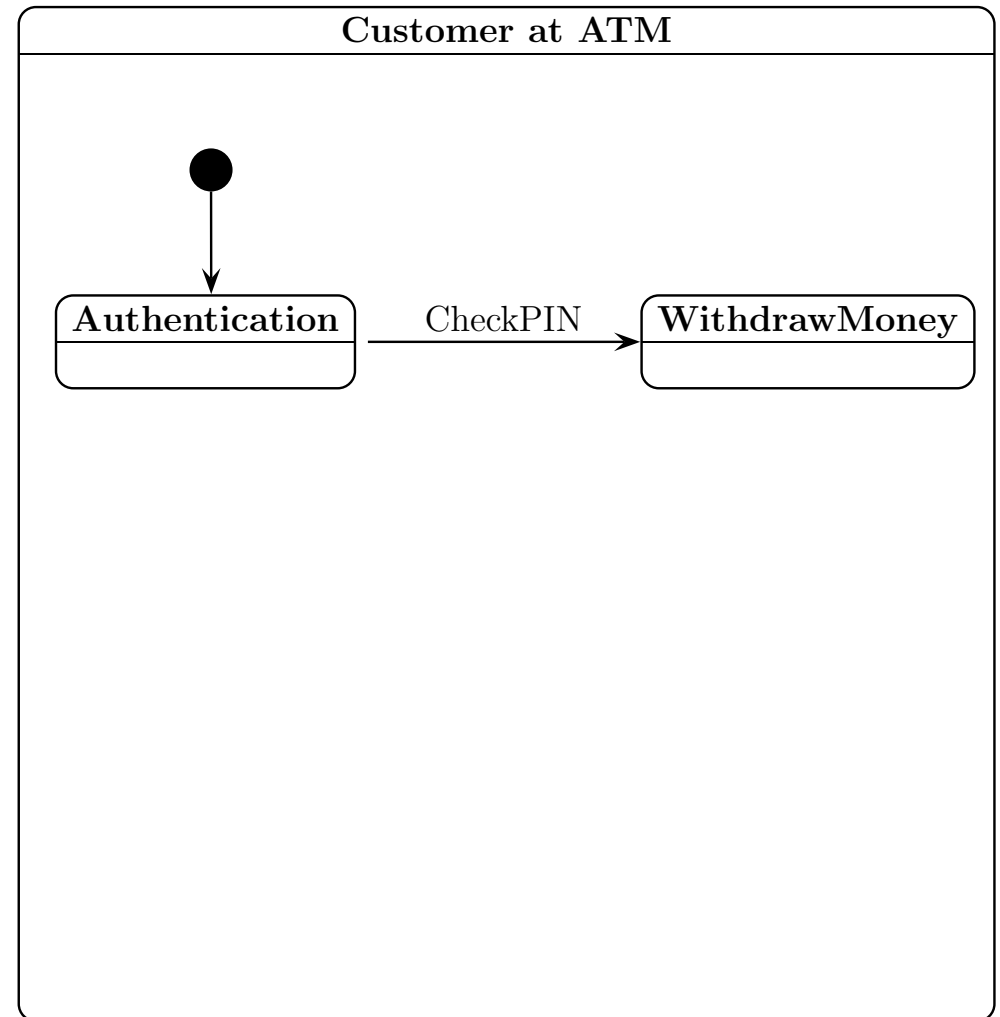
Authentication is done by checking a PIN.



# Example: ATM

---

The customer must pass authentication before withdrawing money. Authentication is done by checking a PIN.



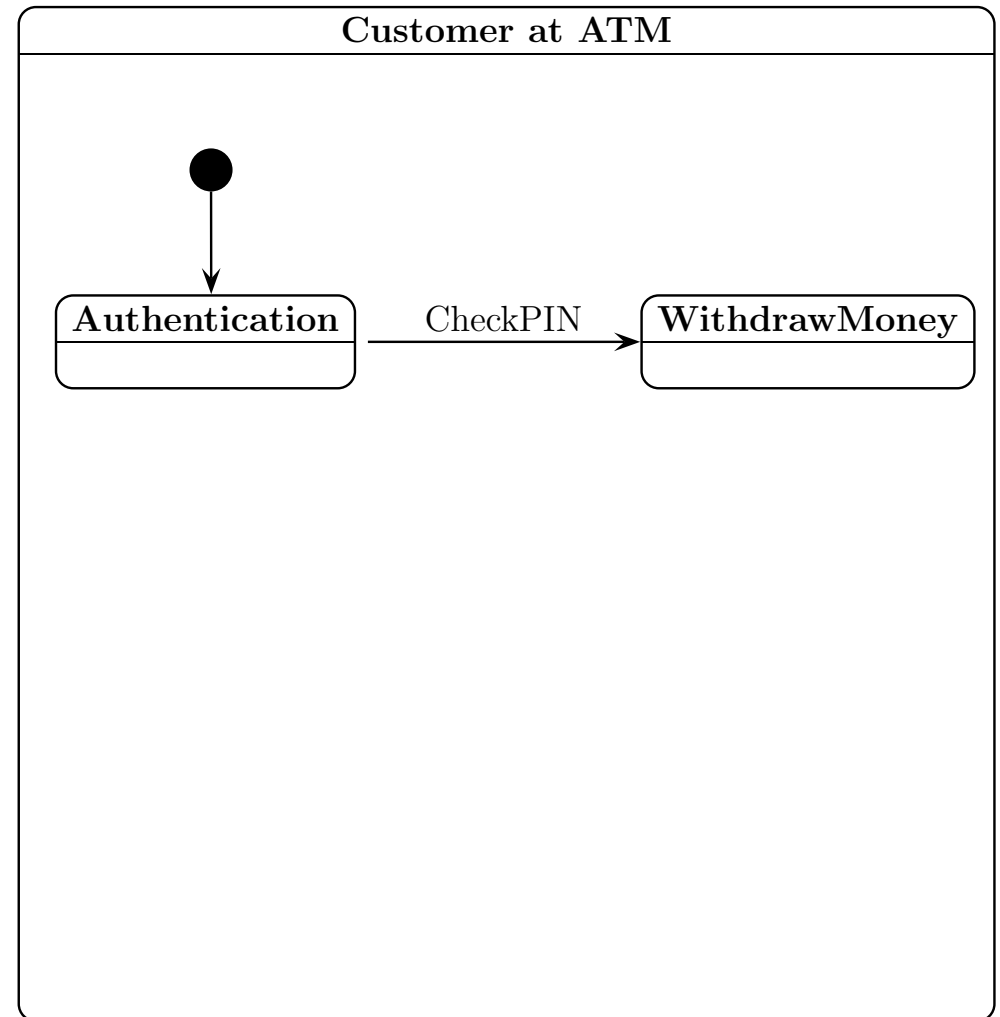
# Example: ATM

---

The customer must pass authentication before withdrawing money.

Authentication is done by checking a PIN.

The PIN can be correct or not.



# Example: ATM

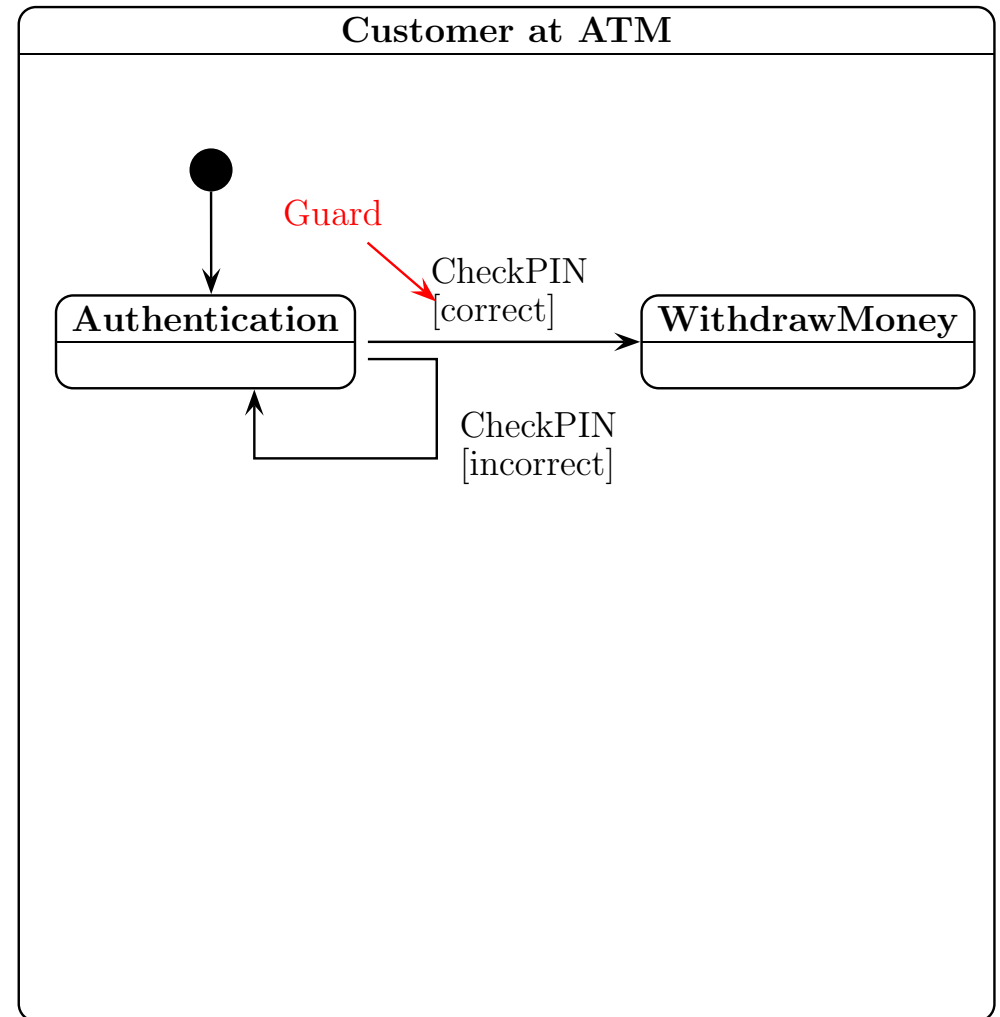
The customer must pass

authentication before

withdrawing money.

Authentication is done by  
checking a PIN.

The PIN can be correct or  
not.



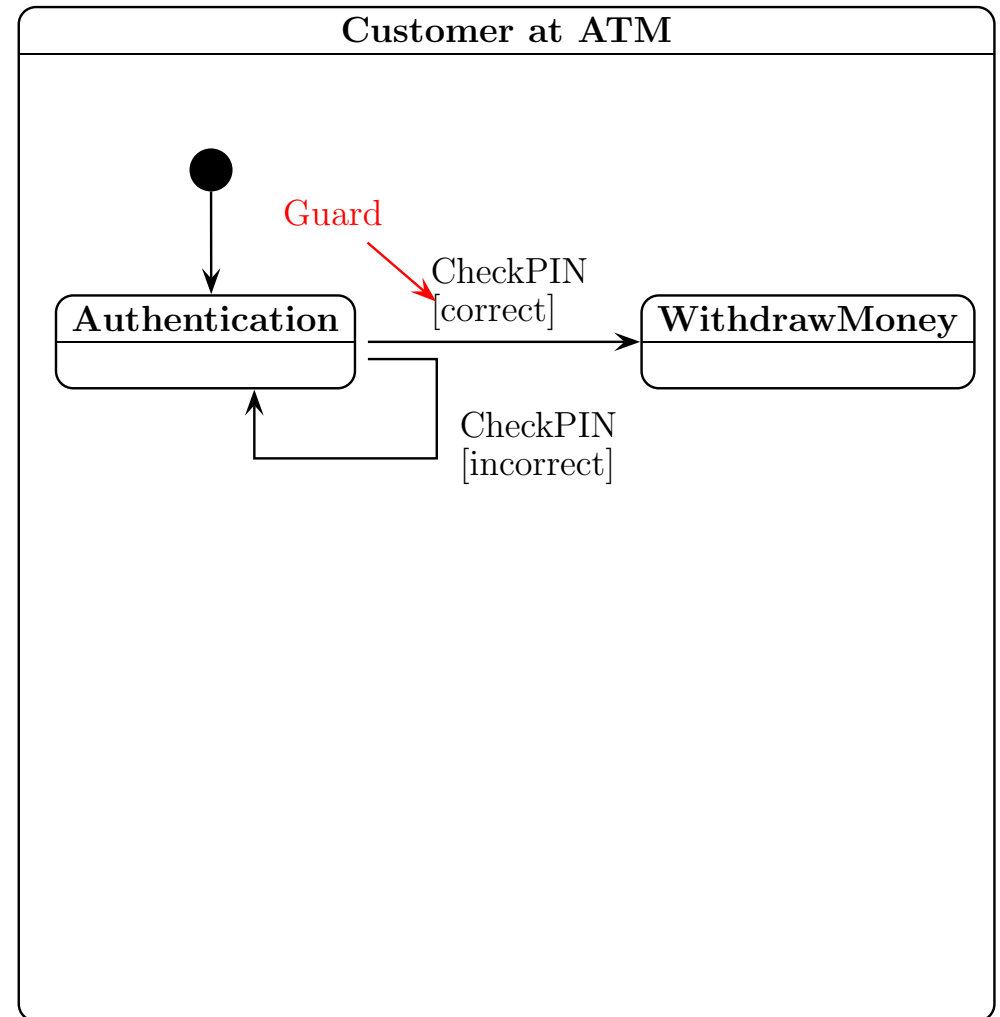
# Example: ATM

The customer must pass authentication before withdrawing money.

Authentication is done by checking a PIN.

The PIN can be correct or not.

Unsuccessful attempts are counted,





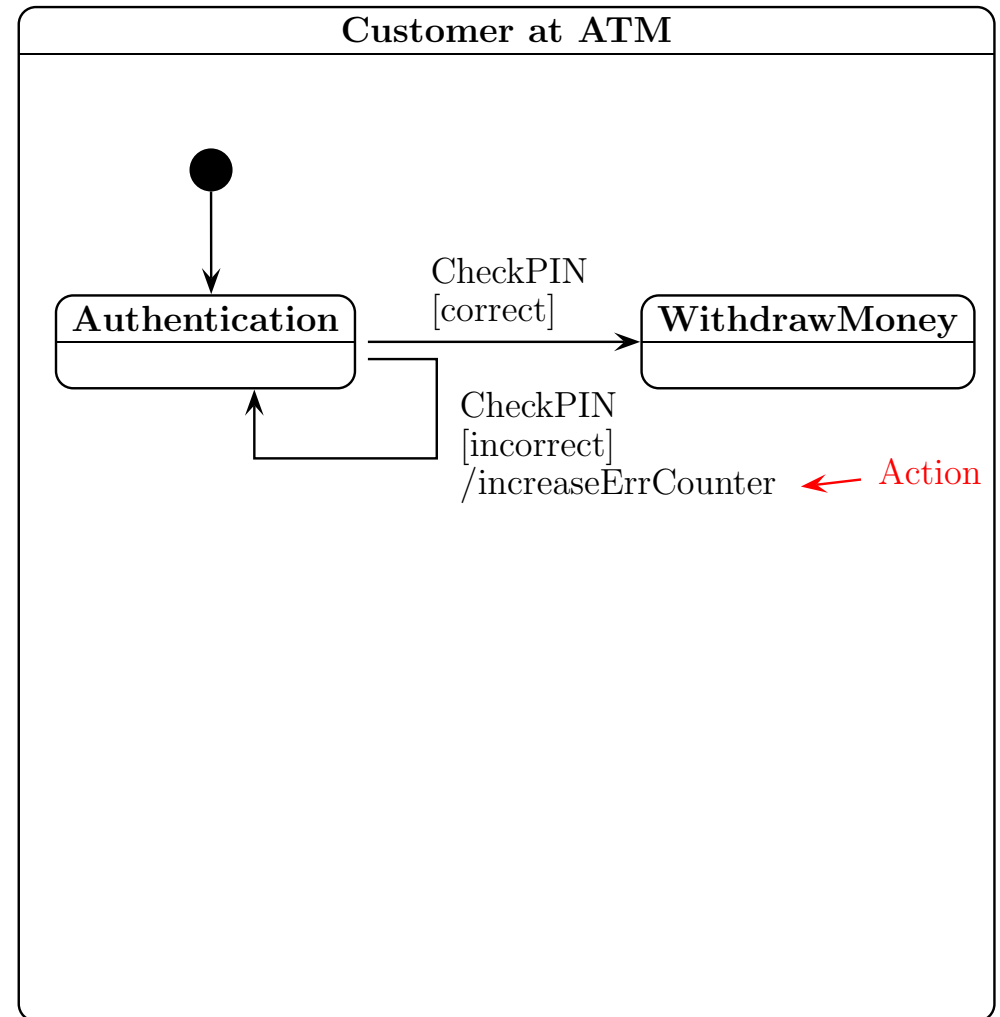
# Example: ATM

The customer must pass authentication before withdrawing money.

