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**Formal Specification of Software**

**Role-based Access Control:  
An Example in OCL Formalisation**

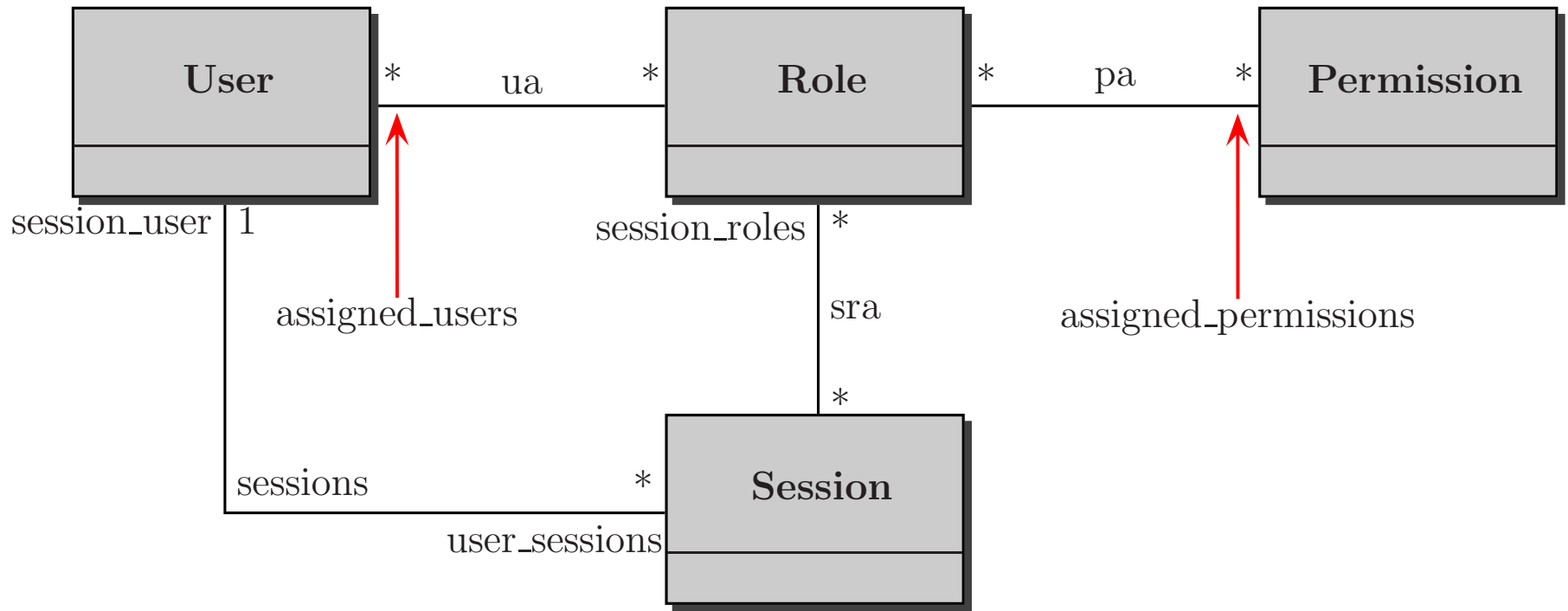
**Bernhard Beckert**



**UNIVERSITÄT KOBLENZ-LANDAU**

# Class Diagram for the RBAC Core

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# Top Level Constraint

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**context u:User**

**inv u.role  $\rightarrow$  includesAll(u.user\_sessions.session\_roles)**

# The Class User

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## User

name : Name

assignRole(r:Role)

deassignRole(r:Role)

addUser(c:Name)

deleteUser()

assignedRoles():Set(Role)      << query >>

userPermissions():Set(Permission)      << query >>

# Constraints on Operations of Class User

---

## assignRole

context **u:User::assignRole(r:Role)**

pre **role  $\rightarrow$  excludes(r)**

post **role = role@pre  $\rightarrow$  including(r)**

# Constraints on Operations of Class User

---

## assignRole

context **u:User::assignRole(r:Role)**

pre **role  $\rightarrow$  excludes(r)**

post **role = role@pre  $\rightarrow$  including(r)**

## deassignRole

context **u:User::deassignRole(r:Role)**

pre **role  $\rightarrow$  includes(r)**

post **role = role@pre  $\rightarrow$  excluding(r) and  
u.user\_sessions =  
u.user\_sessions@pre  $\rightarrow$  reject(  
s | s.session\_roles  $\rightarrow$  includes(r))**

