White-box Testing by Combining Deduction-based Specification Extraction and Black-box Testing

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www.key-project.org

6th KeY Symposium 2007

Nomborn, Germany June 14, 2007

Requirement Specificaiton

- Given by the user
- Role: To be tested or verified

- Must comply with the IUT (Impl. Under Test)
- Reflects the structure of the program
- Can be extracted automatically

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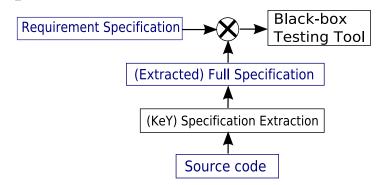
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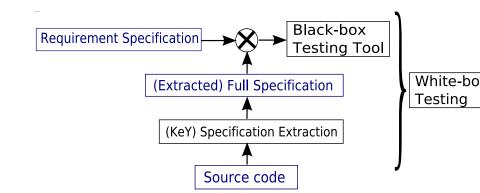
Tool Chain

Requirement Specification Black-box Testing Tool

Tool Chain



Tool Chain



- Using of existing Black-box Testing Tools for White-box testing
- Separation of concerns Modularity
- Combination of Coverage Criteria

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Program Variable = non-rigid Function Symbol

$$(prog.var.)$$
 a = a (logic const.)
 $\circ .$ a = $a(\circ)$

Modal Operators

$$\begin{aligned} [p]\phi & \langle p\rangle\phi & \{a:=b\}\phi \\ \langle \texttt{o.a} = \texttt{t;u.b} = \texttt{s}\rangle\phi & \leadsto & \{a(o):=t \mid \mid b(u'):=s'\}\phi \\ \{\textit{for } x; f_x := g_x\}\phi & \leadsto & \{f_n := g_n||..||f_0 := g_0\}\phi \end{aligned}$$

$$\frac{\Gamma, c = true \Longrightarrow \langle \mathbf{p} \rangle \phi, \Delta \qquad \Gamma, c = false \Longrightarrow \langle \mathbf{q} \rangle \phi, \Delta}{\Gamma \Longrightarrow \langle \mathbf{if}(\mathbf{c}) \{ \mathbf{p} \} \mathbf{else} \{ \mathbf{q} \} . . \rangle \phi, \Delta}$$



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```
public class AbsDiff{
   public static int d;
    /*@ public normal_behavior
       @ requires true;
       0 ensures d==x-y \mid \mid d==y-x;
       @ ensures d \ge x - y \&\& d \ge y - x;
      0*/
    public static void diff(int x, int y){
         if(x < y) d = y;
          else d=x:
         if(d \le y) d = d - x;
          else d=d-y;
```

```
 \begin{array}{c} x < y, x \leq y & \hline x < y, x > y \\ \Rightarrow \{d := y - x\} \Delta & \Rightarrow \{d := y - x\} \Delta & (B_3) & (B_4) \\ \hline & \dots & \\ \hline & x < y \Rightarrow \{d := y\} [\text{if } \dots] \Delta & \{d := x\} [\text{if } \dots] \Delta \\ \Rightarrow [\text{if } (x < y) d = y; \text{else } d = x; \text{ if } (d < = y) \dots] \Delta \\ \end{array}
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```

```
B1: req x<y && y<=y ens d=\old(y-x); also
B3: req x>=y && x<=y ens d=\old(x-y); also
B4: req x>=y && x>y ens d=\old(x-y);
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```
/*@ public normal_behavior
  @ requires true;
  @ ensures d==x-y || d==y-x;
  @ ensures d \ge x - y \& \& d \ge y - x;
  @ also
  0 requires y < x;</pre>
  0 ensures d == \operatorname{old}(x - y);
  @ also
  0 requires y == x;
  @ ensures d == \old(0);
  @ also
  @ requires y > x;
  0 ensures d == \operatorname{old}(y - x);
  @*/
```

```
/*@ public normal_behavior
  @ requires y < x && true;</pre>
  0 ensures d == \operatorname{old}(x - y)
      && (d==x-y \mid | d==y-x) && d>=x-y && d>=y-x;
  @ also
  0 requires y == x && true;
  0 ensures d == \old(0)
      && (d==x-y \mid | d==y-x) && d>=x-y && d>=y-x;
  @ also
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  0 ensures d == \old(y - x)
      && (d==x-y \mid | d==y-x) && d>=x-y && d>=y-x;
  0*/
```

Using the extracted Post Condition

Requirement Specification

With Full Specification

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. . .

Using the extracted Post Condition

Requirement Specification

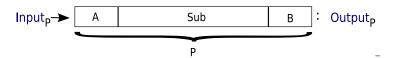
With Full Specification

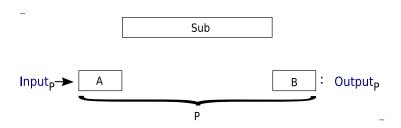
Loops

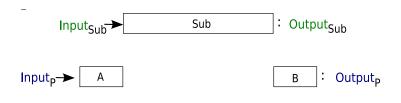
```
while (k<n) {
   if (j=7) {
        j = 0;
        line = new Line(line);
   }
   line.buf[j]=a[k];
   k++; j++;
}</pre>
```

Loops (Unfolding)

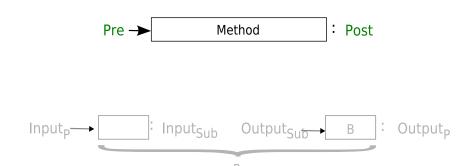
```
if (k<n)
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    line.buf[j]=a[k]; k++; j++;
    if(k<n)
        {if(j=7){..};if(j>7||k>n)..;
        line.buf[j]=a[k]; k++; j++;
        ...
        while(k<n){...}
}</pre>
```