Authentication is done by checking a PIN.

The PIN can be correct or not.

Unsuccessful attempts are counted,



# Example: ATM

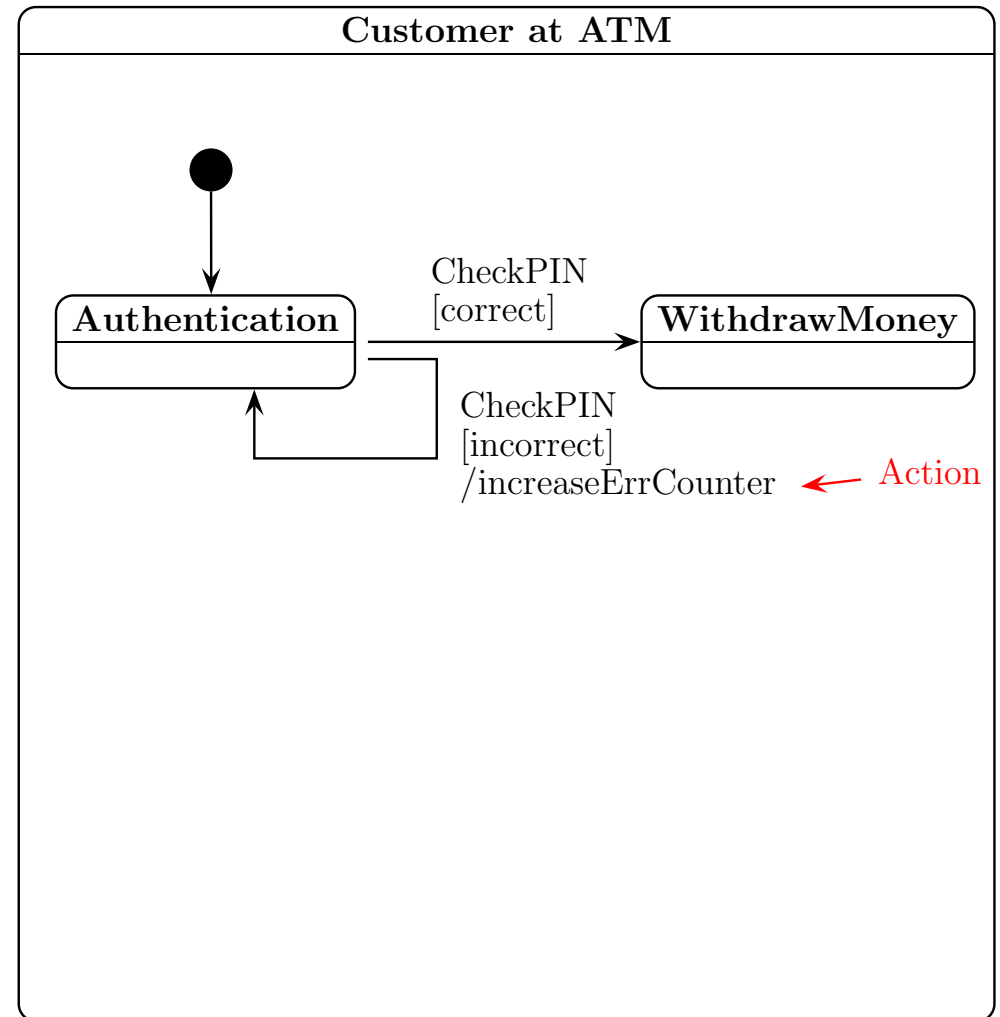
The customer must pass authentication before withdrawing money.

Authentication is done by checking a PIN.

The PIN can be correct or not.

Unsuccessful attempts are counted,

If the counter exceeds a limit, the customer is rejected.



# Example: ATM

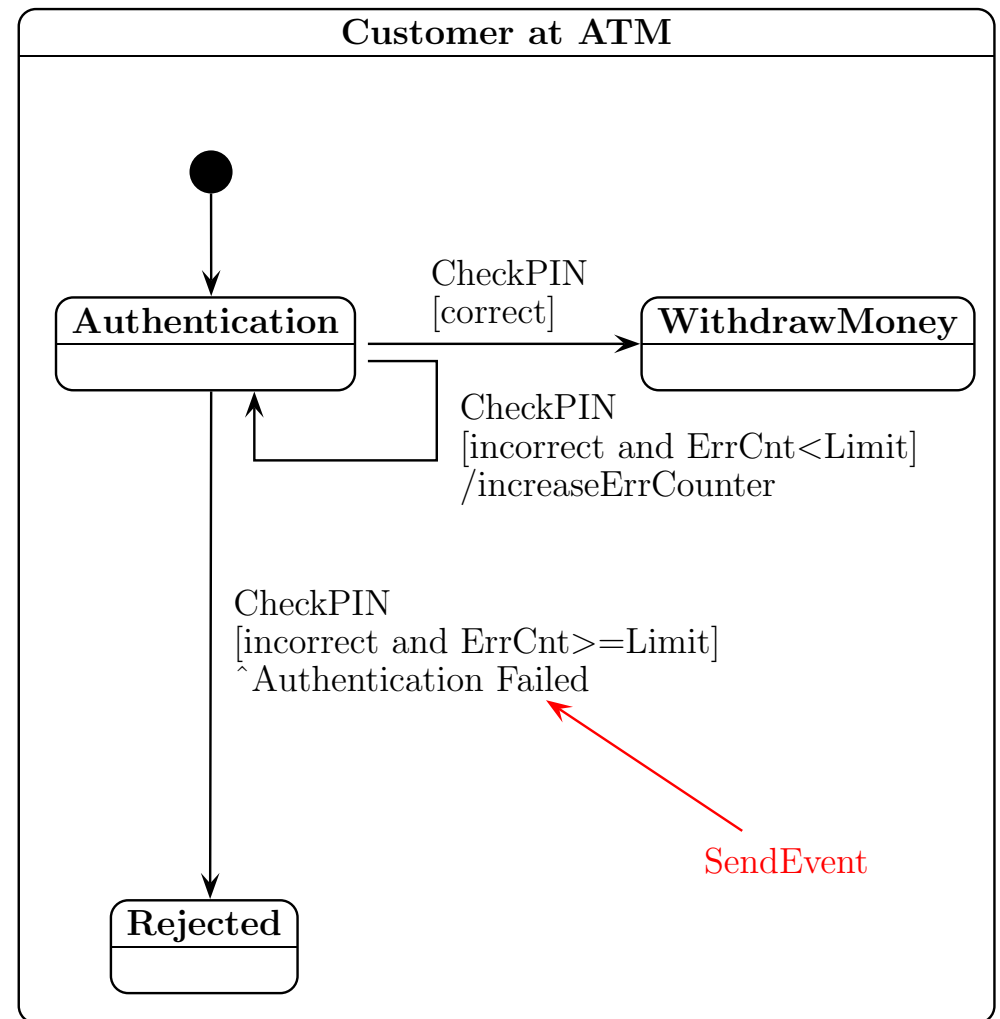
The customer must pass authentication before withdrawing money.

Authentication is done by checking a PIN.

The PIN can be correct or not.

Unsuccessful attempts are counted,

If the counter exceeds a limit, the customer is rejected.



# Internal Transitions

---

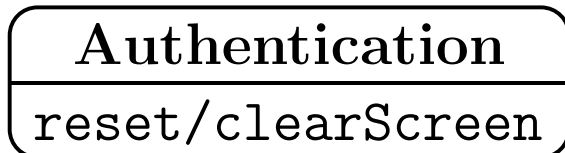
## Notation

Written as

*Event[Guard]/Action*

within the state box

## Example



## Difference to self transition

Entry and exit actions are not dispatched

# Entry and Exit Actions

---

## Notation

### Written as

entry/*Action*      **resp.**  
exit/*Action*

### within the state box

## Semantics

Dispatched on entering resp. exiting the state

# Activities

---

## Notation

**Written as**

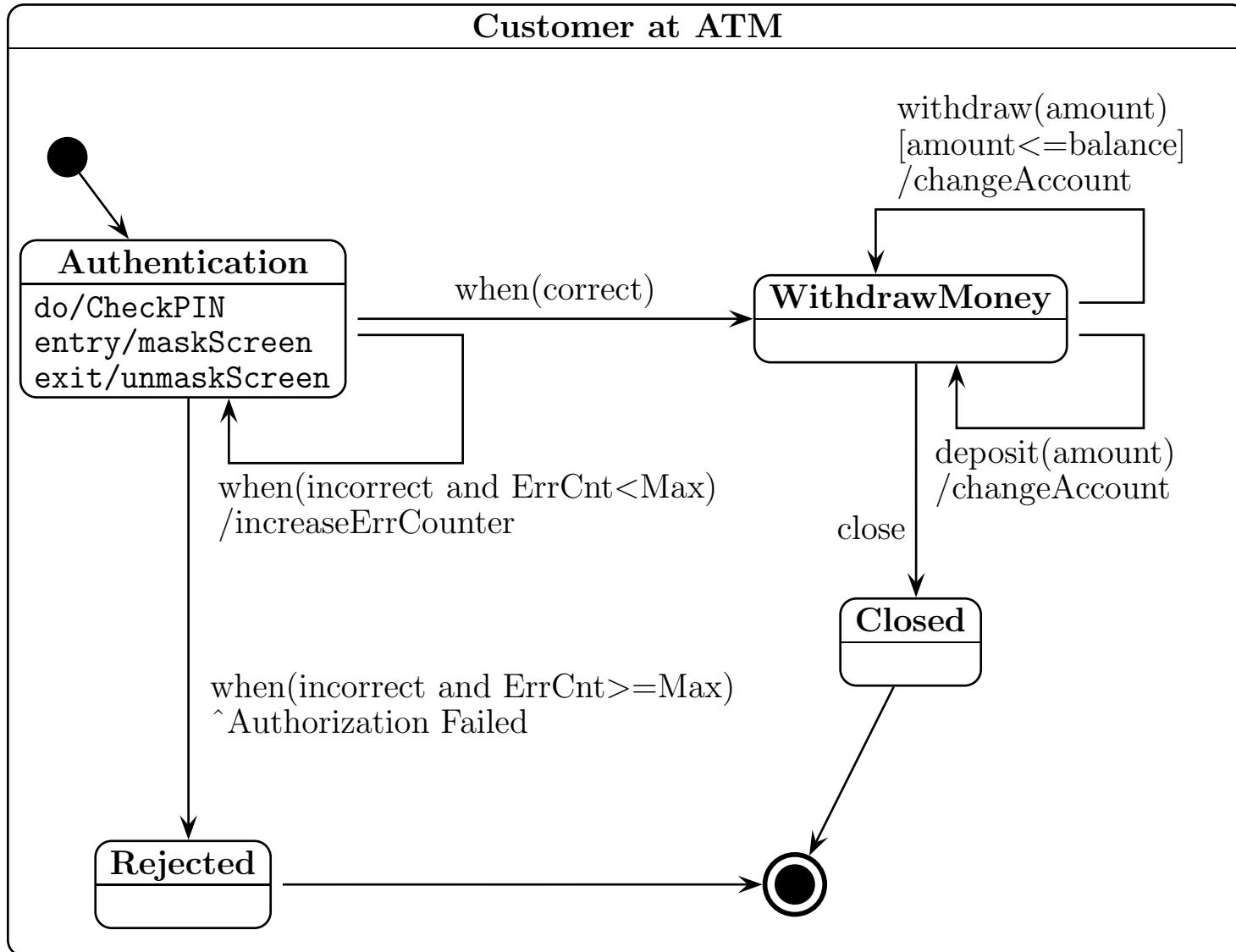
*do/Action*

**within the state box**

## Semantics

- **have duration**
- **can be finished by event for outgoing transitions**

# Example: ATM (Alternative Formalisation)



# Exercise

---

**A student must complete the basic level before entering the advanced level.**

**After both levels, the student has to pass five examinations.**

**An examination can be retaken at most twice.**

**After the third failed attempt the student's registration is cancelled.**



# Exercise: Student

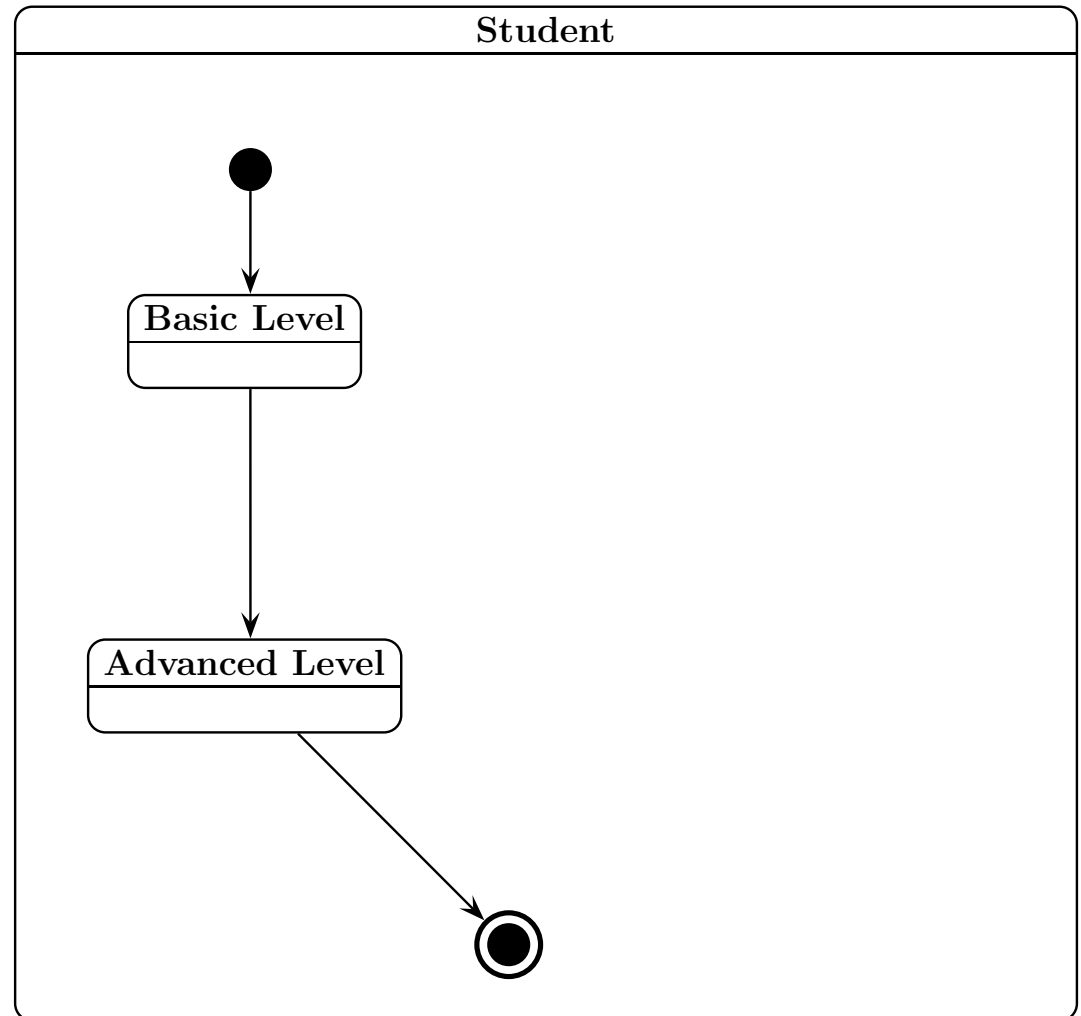
---

**A student must complete  
the basic level before  
entering the advanced level.**

# Exercise: Student

---

A student must complete the basic level before entering the advanced level.