# Constraints on Operations of Class User

---

## addUser

context **u:User::addUser(c:Name)**

pre **User.allInstances  $\rightarrow$  forAll( $u_1$  |  $u_1.name \neq c$ )**

post **User.allInstances  $\rightarrow$  exists(  $u_1$  |  
    **User.allInstances@pre  $\rightarrow$  excludes(  $u_1$ ) and**  
     **$u_1.name = c$  and**  
    **User.allInstances = User.allInstances@pre  $\rightarrow$  including( $u_1$ )**)**

# Constraints on Operations of Class User

---

## addUser

context **u:User::addUser(c:Name)**

pre **User.allInstances  $\rightarrow$  forAll( $u_1$  |  $u_1.name <> c$ )**

post **User.allInstances  $\rightarrow$  exists(  $u_1$  |  
User.allInstances@pre  $\rightarrow$  excludes(  $u_1$ ) and  
 $u_1.name = c$  and  
User.allInstances = User.allInstances@pre  $\rightarrow$  including( $u_1$ ))**

## deleteUser

context **u:User::deleteUser()**

pre **true**

post **User.allInstances = User.allInstances@pre  $\rightarrow$  excluding(u) and  
Session.allInstances = Session.allInstances@pre  $\rightarrow$   
reject(s | u.user\_sessions  $\rightarrow$  includes(s))**



# The Operation `oclIsNew`

---

**context** `u:User::addUser(c:Name)`

**pre** `User.allInstances -> forAll(u1 | u1.name <> c)`

**post** `User.allInstances -> exists( u1 |  
    User.allInstances@pre -> excludes( u1) and  
    u1.name = c and  
    User.allInstances = User.allInstances@pre -> including(u1))`

# The Operation oclIsNew

---

context **u:User::addUser(c:Name)**

pre **User.allInstances  $\rightarrow$  forAll( $u_1$  |  $u_1.name \neq c$ )**

post **User.allInstances  $\rightarrow$  exists(  $u_1$  |  
**User.allInstances@pre  $\rightarrow$  excludes(  $u_1$ ) and**  
 **$u_1.name = c$  and**  
**User.allInstances = User.allInstances@pre  $\rightarrow$  including( $u_1$ )**)**

**is equivalent to**

context **u:User::addUser(c:Name)**

pre **User.allInstances  $\rightarrow$  forAll( $u_1$  |  $u_1.name \neq c$ )**

post **User.allInstances  $\rightarrow$  exists(  $u_1$  |  
 **$u_1.oclIsNew$  and**  
 **$u_1.name = c$  and**  
**User.allInstances = User.allInstances@pre  $\rightarrow$  including( $u_1$ )**)**

# Constraints on Operations of Class User

---

## assignedRoles

context **u:User::assignedRoles()**

pre **true**

post **result = u.role**

# Constraints on Operations of Class User

---

## assignedRoles

context **u:User::assignedRoles()**

pre **true**

post **result = u.role**

## userPermissions

context **u:User::userPermissions()**

pre **true**

post **result = u.role.assigned\_permissions -> asSet()**

# The Class Role

---

## Role

name : Name

grantPermission(p:Permission)

revokePermission(p:Permission)

addRole(r:Name)

deleteRole()

rolePermissions():Set(Permission) << query >>

assignedUsers():Set(User) << query >>

# Constraints on Operations of Class Role

---

## grantPermission

context **r:Role::grantPermission(p:Permission)**

pre **true**

post **r.assigned\_permissions =  
r.assigned\_permissions@pre -> including(p)**

# Constraints on Operations of Class Role

---

## grantPermission

```
context  r:Role::grantPermission(p:Permission)
pre      true
post     r.assigned_permissions =
         r.assigned_permissions@pre -> including(p)
```

## revokePermission

```
context  r:Role::revokePermission(p:Permission)
pre      r.assigned_permissions -> includes(p)
post     r.assigned_permissions =
         r.assigned_permissions@pre -> excluding(p)
```

