# Analysing Probabilistic Network Flooding KeY Symposium 2007

#### Frank Werner

University Karlsruhe

15.06.2007

#### Introduction

- Probabilistic Model Checking
- Authenticated Query Flooding

#### 2 Analysis of the AQF

• Results: Computing Rewards



Application Areas of PMC:

- unreliable or unpredictable behaviour
- analyse system performance
- distributed algorithms

Application Examples

- randomised leader election algorithm
- any system that can suffer failures
- communication with unreliable links (wireless networks)
- security systems

# Introduction: DTMC



## **Discrete Time Markov Chains: Transitions**



#### **Transition Probabilities**

## Discrete Time Markov Chains: Labels



## Introduction: Reward Rates



#### **Reward Variables**

# Probabilistic Computation Tree Logic (PCTL)

State Formulas  $\phi$ :

- true
- a
- $\neg \phi$
- $\phi_1 \wedge \phi_2$
- $\mathcal{P}_{\triangleleft p}[\psi]$
- $\mathcal{C}_{\triangleleft c}[\phi]$

#### Path Formulas $\psi$ :

•  $\phi$ 

- φ<sub>1</sub>Uφ<sub>2</sub>
- $\phi_1 \mathcal{U}^{\leq k} \phi_2$

### with $\triangleleft \in \{\leq, <, \geq, >\}$ , $p \in [0, 1]$ , $c \in \mathbb{R}^{\geq 0}$ , $k \in \mathbb{N}$

## Why doing Authenticated Query Flooding...

Secure technique for obtaining information about the network and recognize fake queries which possibly stem from an "intruder"

Assumptions underlying the model:

- queries are injected by a base station at sensor A
- propagation along the bidirectional links
- What a sensor does
  - upon packet reception
    - $\implies$  apply the AQF algorithm
  - after processing
    - $\Longrightarrow$  go to sleep



# Introduction to AQF

- security mechanism for multicast communication (ID-based key distribution)
- a tradeoff between MACs and digital signatures
- each sensor loaded with a defined number of keys
- on reception of a packet q:
  - packet is authenticated and distributed to the sensor's neighbours
  - packet is not authenticated and dropped
  - packet q can not be authenticated due to a missing key → q is distributed to the neighbours (AQF-pass)

#### proability that a sensor accepts query with fake authenticator

$$p_f = \left(rac{l-k}{l} + rac{k}{l} rac{B}{m}
ight)^m$$

- Modelling using probabilistic automata (Prism tool)
- finding proper parameters for the AQF algorithm
   ⇒ energy/security trade-off
- estimation of energy consumption (reward variables) with real-world sensor data from the TMote Sky sensor board
- comparison of different topologies with regard to energy efficiency, security, and AQF parameter



# Results: Energy Rewards for Sensor Network



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- Analysis of arbitrary complex topologies by PA
- proper solutions for the energy/security tradeoff
- fast and exact solutions (no confidence levels as opposed in simulation)
- maximal network size somehow restricted to about 20 nodes (sufficient for many real life scenarios)

# THANK YOU...