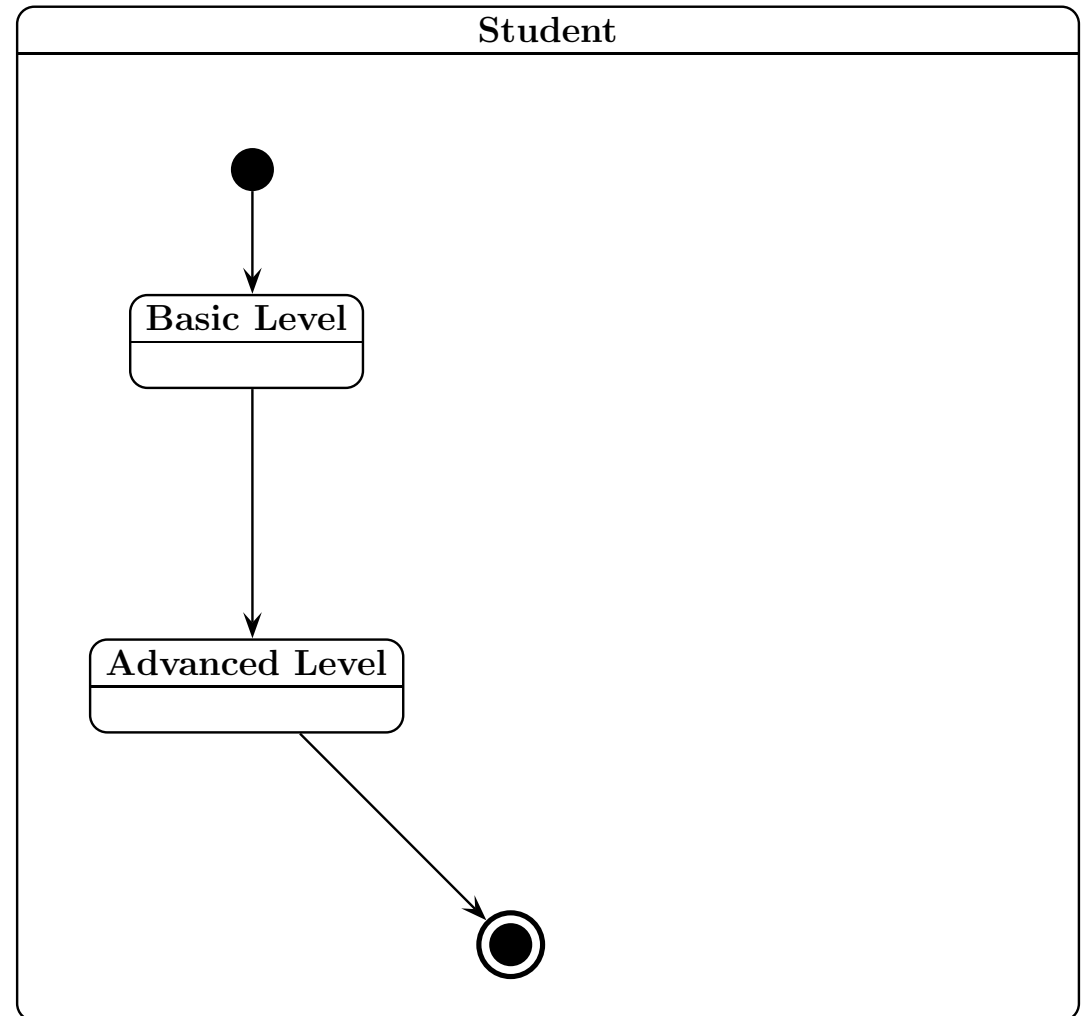


# Exercise: Student

---

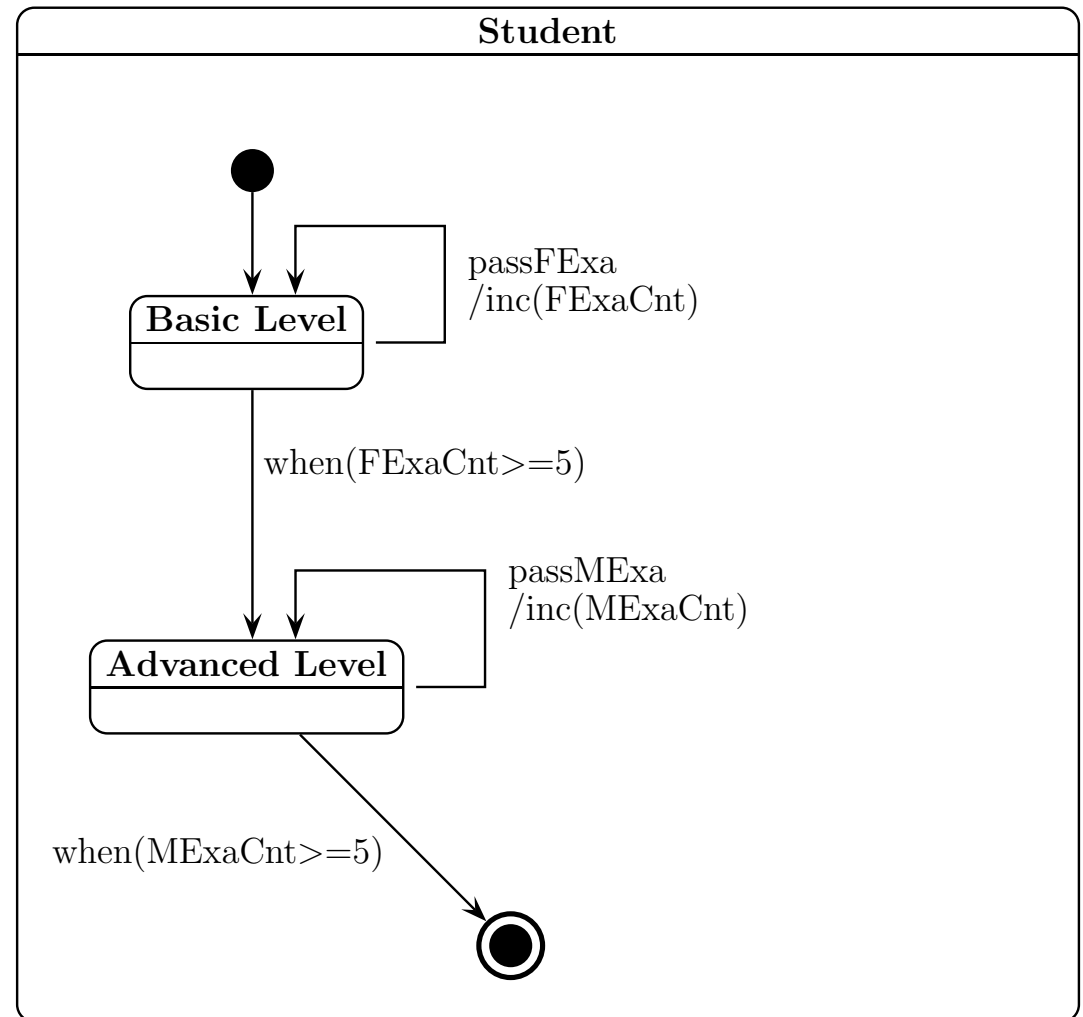
A student must complete the basic level before entering the advanced level.

After both levels, the student has to pass five examinations.



# Exercise: Student

**A student must complete the basic level before entering the advanced level. After both levels, the student has to pass five examinations.**

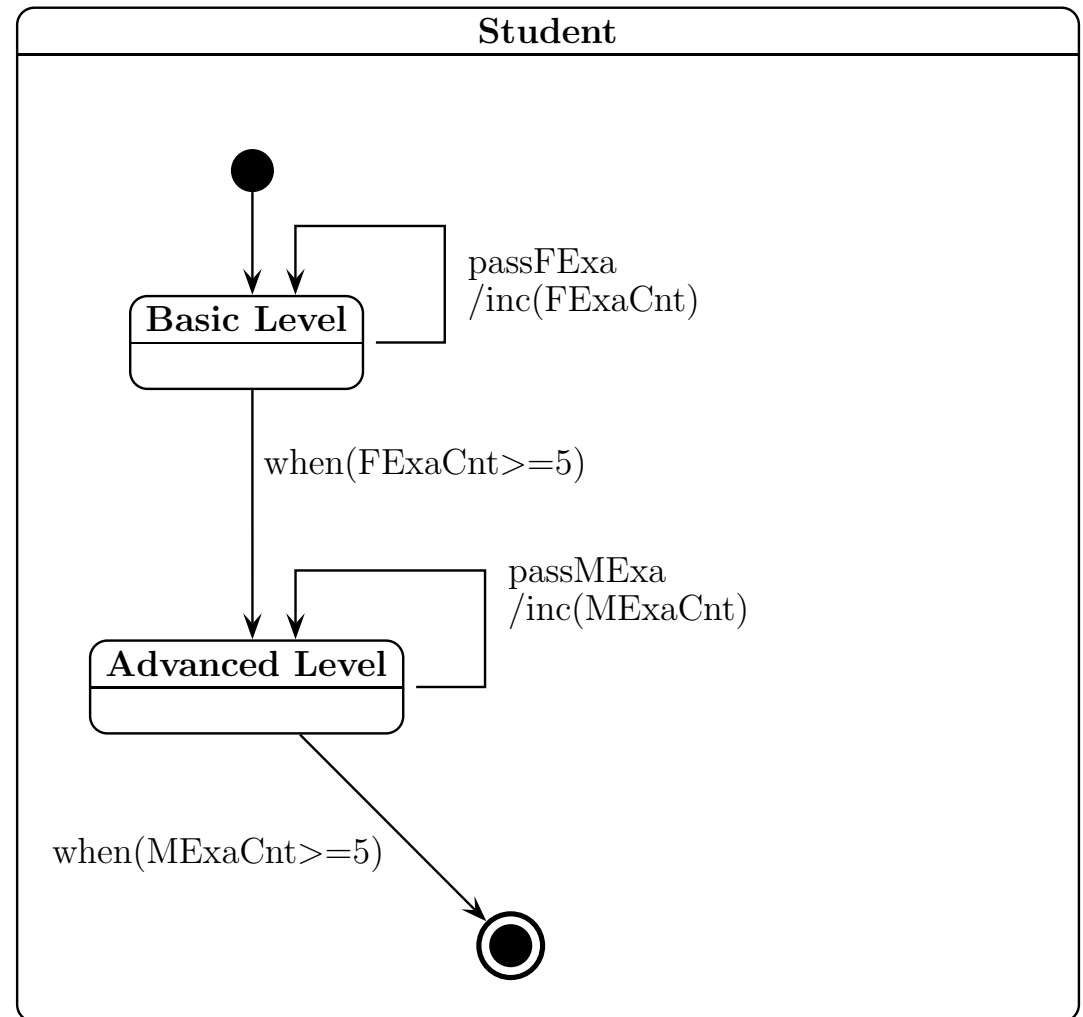


# Exercise: Student

A student must complete the basic level before entering the advanced level.

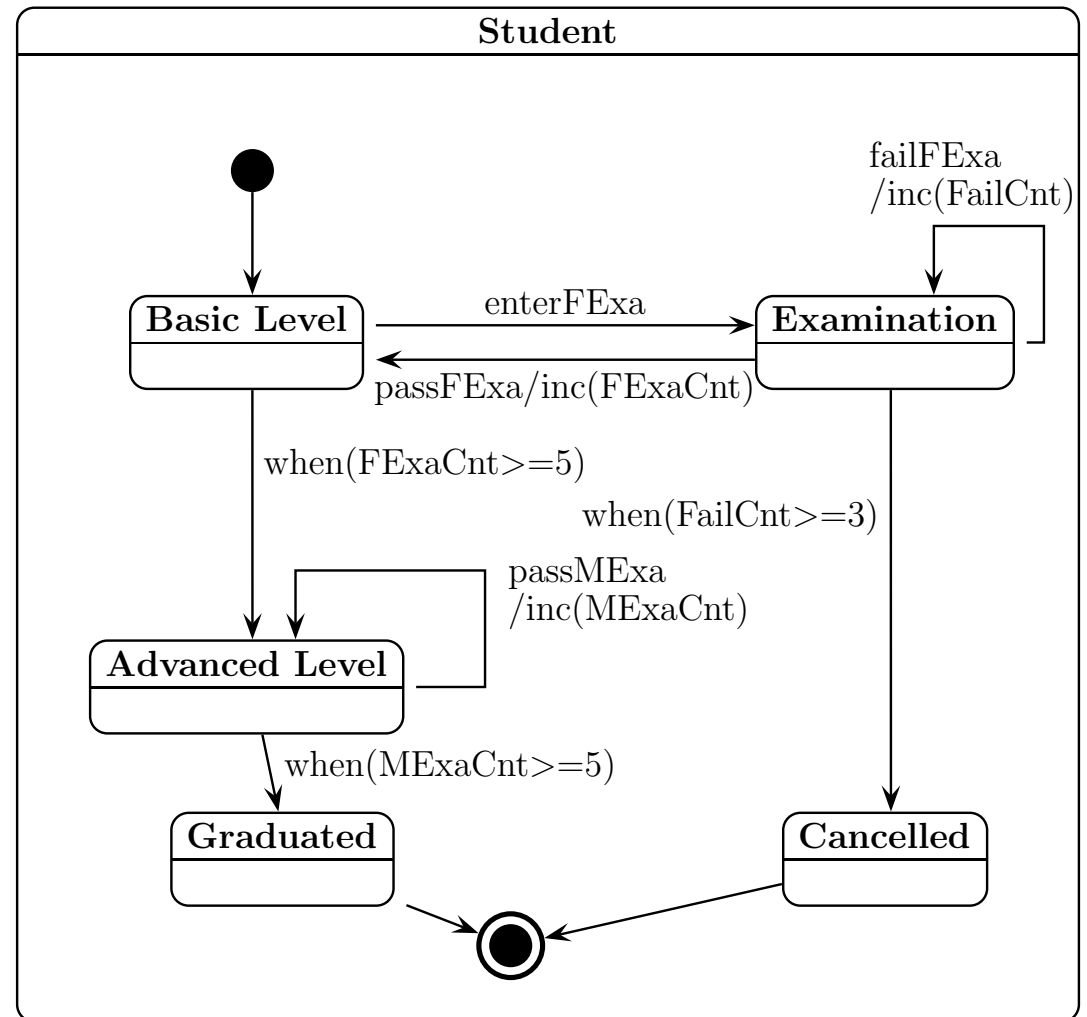
After both levels, the student has to pass five examinations.

An examination can be retaken at most twice. After the third failed attempt the student's registration is cancelled.



# Exercise: Student

A student must complete the basic level before entering the advanced level. After both levels, the student has to pass five examinations. An examination can be retaken at most twice. After the third failed attempt the student's registration is cancelled.



# Criticism

---

**Not really a good model, because ...**

- the student leaves the basic level to take an exam**
- the student can cheat by repeating a passed exam**
- the student cannot enter parallel exams**
- the student has to complete each exam once tried**
- the student cannot pass exams of the advanced level while in the basic level**

# Advanced Constructs Can Help

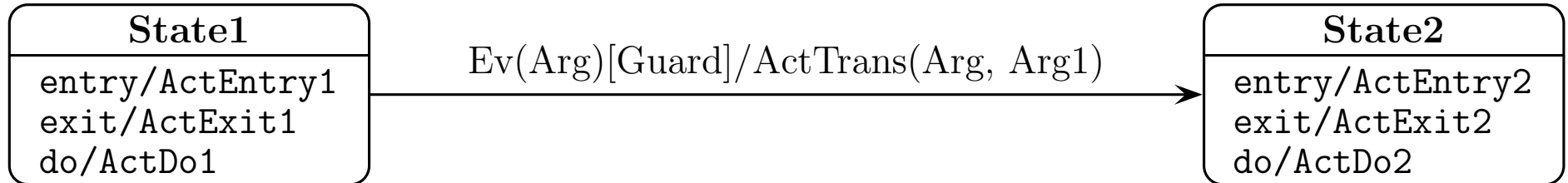
---

- **Deferred event**
- **Composite state**
- **Concurrent composite state**
- **Join state, Fork State**
- **Concurrent transition**
- **Junction state**
- **Sync state**



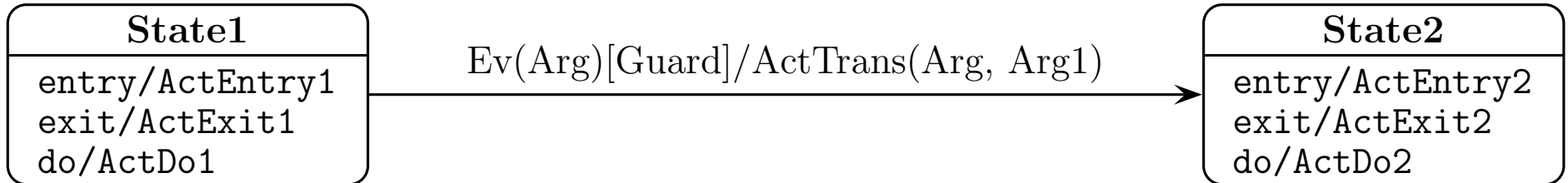
# Events: The Detailed View

---



# Events: The Detailed View

---

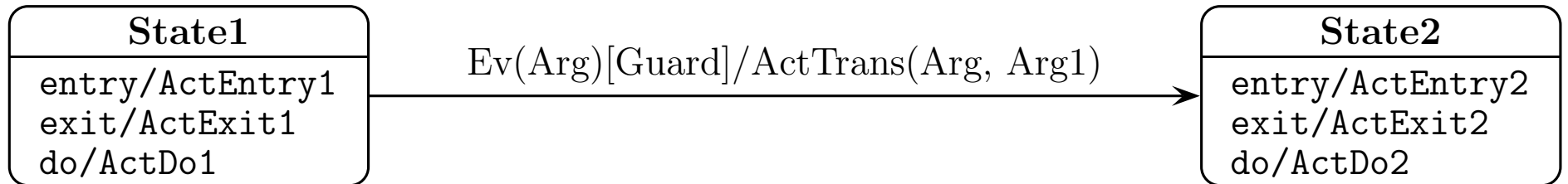


**1. Event is generated:**

**Event raised (somewhere) by some action**

# Events: The Detailed View

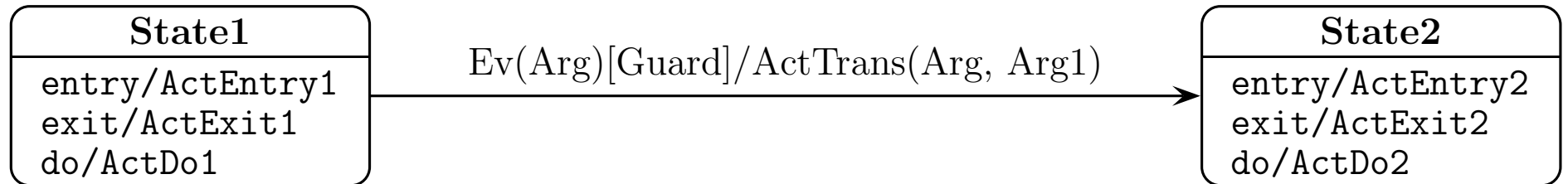
---



- 1. Event is generated:** Event raised (somewhere) by some action
- 2. Event is conveyed:** Event transported to current object (transportation does not change event)