# Constraints on Operations of Class Role

---

## addRole

context **r:Role::addRole(c:Name)**

pre **Role.allInstances  $\rightarrow$  forAll(r | r.name  $\langle \rangle$  c)**

post **Role.allInstances  $\rightarrow$  exists( r<sub>1</sub> |  
r<sub>1</sub>.oclIsNew and  
r<sub>1</sub>.name = c and  
Role.allInstances = Role.allInstances@pre  $\rightarrow$  including(r<sub>1</sub>))**



# Constraints on Operations of Class Role

---

## addRole

context **r:Role::addRole(c:Name)**

pre **Role.allInstances  $\rightarrow$  forAll(r | r.name  $\langle \rangle$  c)**

post **Role.allInstances  $\rightarrow$  exists( r<sub>1</sub> |  
r<sub>1</sub>.ocllsNew and  
r<sub>1</sub>.name = c and  
Role.allInstances = Role.allInstances@pre  $\rightarrow$  including(r<sub>1</sub>))**

## deleteRole

context **r:Role::deleteRole()**

pre **true**

post **Role.allInstances = Role.allInstances@pre  $\rightarrow$  excluding(r) and  
Session.allInstances = Session.allInstances@pre  $\rightarrow$   
reject(s | s.session\_roles  $\rightarrow$  includes(r))**

# Constraints on Operations of Class Role

---

## **rolePermissions**

```
context  r:Role::rolePermissions()  
  pre    true  
  post   result = r.assigned_permissions
```

# Constraints on Operations of Class Role

---

## rolePermissions

```
context  r:Role::rolePermissions()  
  pre    true  
  post   result = r.assigned_permissions
```

## assignedUsers

```
context  r:Role::assignedUsers()  
  pre    true  
  post   result = r.assigned_users
```

# The Class Session

---

## Session

session\_ID:String

addActiveRole(r:Role)

dropActiveRole(r:Role)

createSession(u:User,ars:Set(Role),id:String)

deleteSession()

sessionRoles():Set(Role)

« query »

sessionPermissions():Set(Permissions)

« query »

# Constraints on Operations of Class Session

---

## **addActiveRole**

**context** **s:Session::addActiveRole(r:Role)**

**pre** **r.assigned\_users  $\rightarrow$  includes(s.session\_user) and**  
**s.session\_roles  $\rightarrow$  excludes(r)**

**post** **s.session\_roles =**  
**s.session\_roles@pre  $\rightarrow$  including(r)**

# Constraints on Operations of Class Session

---

## addActiveRole

context **s:Session::addActiveRole(r:Role)**

pre **r.assigned\_users  $\rightarrow$  includes(s.session\_user) and  
s.session\_roles  $\rightarrow$  excludes(r)**

post **s.session\_roles =  
s.session\_roles @pre  $\rightarrow$  including(r)**

## dropActiveRole

context **s:Session::dropActiveRole(r:Role)**

pre **s.session\_roles  $\rightarrow$  includes(r)**

post **s.session\_roles =  
s.session\_roles @pre  $\rightarrow$  excluding(r)**

# Constraints on Operations of Class Session

---

## createSession

context **s:Session::**

**createSession(u:User,ars:Set(Role),id:String)**

**pre Session.allInstances -> forAll(s | s.session\_ID <> id) and  
u.role -> includesAll(ars)**

**post u.user\_sessions -> exists( s<sub>1</sub> |  
s<sub>1</sub>.ocllsNew and  
s<sub>1</sub>.session\_ID = id and  
s<sub>1</sub>.session\_roles = ars  
u.user\_sessions =  
u.user\_sessions@pre -> including(s<sub>1</sub>) and  
)**