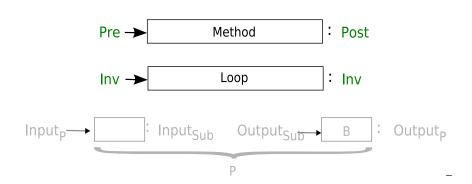


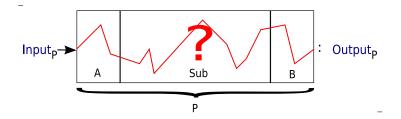




 $\mathsf{Input}_{\mathsf{P}} \longrightarrow \mathsf{A} \quad : \; \mathsf{Input}_{\mathsf{Sub}} \quad \; \mathsf{Output}_{\mathsf{Sub}} \longrightarrow \mathsf{B} \quad : \; \mathsf{Output}_{\mathsf{F}}$







$$\begin{array}{c|c} Post_{C} \Longrightarrow Post \\ \hline Pre \Longrightarrow Pre_{C}, \langle \mathbf{p} \rangle Post & \langle \mathbf{p} \rangle Post_{C}, Pre \Longrightarrow \langle \mathbf{p} \rangle Post \\ \hline Pre_{C} \longrightarrow \langle \mathbf{p} \rangle Post_{C}, Pre \Longrightarrow \langle \mathbf{p} \rangle Post \\ \hline Pre_{C} \longrightarrow \langle \mathbf{p} \rangle Post_{C} \Longrightarrow Pre \longrightarrow \langle \mathbf{p} \rangle Post \\ \hline Contract & \end{array}$$

$$\begin{array}{c|c} Post_{C} \Longrightarrow Post \\ \hline Pre \Longrightarrow Pre_{C}, \langle p \rangle Post & \hline \langle p \rangle Post_{C}, Pre \Longrightarrow \langle p \rangle Post \\ \hline Pre_{C} \to \langle p \rangle Post_{C}, Pre \Longrightarrow \langle p \rangle Post \\ \hline Pre_{C} \to \langle p \rangle Post_{C} \Longrightarrow Pre \to \langle p \rangle Post \\ \hline Contract & \\ \end{array}$$

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$$Pre \Rightarrow Pre_{C}, \langle p \rangle Post \qquad \langle p \rangle Post_{C}, Pre \Rightarrow \langle p \rangle Post$$

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$$Contract$$

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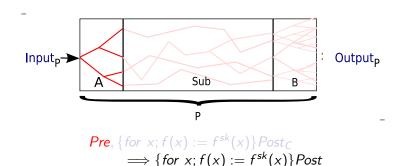
KeY's Contract Rule

```
Pre, \{for \ x; f(x) := f^{sk}(x)\} Post_C
         \implies {for x; f(x) := f^{sk}(x)} Post
                 \langle p \rangle Post_C, Pre \Longrightarrow \langle p \rangle Post
  Pre, Pre_C \rightarrow \langle p \rangle Post_C \Longrightarrow \langle p \rangle Post
Pre_C \rightarrow \langle p \rangle Post_C \Longrightarrow Pre \rightarrow \langle p \rangle Post
          Contract
```

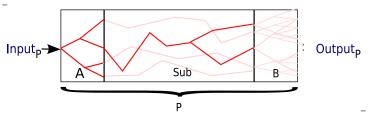
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                              Pre, Pre_C \rightarrow \langle p \rangle Post_C \Longrightarrow \langle p \rangle Post
                            Pre_C \rightarrow \langle p \rangle Post_C \Rightarrow Pre \rightarrow \langle p \rangle Post
                                      Contract
where \{forx.f(x) := f^{sk}(x)\} abbrev.
\{for \ x_{0,1},\ldots x_{0,n_0},f_0(x_{0,1},\ldots,x_{0,n_0}):=f_0^{sk}(x_{0,1},\ldots,x_{0,n_0})\}
\{for \ x_{m \ 1}, \dots, x_{m \ n_m}, f_m(x_{m \ 1}, \dots, x_{m \ n_m}) := f_m^{sk}(x_{m \ 1}, \dots, x_{m \ n_m})\}
```

Explicit Structural Coverage



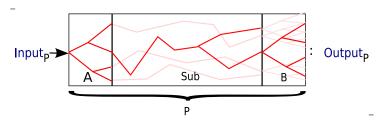
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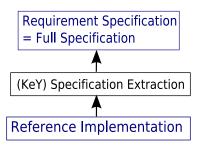
Loops (Invariants)

```
while (k < n) {
  if (j=7) {
             = 0;
    line = new Line(line);
  line.buf[j]=a[k];
  k++; j++;
            0 < k < n \land 0 < j < n \land j < 7
```

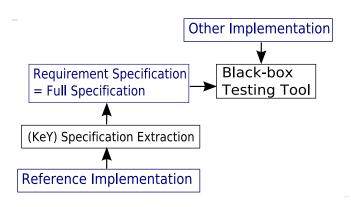
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  k++; j++;
Invariant:
             0 < k < n \land 0 < j < n \land j < 7
```

Requirement Specification from a Reference Implementation



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- Enrich existing Requirement Specification with Program Structure
- Use Black-box Testing tool for White-box testing
- Tools that use Symbolic Execution can be extended
- An Importer and Exporter for a Specification language has to be implemented

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