# Events: The Detailed View

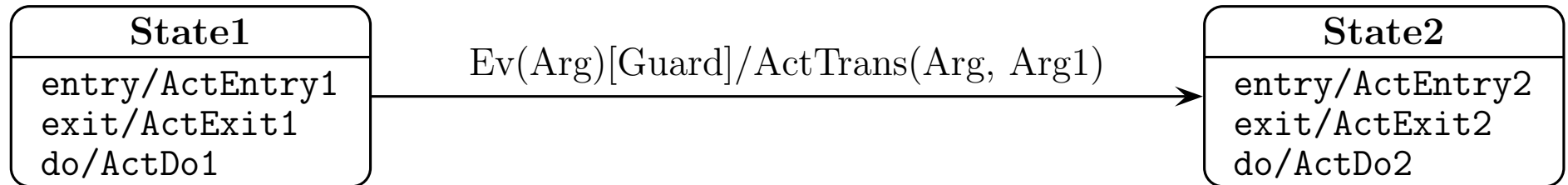
---



- 1. Event is generated:** Event raised (somewhere) by some action
- 2. Event is conveyed:** Event transported to current object (transpotation does not change event)
- 3. Event is received:** Event placed on event queue of current object

# Events: The Detailed View

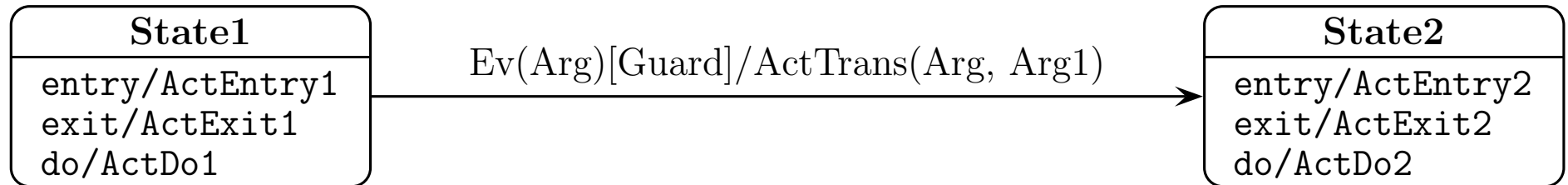
---



- 1. Event is generated:** Event raised (somewhere) by some action
- 2. Event is conveyed:** Event transported to current object (transportation does not change event)
- 3. Event is received:** Event placed on event queue of current object
- 4. Event is dispatched:** Event de-queued from event queue (becomes *current event*)

# Events: The Detailed View

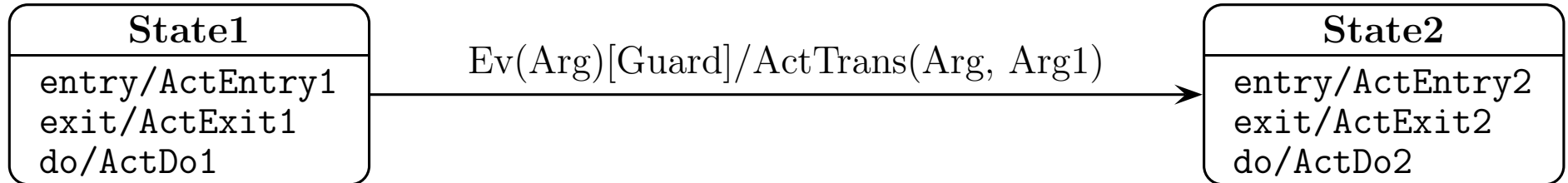
---



- 1. Event is generated:** Event raised (somewhere) by some action
- 2. Event is conveyed:** Event transported to current object (transportation does not change event)
- 3. Event is received:** Event placed on event queue of current object
- 4. Event is dispatched** Event de-queued from event queue (becomes *current event*)
- 5. Event is consumed** Event is processed

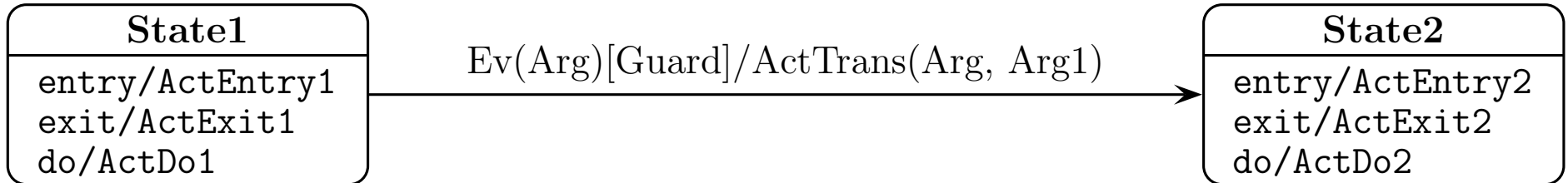
# Event Processing: The Detailed View

---



# Event Processing: The Detailed View

---

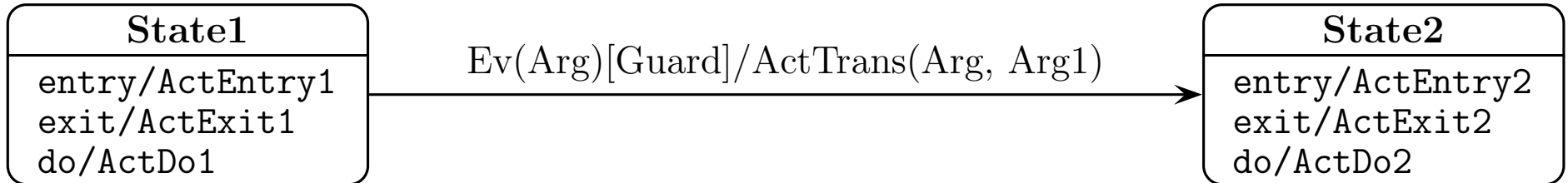


1. **check** Guard – if false **abort**



# Event Processing: The Detailed View

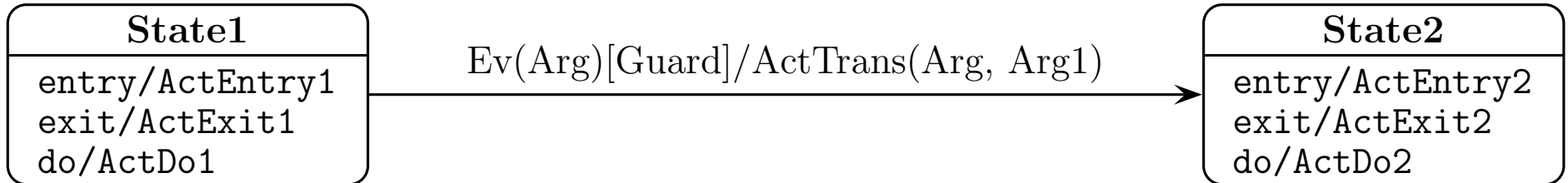
---



1. **check** Guard – if false **abort**
2. **abort** ActDo1

# Event Processing: The Detailed View

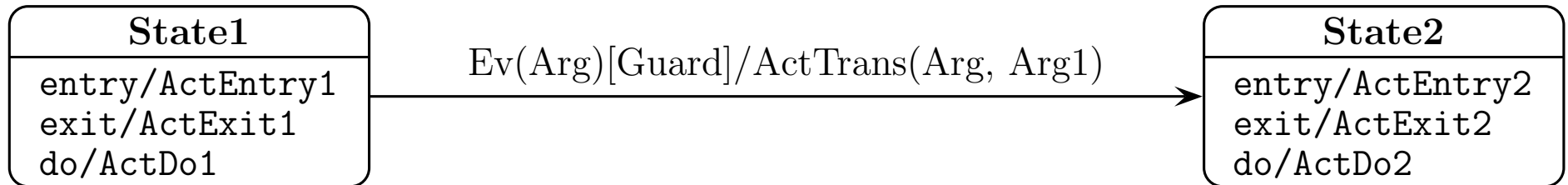
---



1. **check** Guard – if false **abort**
2. **abort** ActDo1
3. **execute** ActExit1

# Event Processing: The Detailed View

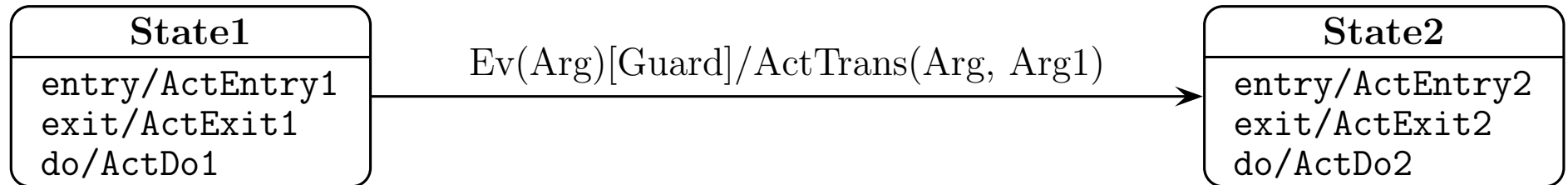
---



1. **check** Guard – if false **abort**
2. **abort** ActDo1
3. **execute** ActExit1
4. **execute** ActTrans(Arg, Arg1)  
(synchronous processing, i.e. wait until finished)

# Event Processing: The Detailed View

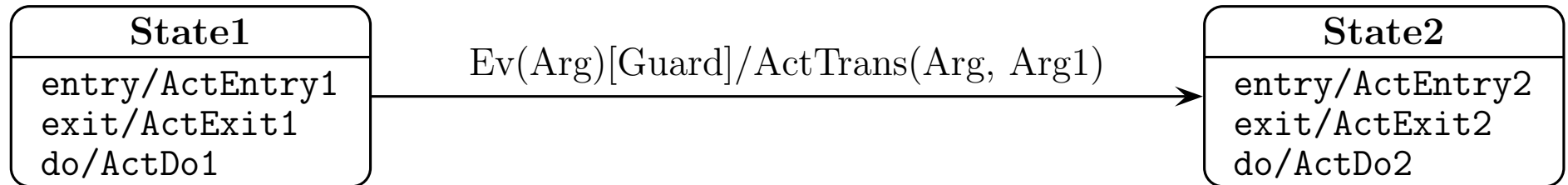
---



1. **check** Guard – if false **abort**
2. **abort** ActDo1
3. **execute** ActExit1
4. **execute** ActTrans(Arg, Arg1)  
(synchronous processing, i.e. wait until finished)
5. **execute** ActEntry2

# Event Processing: The Detailed View

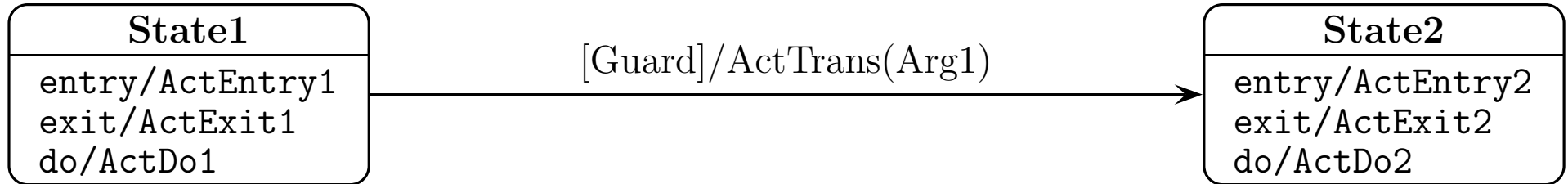
---



1. **check** Guard – if false **abort**
2. **abort** ActDo1
3. **execute** ActExit1
4. **execute** ActTrans(Arg, Arg1)  
(synchronous processing, i.e. wait until finished)
5. **execute** ActEntry2
6. **execute** ActDo2

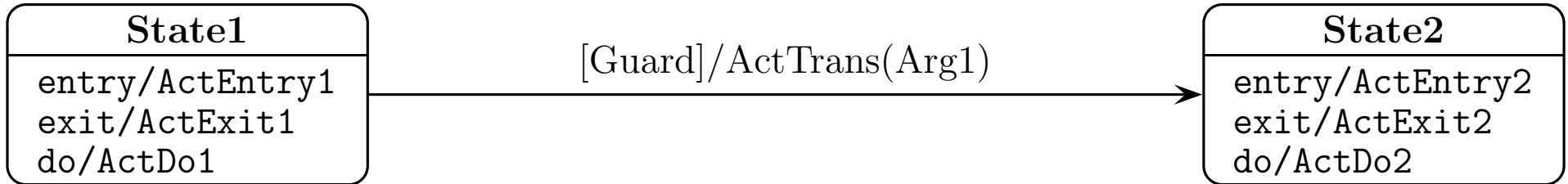
# Event Processing: Completion Event

---



# Event Processing: Completion Event

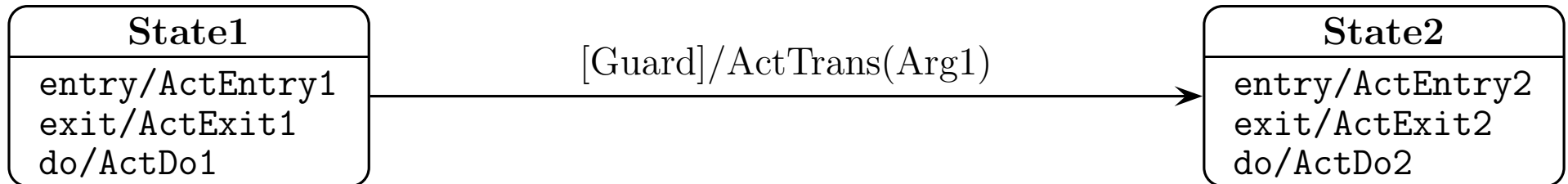
---



1. **wait until** ActDo1 **finishes** (*raises completion event*)

# Event Processing: Completion Event

---

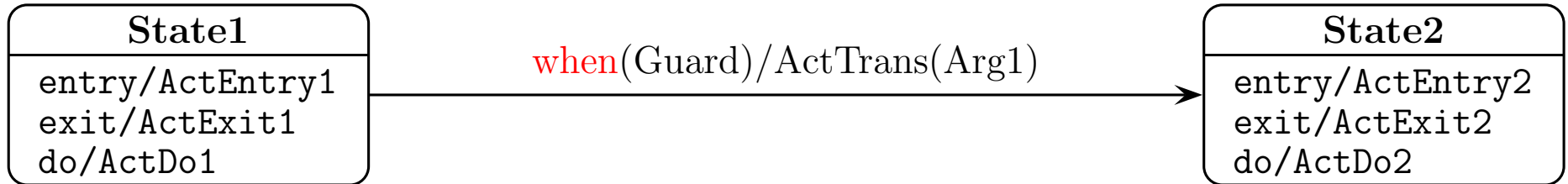


1. **wait until** ActDo1 **finishes** (*raises completion event*)
2. **check** Guard – **if** false **abort**
3. **execute** ActExit1
4. **execute** ActTrans(Arg1)
5. **execute** ActEntry2
6. **execute** ActDo2