# Constraints on Operations of Class Session

---

## **deleteSession**

**context** **s:Session::deleteSession()**

**pre** **true**

**post** **Session.allInstances =  
          Session.allInstances @pre -> excluding(s)**



# Constraints on Operations of Class Session

---

## **sessionRoles**

**context** **s:Session::sessionRoles()**

**pre** **true**

**post** **result = s.session\_roles**

# Constraints on Operations of Class Session

---

## sessionRoles

context **s:Session::sessionRoles()**

pre **true**

post **result = s.session\_roles**

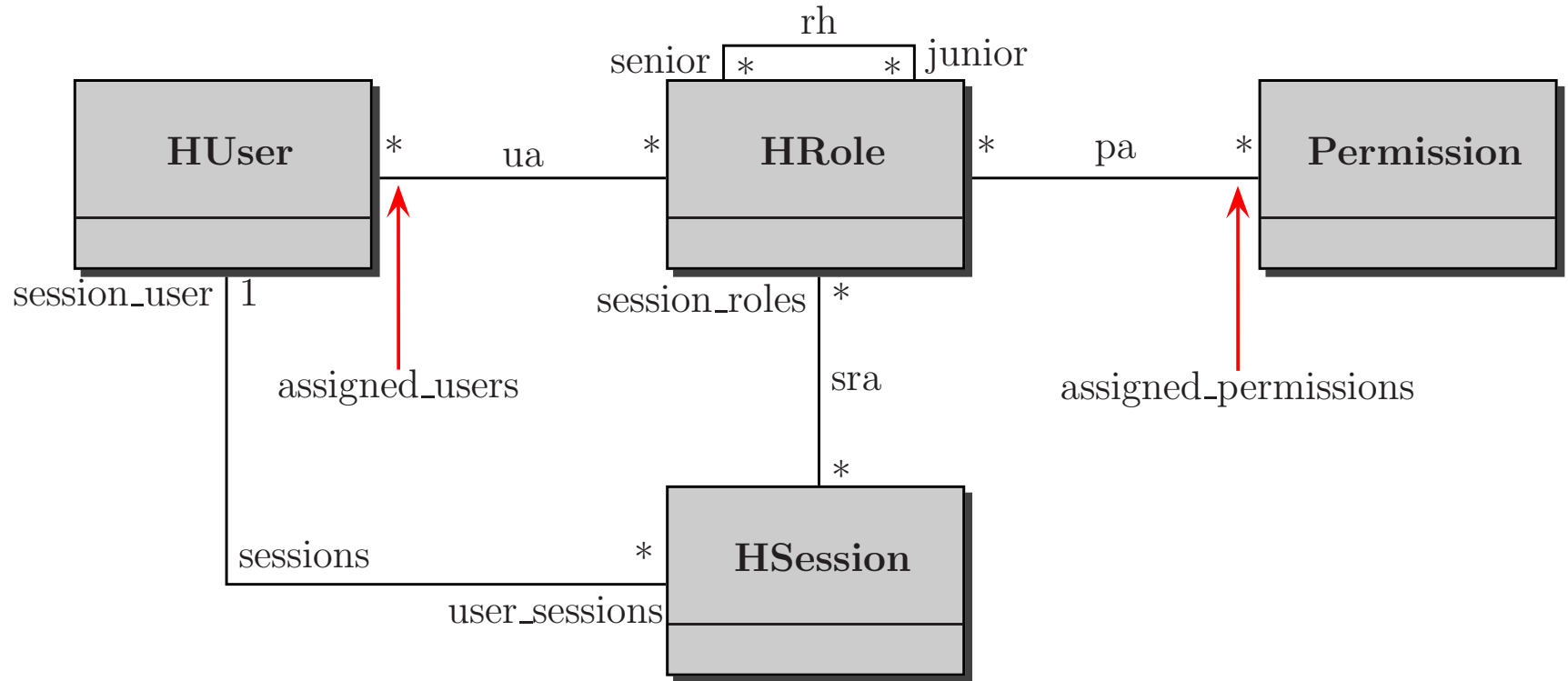
## sessionPermissions

context **s:Session::sessionPermissions()**

pre **true**

post **result = s.session\_roles.assigned\_permissions -> asSet()**

# Class Diagram for RBAC with Hierarchy



# Auxilliary Definitions

---

**senior<sup>+</sup>**

**r.senior<sup>+</sup>** abbreviation for

**HRole.allInstances ->**

**iterate(r<sub>1</sub> ; y:Set(HRole) = r.senior | y -> union(y.senior))**

# Auxilliary Definitions

---

**senior<sup>+</sup>**

**r.senior<sup>+</sup>** abbreviation for

**HRole.allInstances ->**

**iterate(r<sub>1</sub> ; y:Set(HRole) = r.senior | y -> union(y.senior))**

**senior<sup>\*</sup>**

**r.senior<sup>\*</sup>** abbreviation for

**HRole.allInstances ->**

**iterate(r<sub>1</sub> ; y:Set(HRole) = { r } | y -> union(y.senior))**

# Auxilliary Definitions

---

**senior<sup>+</sup>**

**r.senior<sup>+</sup>** abbreviation for

**HRole.allInstances ->**

**iterate(r<sub>1</sub> ; y:Set(HRole) = r.senior | y -> union(y.senior))**

**senior<sup>\*</sup>**

**r.senior<sup>\*</sup>** abbreviation for

**HRole.allInstances ->**

**iterate(r<sub>1</sub> ; y:Set(HRole) = { r } | y -> union(y.senior))**

**junior<sup>+</sup>**

**junior<sup>\*</sup>**

# General Role Hierachies

---

**No skipping of hierarchy levels, no cycles**

**context r:HRole**

**inv GeneralRH :**

**not HRole.allInstances  $\rightarrow$  exists( $r_1, r_2$  |  
    **r.senior  $\rightarrow$  includes( $r_1$ ) and**  
    **r.senior  $\rightarrow$  includes( $r_2$ ) and**  
     **$r_1$ .senior<sup>+</sup>  $\rightarrow$  includes( $r_2$ ))**  
**) and**  
**r.senior<sup>+</sup>  $\rightarrow$  excludes(r)****

**GeneralRH is the name of the invariant**

# Limited Role Hierachies

---

## Hierarchy a tree structure

context  $r, r_1, r_2: \text{HRole}$

inv **LimitedRH :**

**GeneralRH and**

**( $r.\text{senior} \rightarrow \text{includes}(r_1)$  and  $r.\text{senior} \rightarrow \text{includes}(r_2)$ )**

**implies  $r_1 = r_2$**



# Class HRole

---

## HRole

name: Name

grantPermission(p: Permission)

revokePermission(p: Permission)

addRole(c: Name)

deleteRole()

rolePermissions(): Set(Permission) << query >>

assignedUsers(): Set(HUser) << query >>

authorizedUsers(): Set(HUser) << query >>

addInheritance(r: HRole)

deleteInheritance(r: HRole)

addAscendant(c: Name)

addDescendant(c: Name)

# Class HRole (Short version)

---

## HRole enriches Role

`addInheritance(r:HRole)`

`deleteInheritance(r:HRole)`

`addAscendant(c:Name)`

`addDescendant(c:Name)`

`authorizedUsers()`

*<< query >>*

`rolePermissions():Set(Permission)`

*<< query >>*

# Constraints on Operations of Class HRole

---

## addInheritance

context **r:HRole::addInheritance(r<sub>1</sub>:HRole)**

pre **not(r.senior\* -> includes(r<sub>1</sub>)) and  
not(r<sub>1</sub>.senior\* -> includes(r))**

post **r.senior -> includes(r<sub>1</sub>) and  
HRole.allInstances -> forAll(r<sub>2</sub>,r<sub>3</sub> |  
((r<sub>2</sub> <> r or r<sub>3</sub> <> r<sub>1</sub>) implies  
(r<sub>2</sub>.senior -> includes(r<sub>3</sub>) iff  
r<sub>2</sub>.senior@pre -> includes(r<sub>3</sub>)))**

**A iff B** is an abbreviation for **(A implies B) and (B implies A)**

# Constraints on Operations of Class HRole

---

## deleteInheritance

context **r:HRole::deleteInheritance(r<sub>1</sub>:HRole)**

pre **r.senior  $\rightarrow$  includes(r<sub>1</sub>)**

post **r.senior  $\rightarrow$  excludes(r<sub>1</sub>) and  
HRole.allInstances  $\rightarrow$  forAll(r<sub>2</sub>,r<sub>3</sub> |  
((r<sub>2</sub> <> r or r<sub>3</sub> <> r<sub>1</sub>) implies  
(r<sub>2</sub>.senior  $\rightarrow$  includes(r<sub>3</sub>) iff  
r<sub>2</sub>.senior@pre  $\rightarrow$  includes(r<sub>3</sub>)))**

# Constraints on Operations of Class HRole

---

**addAscendant** (combines addRole and addInheritance)

context **r:HRole::addAscendant(c:Name)**

pre **HRole  $\rightarrow$  forAll(r | r.name  $\langle \rangle$  c)**

post **HRole.allInstances  $\rightarrow$  exists( r<sub>1</sub> |  
r<sub>1</sub>.oclIsNew() and  
r<sub>1</sub>.name = c and  
r.senior  $\rightarrow$  includes(r<sub>1</sub>) and  
HRole.allInstances = HRole.allInstances @pre including(r<sub>1</sub>)  
)**