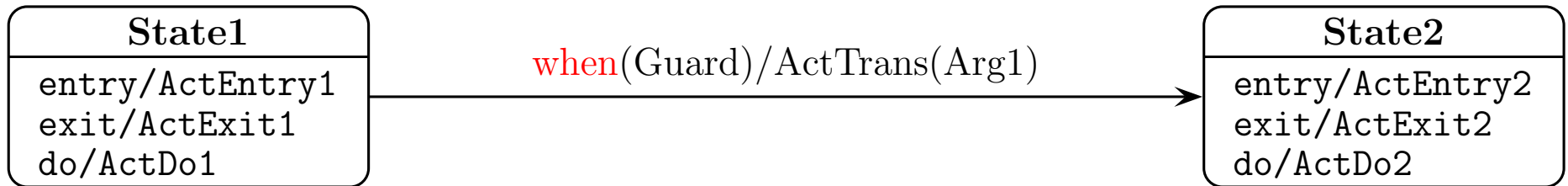
# Event Processing: Change Event

---



# Event Processing: Change Event

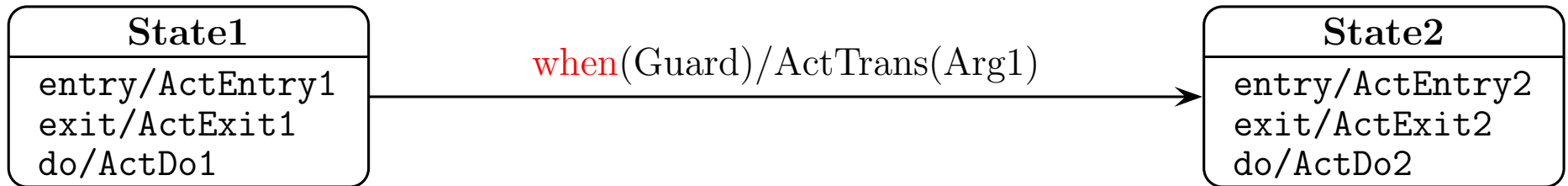
---



1. **wait until** Guard **switches from** false **to** true (**raises *change event***)

# Event Processing: Change Event

---



1. **wait until** Guard **switches from false to true** (**raises *change event***)
2. **abort** ActDo1
3. **execute** ActExit1
4. **execute** ActTrans(Arg1)
5. **execute** ActEntry2
6. **execute** ActDo2

# Completion Event vs. Change Event

---

## Activity

**Completion event:**    **after activity has** `ActDo1` **finished**

**Change event:**        **activity** `ActDo1` **is aborted**

# Completion Event vs. Change Event

---

## Activity

**Completion event:** after activity has `ActDo1` finished

**Change event:** activity `ActDo1` is aborted

## Guard

**Completion event:** guard checked only once (on completion of activity)

**Change event:** guard checked continuously

# Event Processing: Deferred Events

---

**Special action** `defer`

`Ev/defer`

**Puts event  $E_V$  in list of deferred events**

**Can only be used in a state (not to label a transition)**

# Event Processing: Deferred Events

---

## Special action `defer`

`Ev/defer`

**Puts event  $E_V$  in list of deferred events**

**Can only be used in a state (not to label a transition)**

## Triggering deferred events

**A deferred event is activated as soon as a state is entered where it is not deferred**

# Event Processing: Deferred Events

---

## Special action `defer`

`Ev/defer`

**Puts event  $E_V$  in list of deferred events**

**Can only be used in a state (not to label a transition)**

## Triggering deferred events

**A deferred event is activated as soon as a state is entered where it is not deferred**

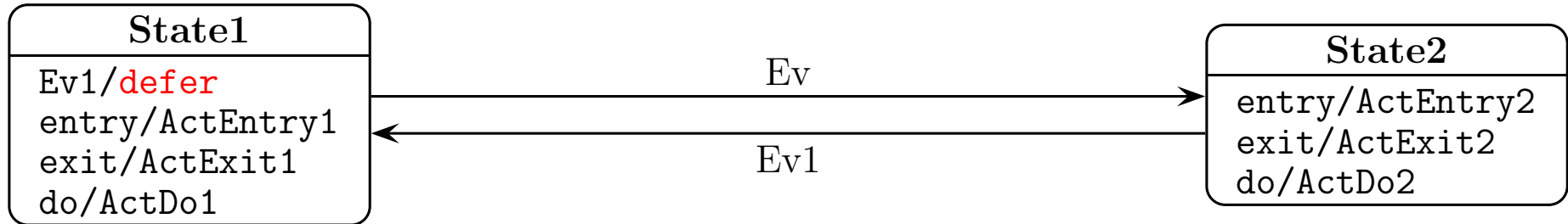
## Lost events

**Events that are neither handled nor deferred in the current state are lost**



# Event Processing: Deferred Events – Example

---



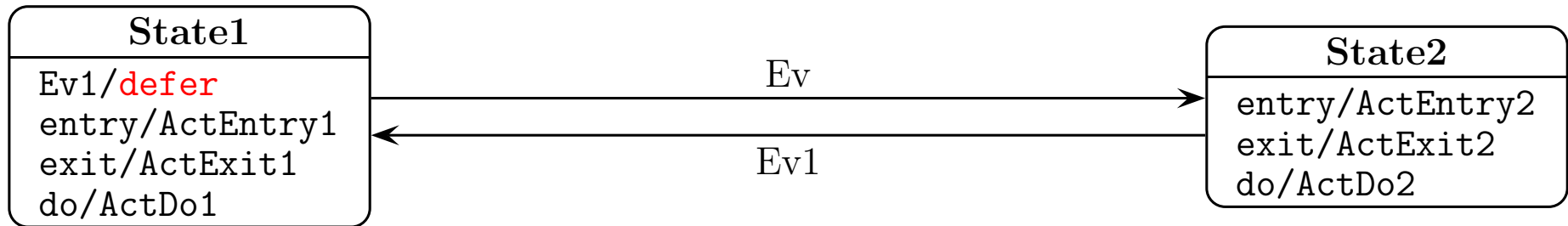
## Scenario

State1 is current state

Ev1 dispatched first, Ev dispatched afterwards

# Event Processing: Deferred Events – Example

---



## Scenario

State1 is current state

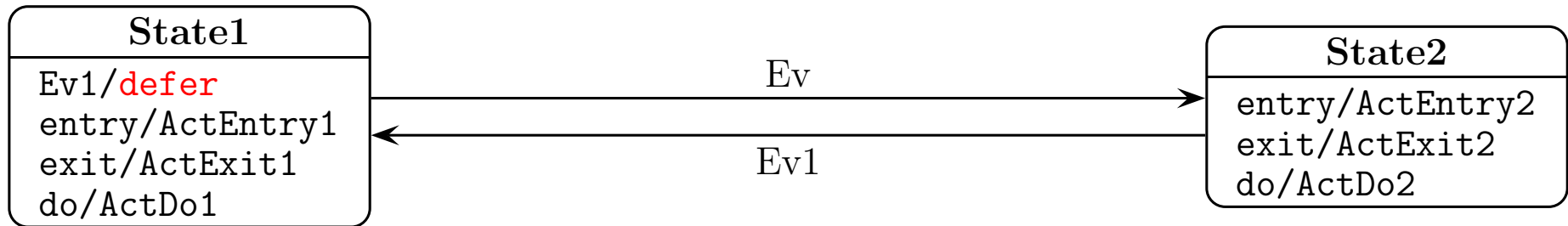
Ev1 dispatched first, Ev dispatched afterwards

Then ...

1. event Ev1 is deferred

# Event Processing: Deferred Events – Example

---



## Scenario

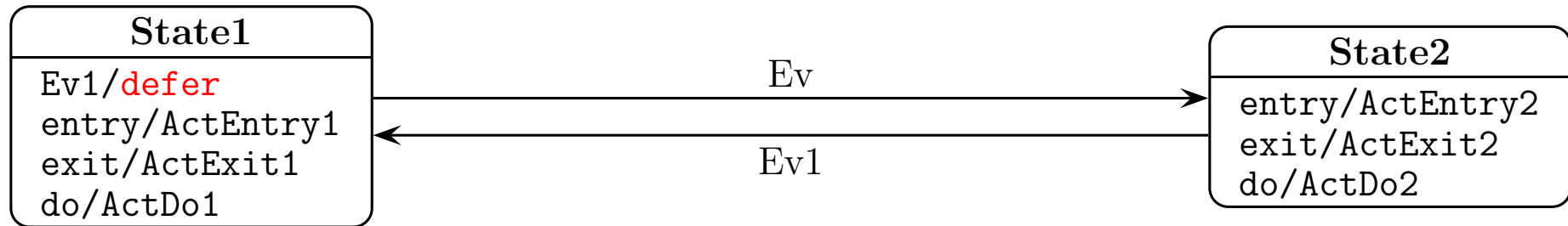
State1 is current state

Ev1 dispatched first, Ev dispatched afterwards

Then ...

1. event Ev1 is deferred
2. transition from State1 to State2, consuming event Ev

# Event Processing: Deferred Events – Example



## Scenario

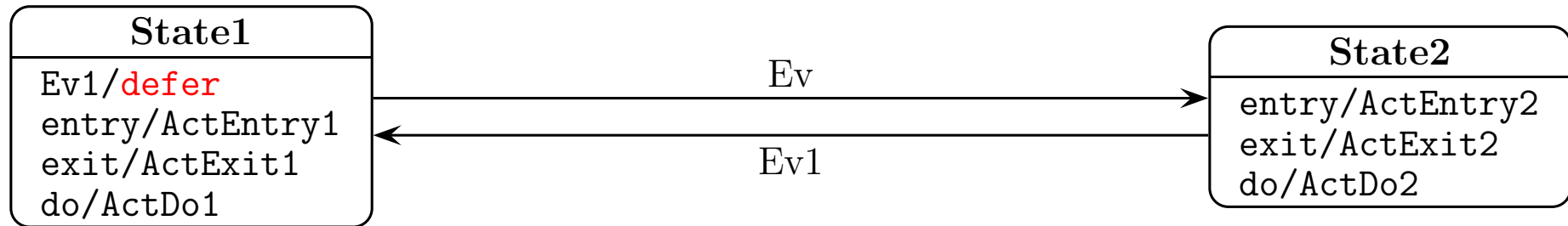
State1 is current state

Ev1 dispatched first, Ev dispatched afterwards

Then ...

1. event Ev1 is deferred
2. transition from State1 to State2, consuming event Ev
3. event Ev1 is re-activated

# Event Processing: Deferred Events – Example



## Scenario

State1 is current state

Ev1 dispatched first, Ev dispatched afterwards

Then ...

1. event Ev1 is deferred
2. transition from State1 to State2, consuming event Ev
3. event Ev1 is re-activated
4. transition from State2 to State1, consuming Ev1

# Composite States

---

## Purpose

Allow to model complex behaviour

## Idea

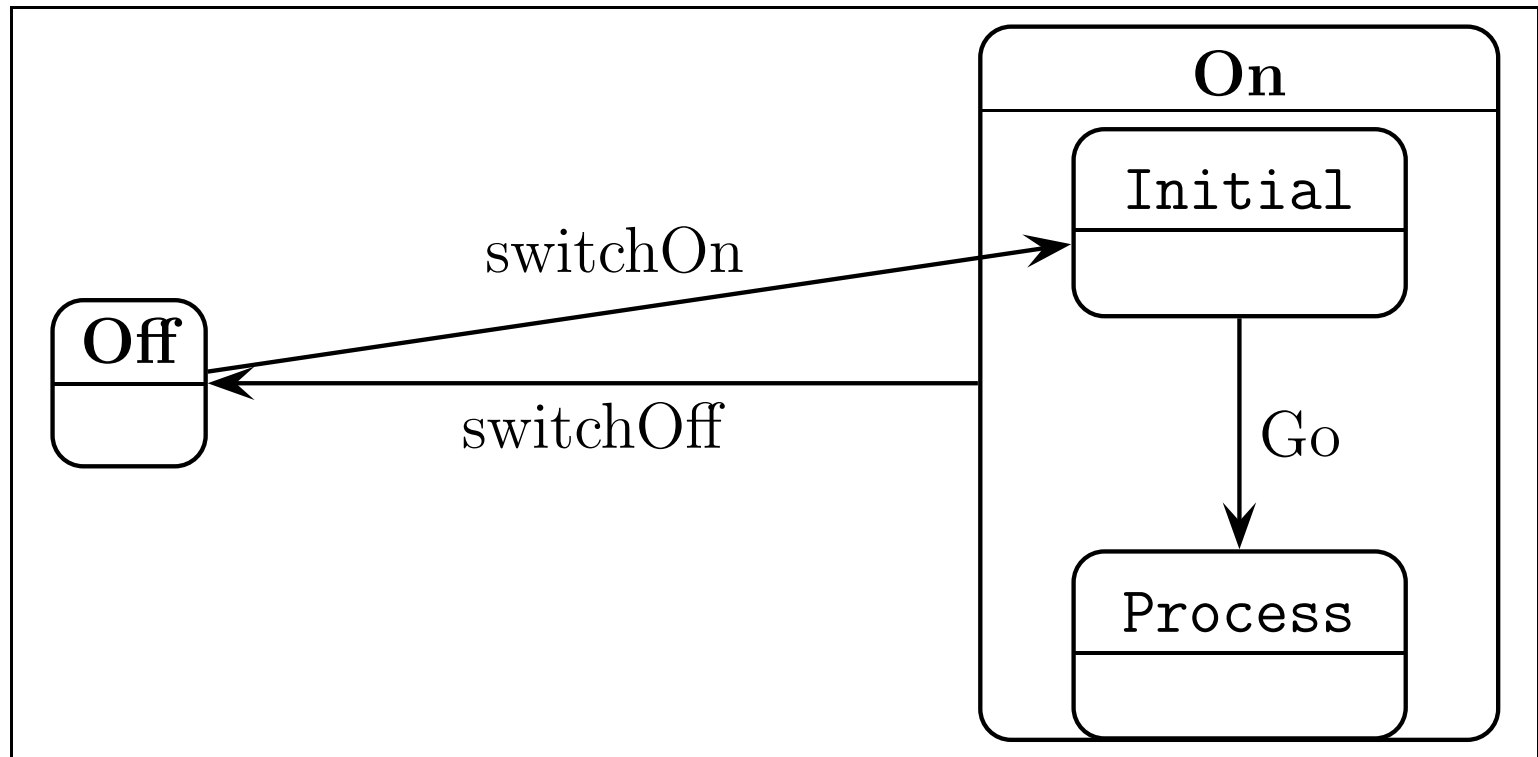
- **Similar sub-states are grouped into a composite state (nesting hierarchy is a tree)**
- **Composite states can have transitions, entry/exit actions, do activities, ... (transitions can connect states from different nesting levels)**
- **Sub-states “inherit” from the composite state**