# Constraints on Operations of Class HRole

---

**addDescendant** (combines addRole and addInheritance)

context **r:HRole::addDescendant(c:Name)**

pre **HRole  $\rightarrow$  forAll(r | r.name  $\langle \rangle$  c)**

post **HRole.allInstances  $\rightarrow$  exists( r<sub>1</sub> |  
r<sub>1</sub>.oclIsNew() and  
r<sub>1</sub>.name = c and  
r<sub>1</sub>.senior  $\rightarrow$  includes(r) and  
HRole.allInstances = HRole.allInstances @pre including(r<sub>1</sub>)  
)**

# Constraints on Operations of Class HRole

---

## authorizedUsers

context **r:HRole::authorizedUsers():Set(HUser)**

pre **true**

post **result =**

**r.senior\*  $\rightarrow$  collect(r<sub>1</sub> | r<sub>1</sub>.assigned\_users)  $\rightarrow$  asSet()**

# Constraints on Operations of Class HRole

---

## Redefining rolePermissions

**context** **r:HRole::rolePermissions()**

**pre** **true**

**post** **result = r.junior\*  $\rightarrow$  collect(r<sub>1</sub> | r<sub>1</sub>.assigned\_permissions)**



# Class HUser

---

HUser enriches User

<code>authorizedRoles():Set(HRole)</code>	<code>&lt;&lt; query &gt;&gt;</code>
<code>userPermissions():Set(Permission)</code>	<code>&lt;&lt; query &gt;&gt;</code>

# Constraints on New Operations of Class HUser

---

## authorizedRoles

context **u:HUser::authorizedRoles():Set(HRole)**

pre **true**

post **result =  
u.role -> collect(r | r.junior\*) -> asSet()**

# Constraints on Operations of Class HUser

---

## Redefining userPermissions

```
context  u:HUser::userPermissions():Set(Permission)
pre     true
post    result =
        u.authorizedRoles() ->
          collect(r1 | r1.assigned_permissions) -> asSet()
```

# Class HSession

---

## HSession enriches Session

```
session_ID:String
```

```
addActiveRole(r:HRole)
```

```
createSession(u:HUser,ars:Set(HUser),id:String)
```

# Modified Constraints on Class HSession

---

## addActiveRole

context **s:HSession::addActiveRole(r:HRole)**

pre **r.authorizedUsers()**  $\rightarrow$  includes(s.session\_user) and  
s.session\_roles  $\rightarrow$  excludes(r)

post s.session\_roles =  
s.session\_roles @pre  $\rightarrow$  including(r)

# Modified Constraints on Class HSession

---

## createSession

context s:HSession::

**createSession(u:HUser,ars:Set(HRole),id:String)**

pre HSessions.allInstances  $\rightarrow$  forAll(s | s.session\_ID  $\neq$  id) and  
u.**authorizedRoles()**  $\rightarrow$  includesAll(ars)

post u.user\_sessions  $\rightarrow$  exists( s<sub>1</sub> |  
s<sub>1</sub>.ocllsNew and  
s<sub>1</sub>.session\_ID = id and  
u.user\_sessions =  
u.user\_sessions @pre  $\rightarrow$  including(s<sub>1</sub>) and  
s.session\_roles = ars  
)

# Derived Invariants

---

## User inheritance relation

context  $r_1, r_2:\text{HRole}$

inv **UserInheritance:**

$r_1.\text{senior}^* \rightarrow \text{includes}(r_2)$  implies

$r_1.\text{authorizedUsers()} \rightarrow$

$\text{includesAll}(r_2.\text{authorizedUsers}())$

# Derived Invariants

---

## User inheritance relation

context  $r_1, r_2:\text{HRole}$

inv **UserInheritance:**

$r_1.\text{senior}^* \rightarrow \text{includes}(r_2)$  implies  
 $r_1.\text{authorizedUsers()} \rightarrow$   
 $\text{includesAll}(r_2.\text{authorizedUsers}())$

## Permission inheritance relation

context  $r_1, r_2:\text{HRole}$

inv **PermissionInheritance:**

$r_1.\text{senior}^* \rightarrow \text{includes}(r_2)$  implies  
 $r_2.\text{rolePermissions()} \rightarrow$   
 $\text{includesAll}(r_1.\text{rolePermissions}())$