## Note

**State Machines are in fact composite states**

# Composite States: Example

---

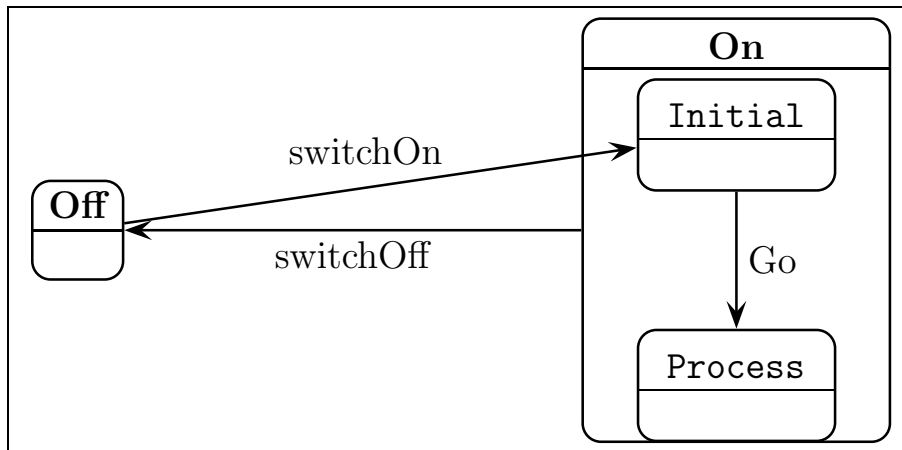


Initial, Process **are sub-states of** On

Initial, Process **“inherit” transition** switchOff

# Composite States: Three Equivalent Models

---

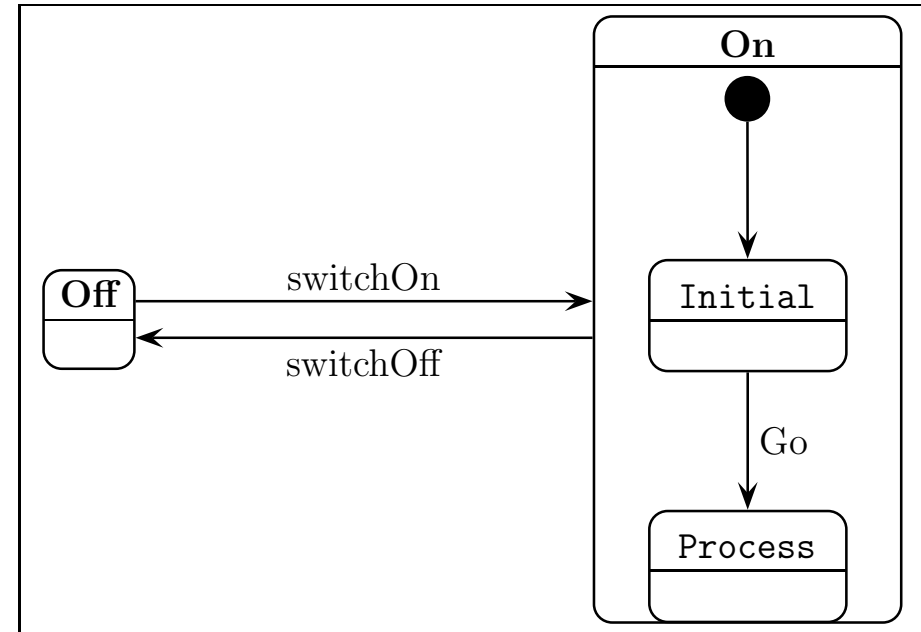
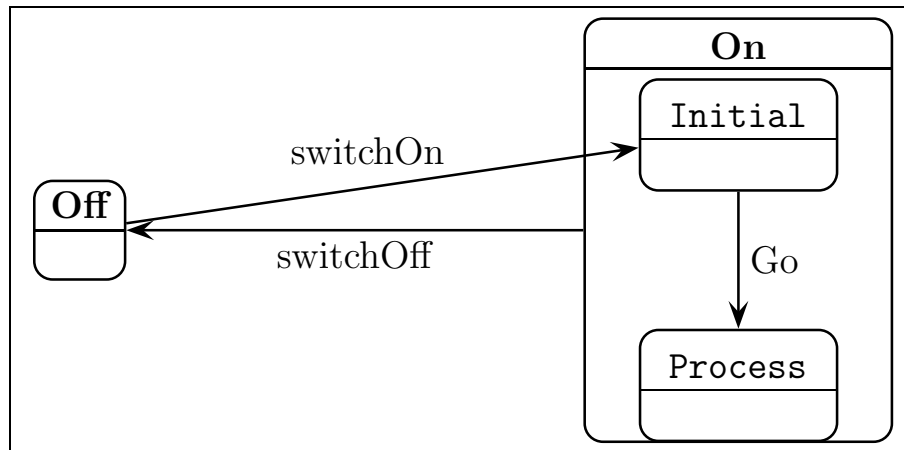


## Note

**These models are equivalent if entry/exit actions and do activities of  $On$  are ignored**



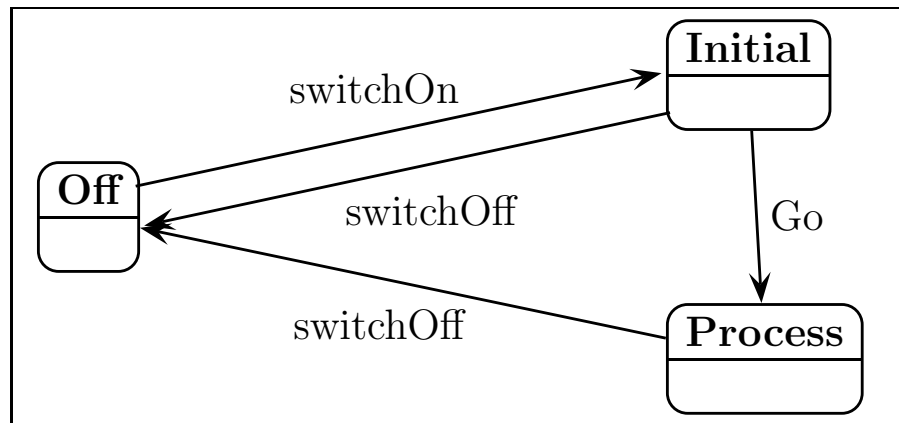
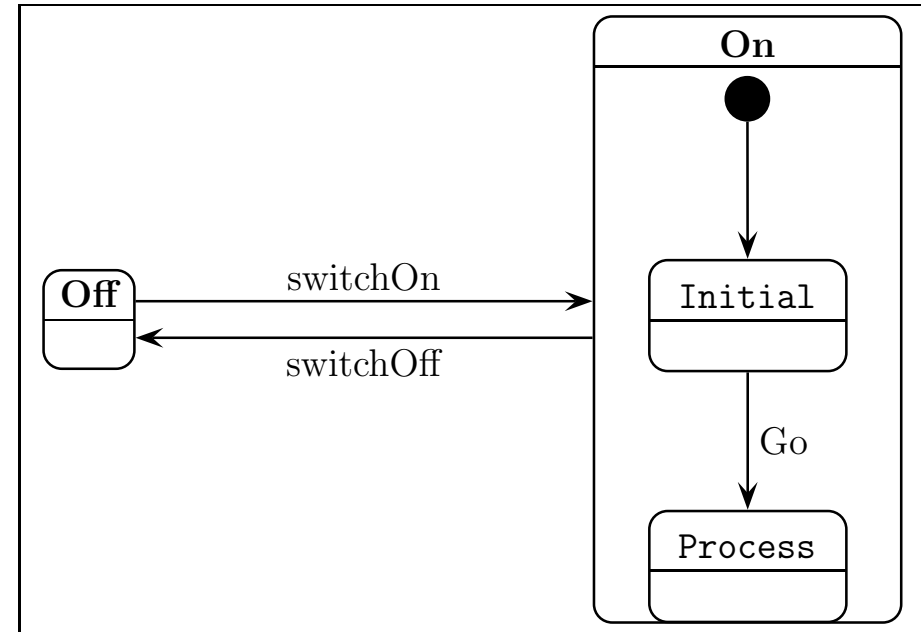
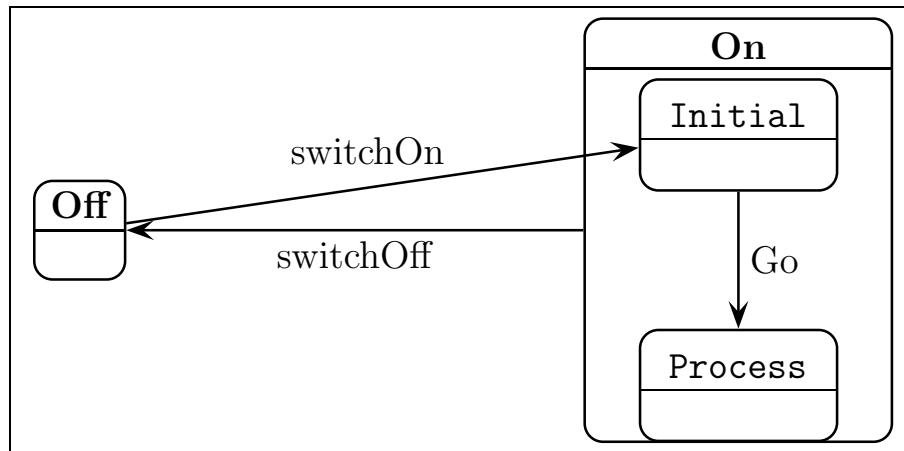
# Composite States: Three Equivalent Models



## Note

**These models are equivalent if entry/exit actions and do activities of  $On$  are ignored**

# Composite States: Three Equivalent Models

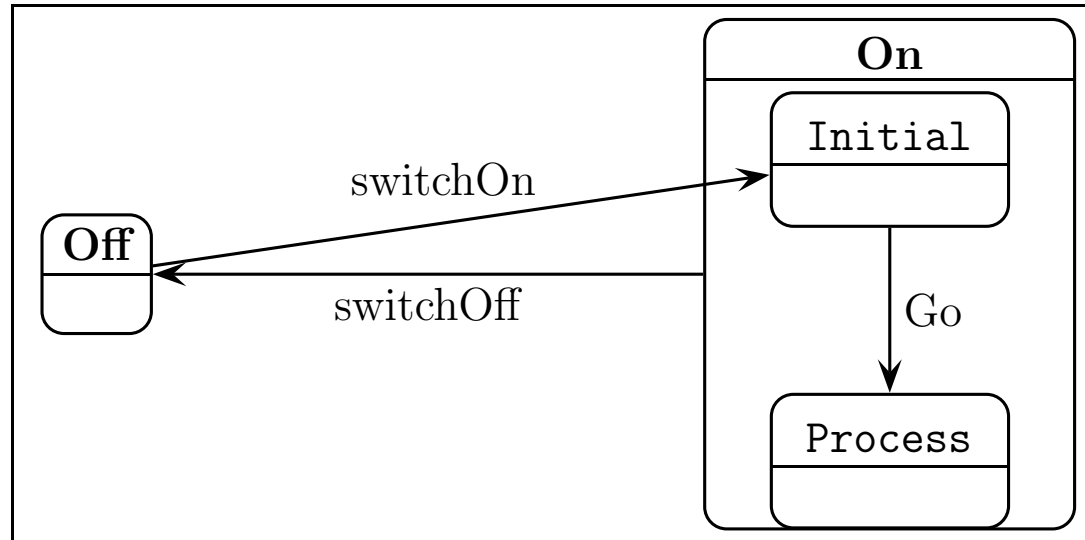


## Note

**These models are equivalent if entry/exit actions and do activities of  $On$  are ignored**

# Composite States: Active States

---



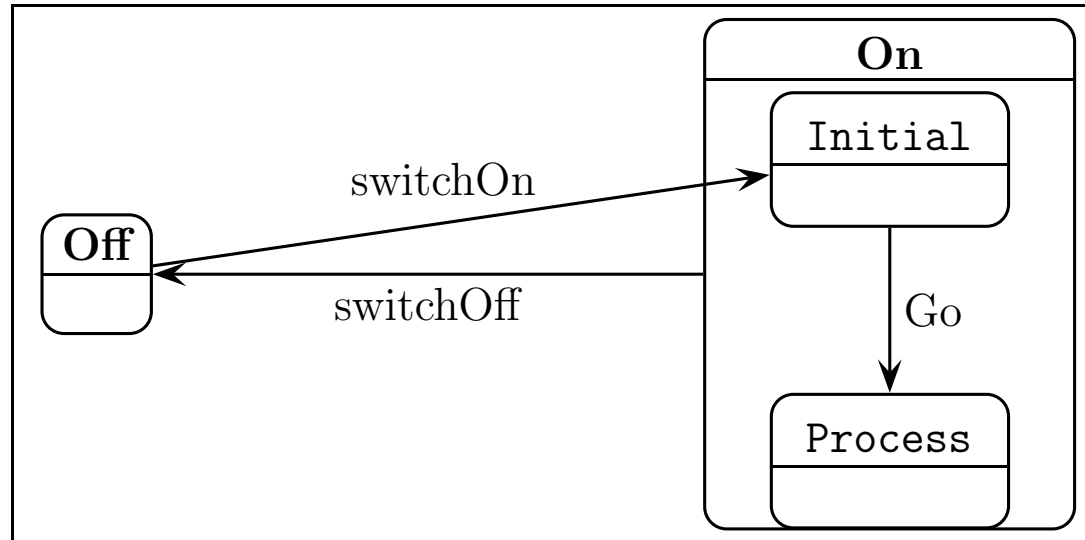
## Active states

**Sub-state and composite state can be active simultaneously**

**“Active state” now denotes a path from a top-level state to a leaf node in the state hierarchy**

# Composite States: Rules for Entering States

---



## Entering a composite state

**There must be an initial sub-state**

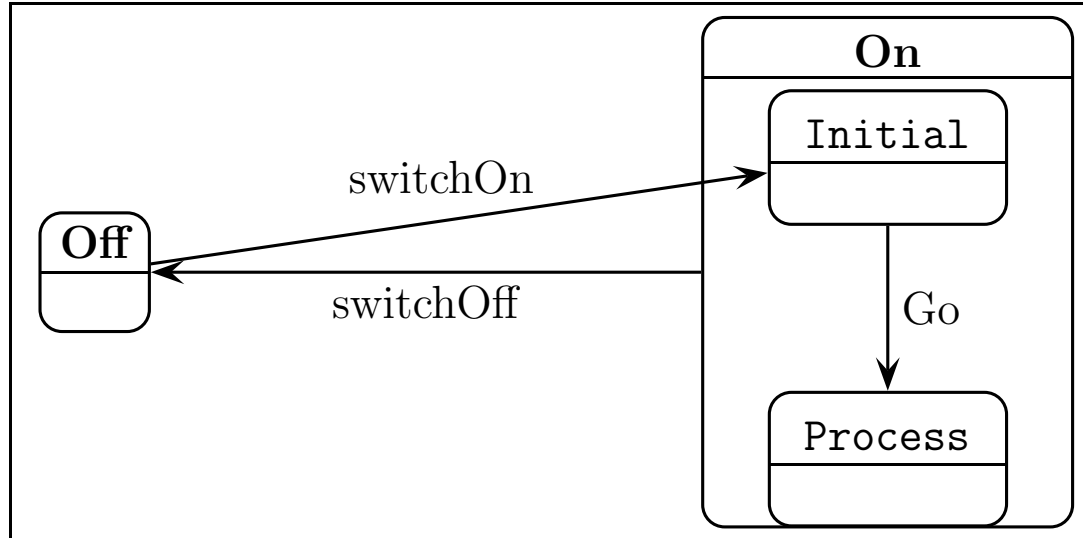
## Entering a sub-state

**Both the composite state and sub-state are activated**

**Order of entry actions: top-down**

# Composite States: Rules for Exiting States

---



## Exiting a composite state

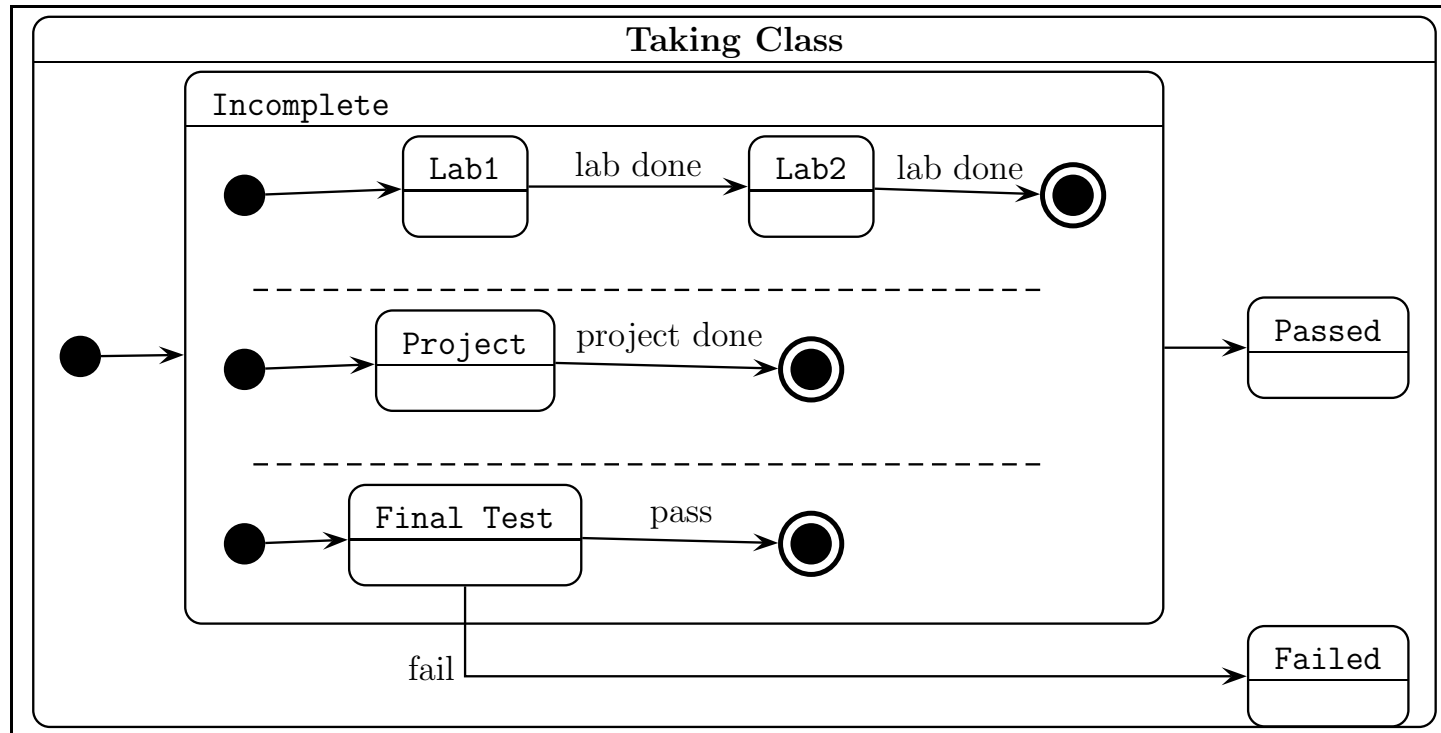
Exit active sub-state as well.

## Exiting a sub-state

Order of exit actions: bottom-up

When final state becomes active sub-state, completion event is raised

# Concurrent Composite States



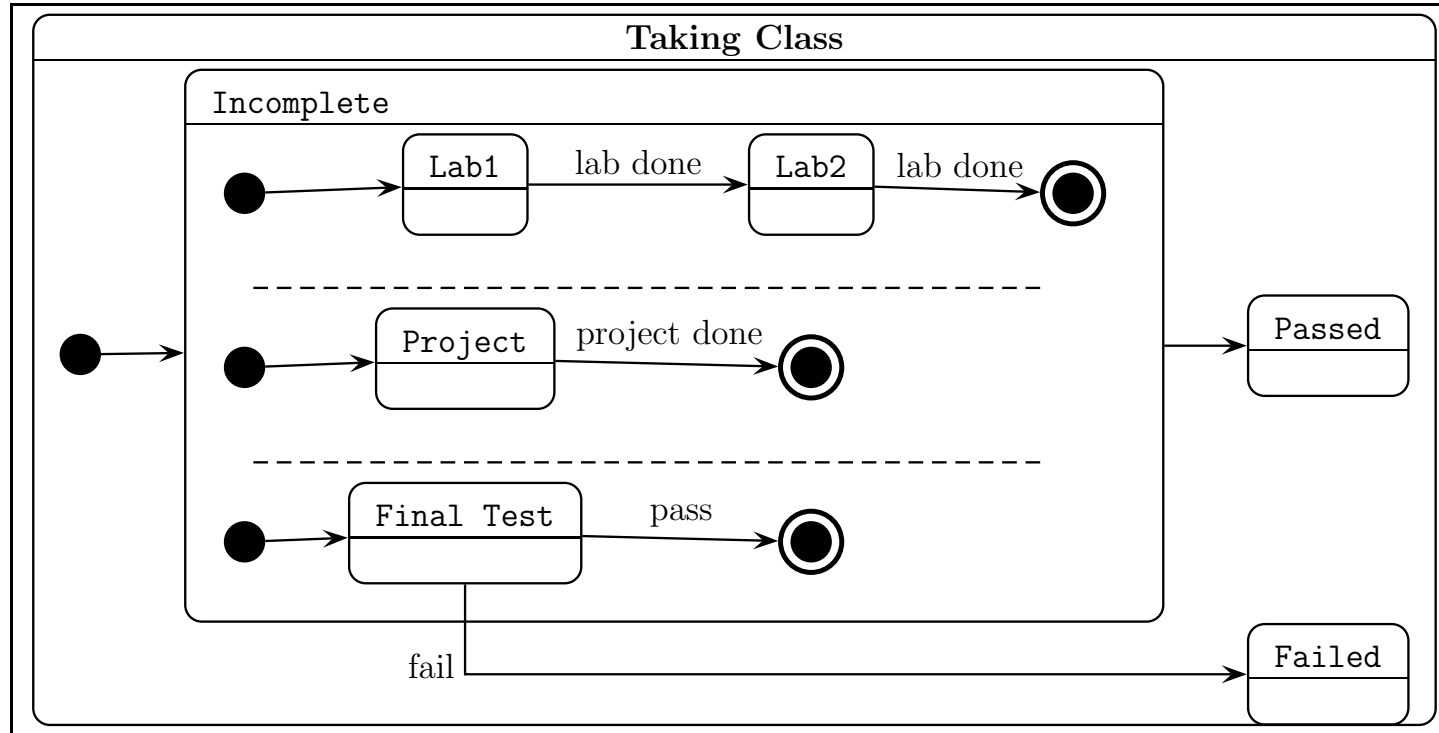
## Regions

Concurrent parts of composite state

Are activated synchronously (when composite state is activated)

Separated by dashed lines

# Concurrent Composite States

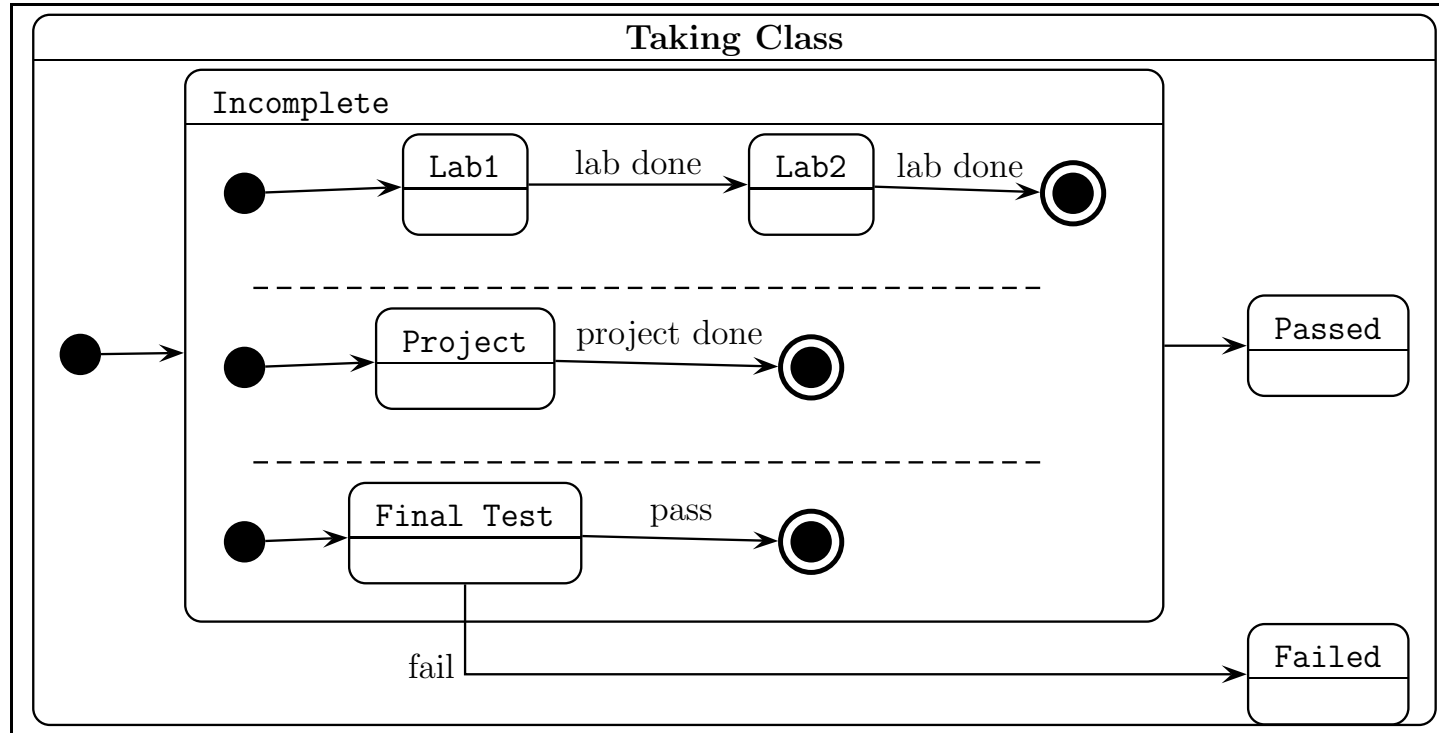


**Active state**

Also called *state configuration*

Now consists of **???**

# Concurrent Composite States



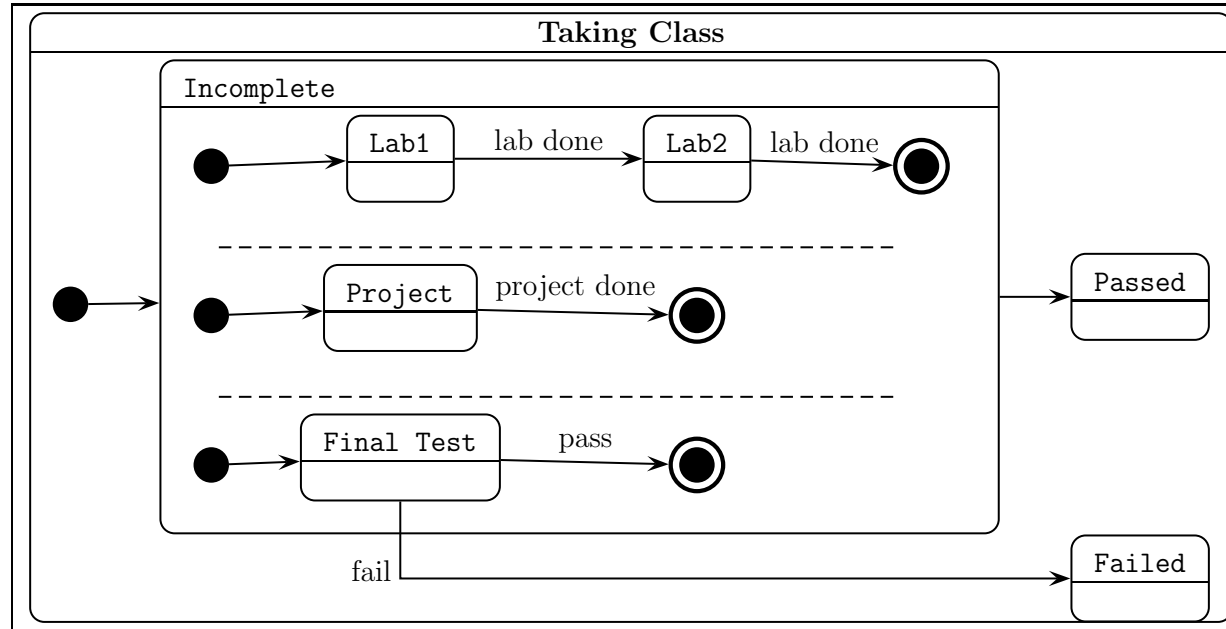
**Active state**

Also called *state configuration*

Now consists of a sub-tree of the state hierarchy



# Concurrent Composite States: Rules for Entering



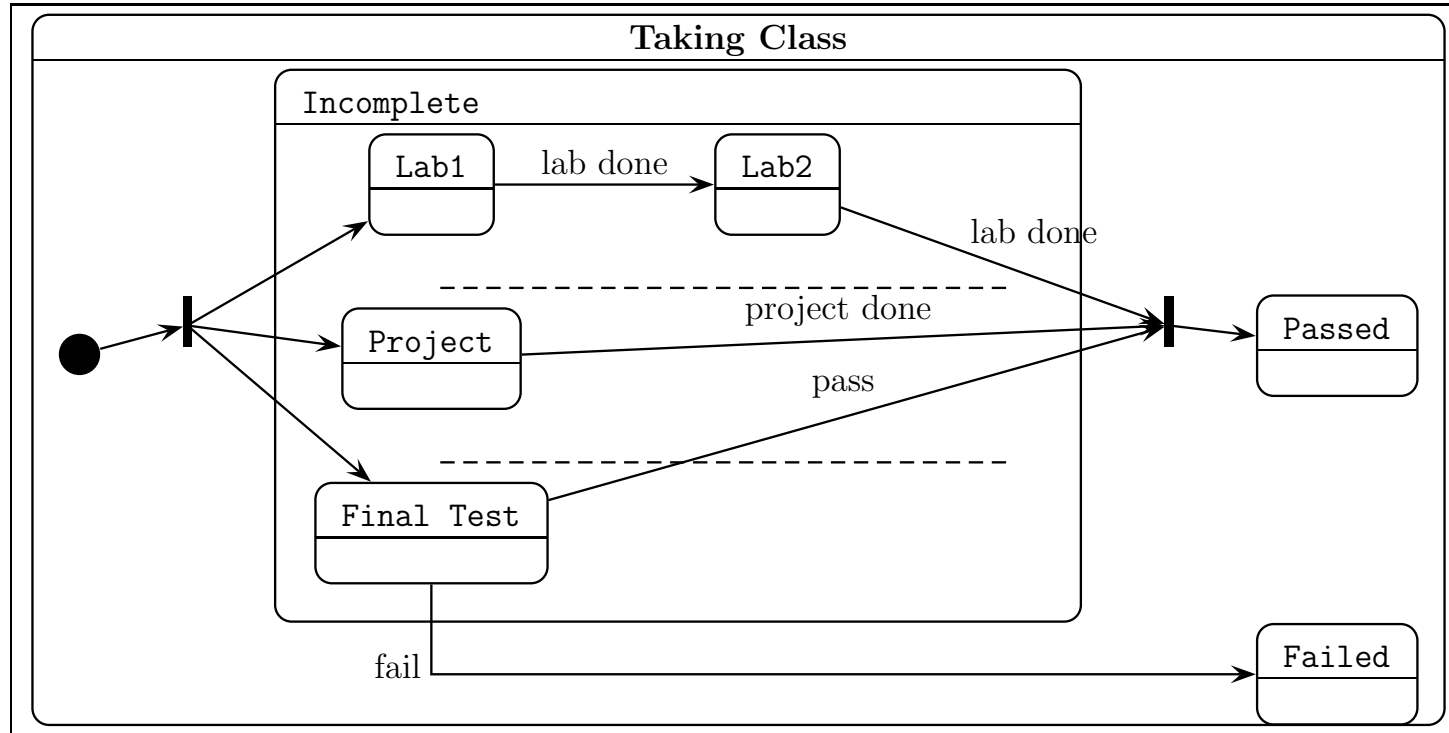
## Entering a composite state

There must be an initial sub-state in each region

## Entering a sub-state

There must be an initial sub-state in all other regions

# Concurrent Transitions

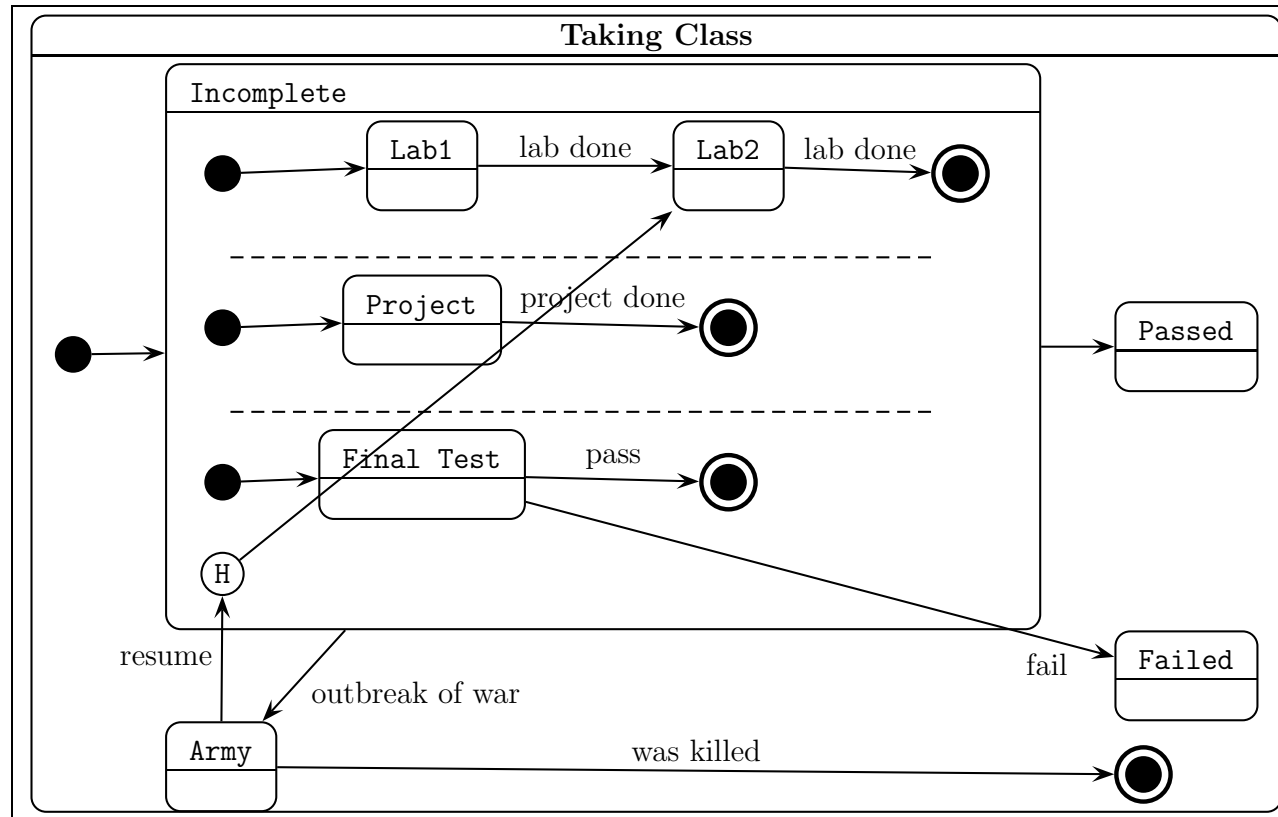


## Concurrent transition

Alternative notation for entering concurrent composite state

Uses pseudo-states “fork” and “join”

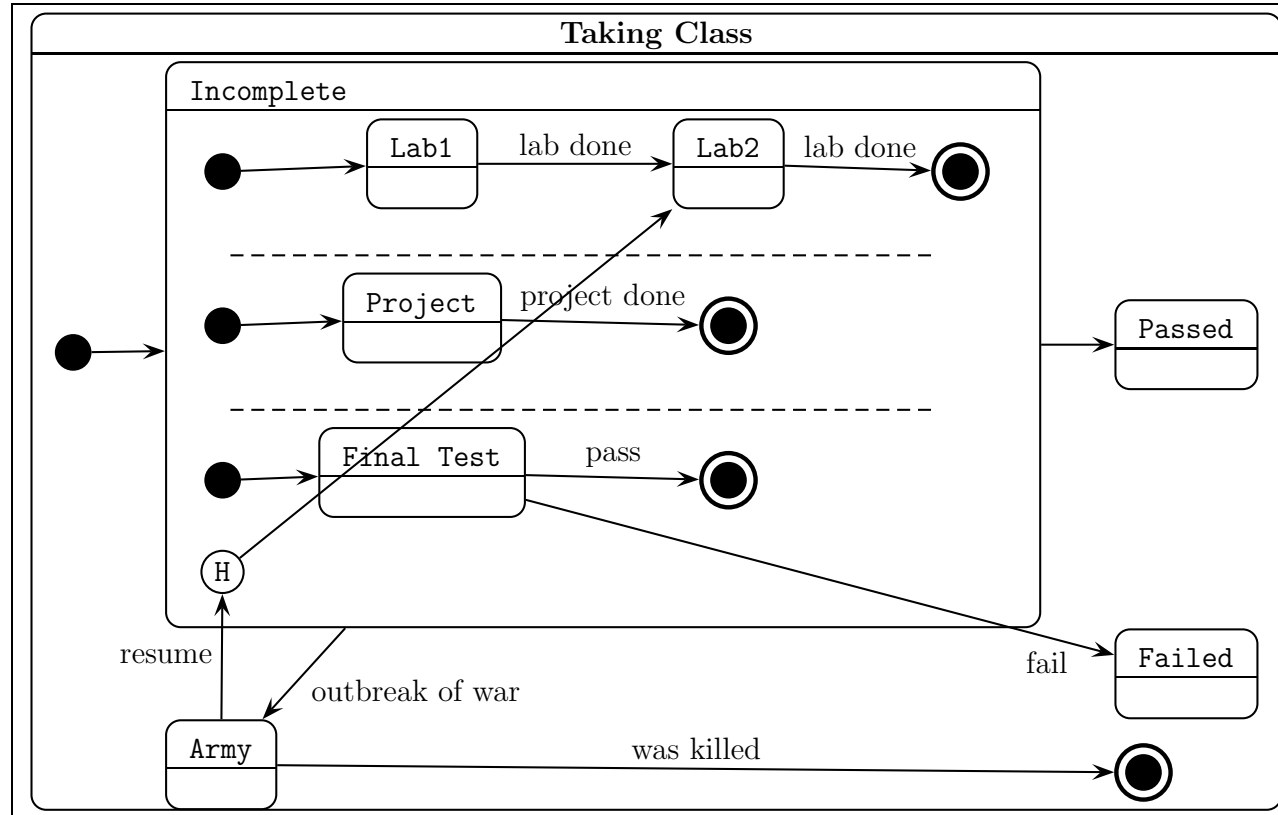
# History States



**When re-entering composite state,  
establishes the last active configuration**

**Outgoing transition indicates default active configuration**

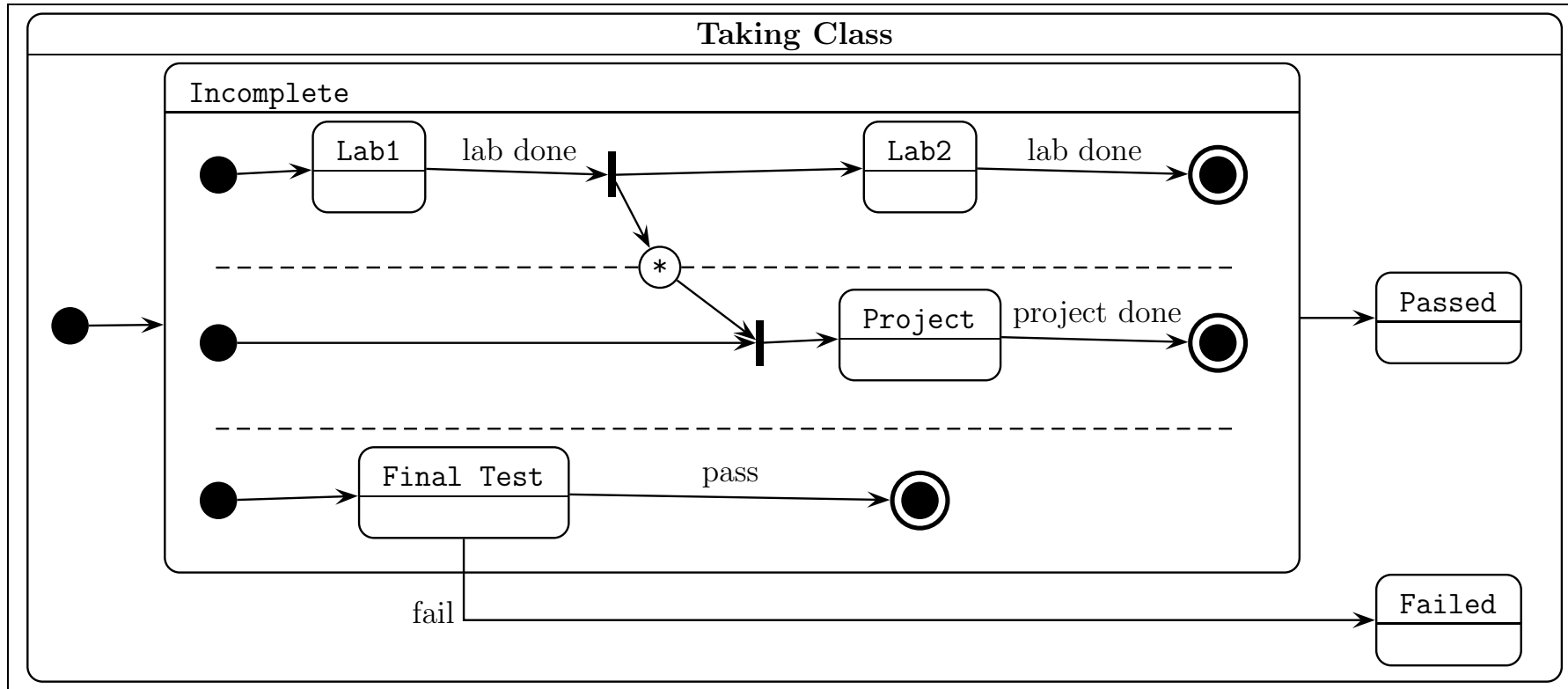
# History States: Shallow vs. Deep



**Shallow (H):** Records history only of composite state is belongs to

**Deep (H\*):** Records history of sub-states as well

# Synch States

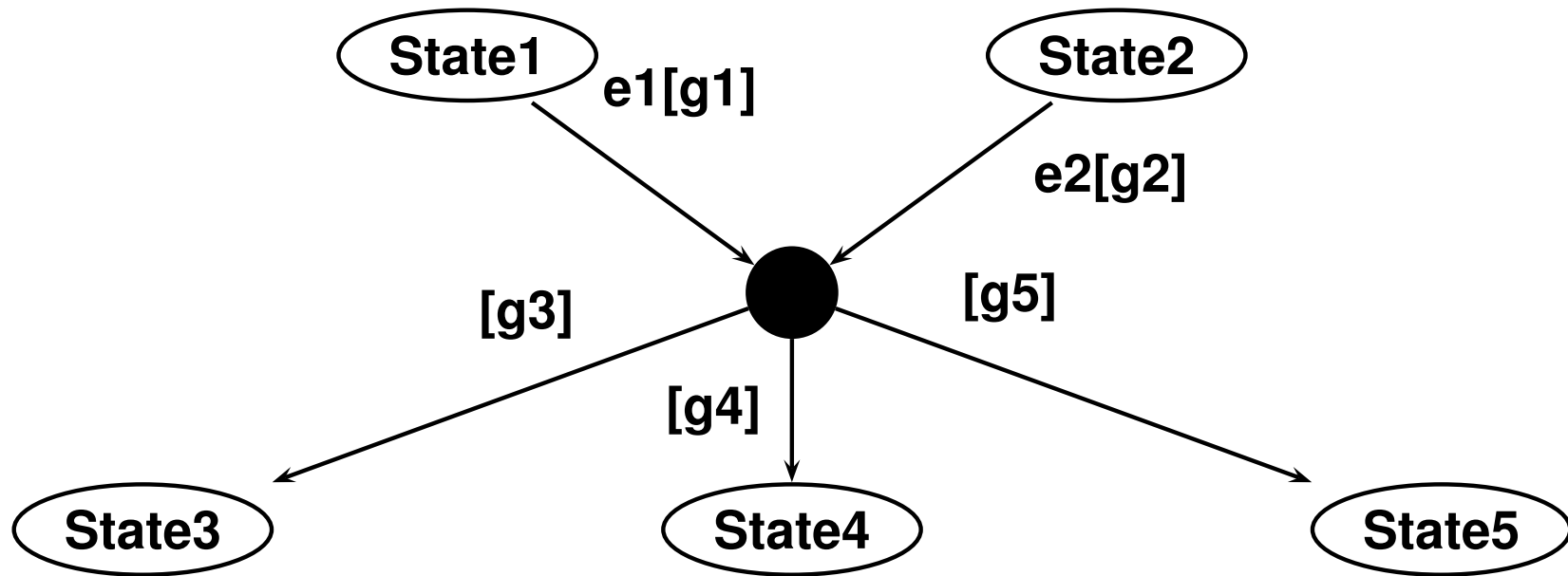


**Allow to synchronise regions**

**Used in combination with fork and join**

# Junction Points

---



## Purpose

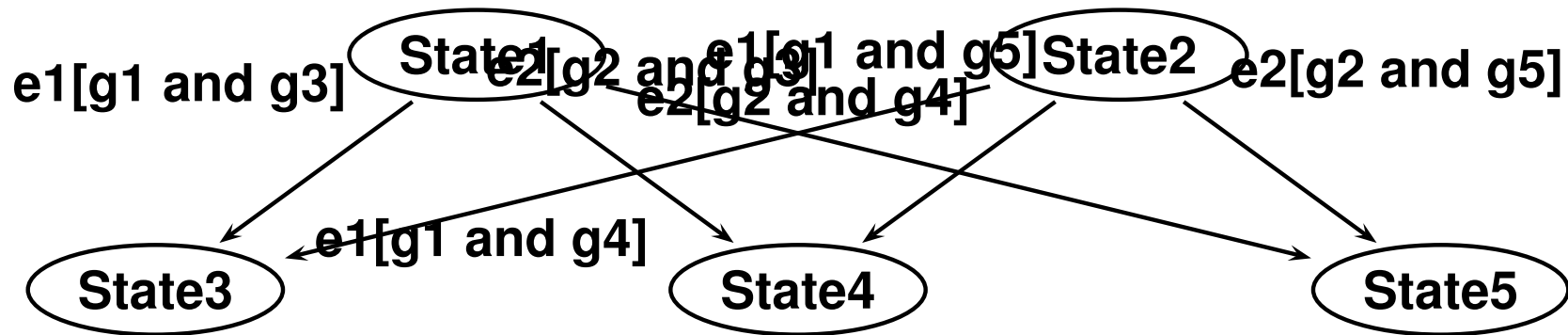
Simplify notation, allow to “factor out” transitions

Different from fork/join

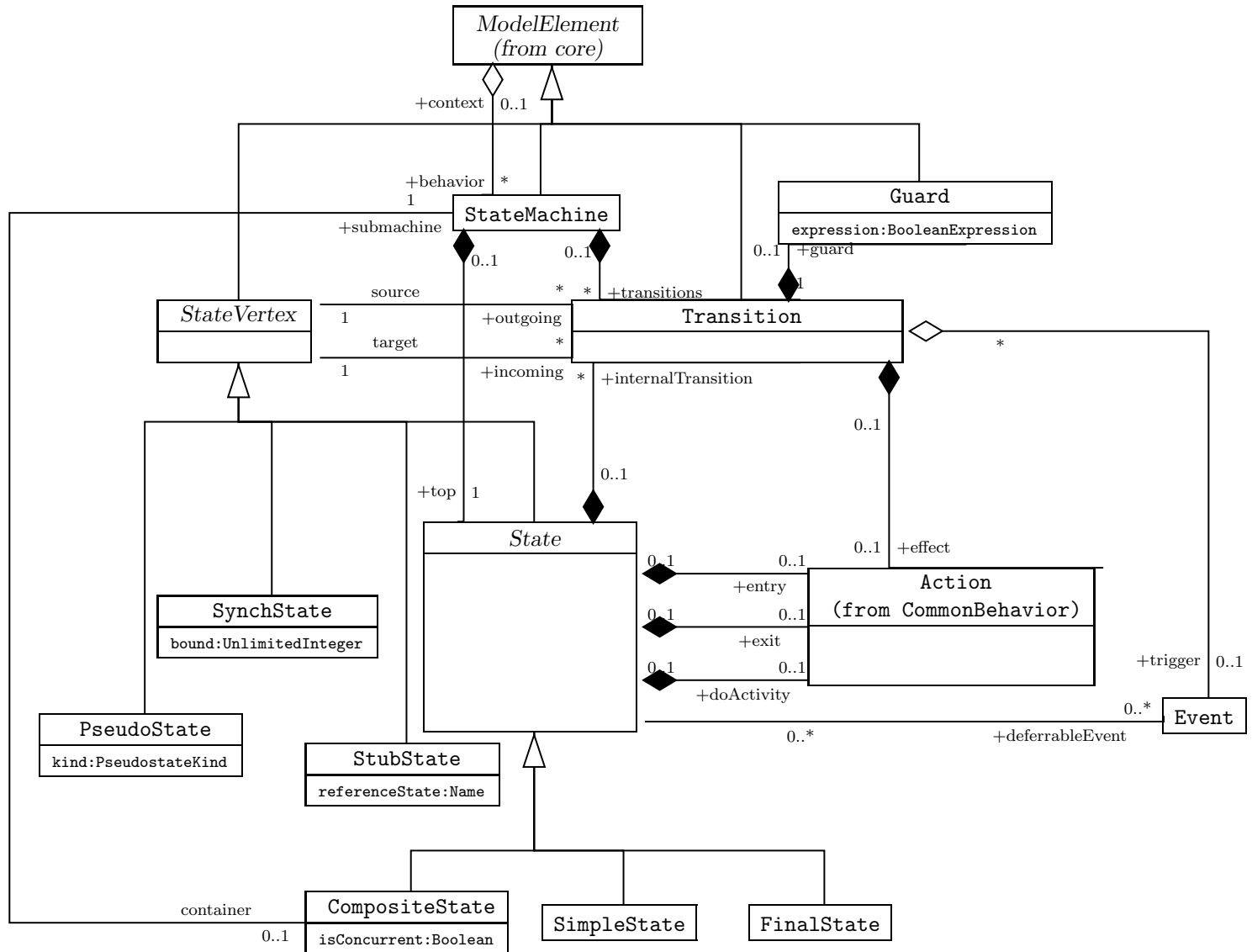
# Junction Points

---

## Example without junction point



# Metamodel for State Machine





# PseudoStateKind

---

- **initial**
- **final**
- **deepHistory**
- **shallowHistory**
- **join**
- **fork**
- **junction**

# A Constraint of the Meta Model

---

## Constraint on context of StateMachine

**A state machine is aggregated within either a classifier or a behavioural feature (e.g. an operation)**

# A Constraint of the Meta Model

---

## Constraint on context of StateMachine

A state machine is aggregated within either a classifier or a behavioural feature (e.g. an operation)

context **StateMachine**

inv **self.context.notEmpty implies**

**self.context.ocllsKindOf(BehavioralFeature) or**

**self.context.ocllsKindOf(Classifier))**

## Note

Nothing said about what happens if **self.context.isEmpty**