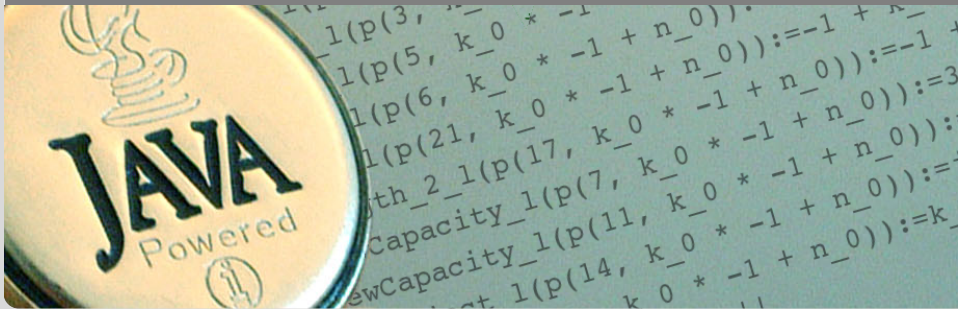


Applications of Formal Verification

Model Checking: Introduction to SPIN

Dr. Vladimir Klebanov · Dr. Mattias Ulbrich | SS 2015

KIT – INSTITUT FÜR THEORETISCHE INFORMATIK



SPIN: Previous Lecture vs. This Lecture

Previous lecture

SPIN appeared as a PROMELA *simulator*

This lecture

Intro to SPIN as a *model checker*

What Does A Model Checker Do?

A Model Checker (MC) is designed to prove the user wrong.

MC tries its best to *find a counter example* to the correctness properties.

It is tuned for that.

MC does not try to prove correctness properties.

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⇒ *Finding no counter example proves stated correctness properties.*

What does 'exhaustive search' mean here?

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=
resolving non-determinism in all possible ways

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For model checking PROMELA code,
two kinds of non-determinism to be resolved:

- *explicit, local:*

`if/do` statements

`:: guardX ->`

`:: guardY ->`

- *implicit, global:*

scheduling of concurrent processes
(see next lecture)

Model Checker for This Course: SPIN

SPIN: “Simple *Promela Interpreter*”

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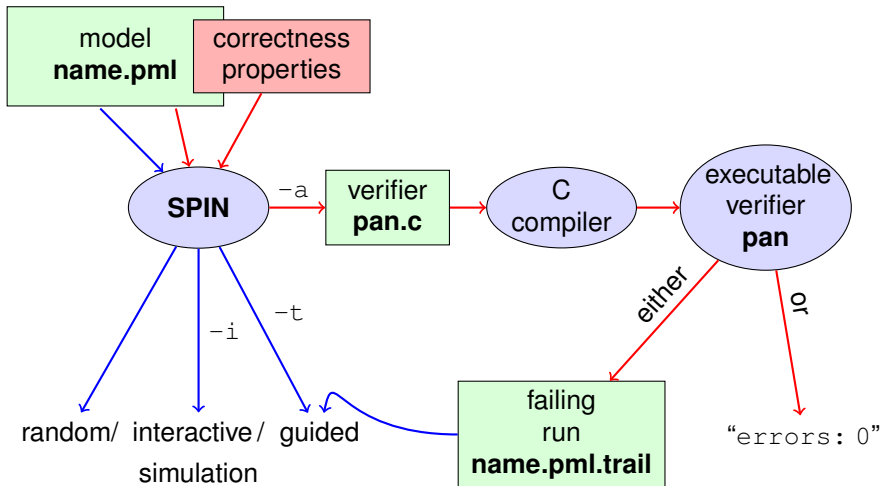
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- simulating a model (randomly/interactively/**guided**)
- generating a *verifier*

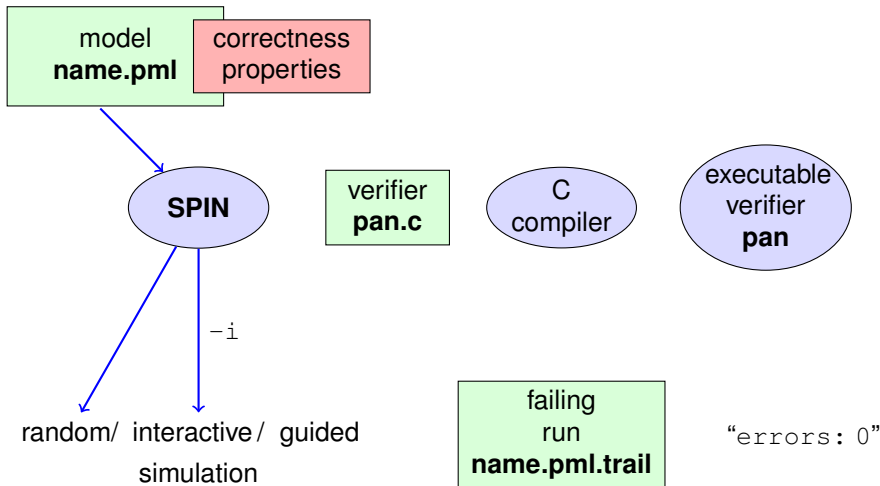
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- in case the check is negative:
generates a **failing run** of the model, **to be simulated by SPIN**

SPIN Workflow: Overview

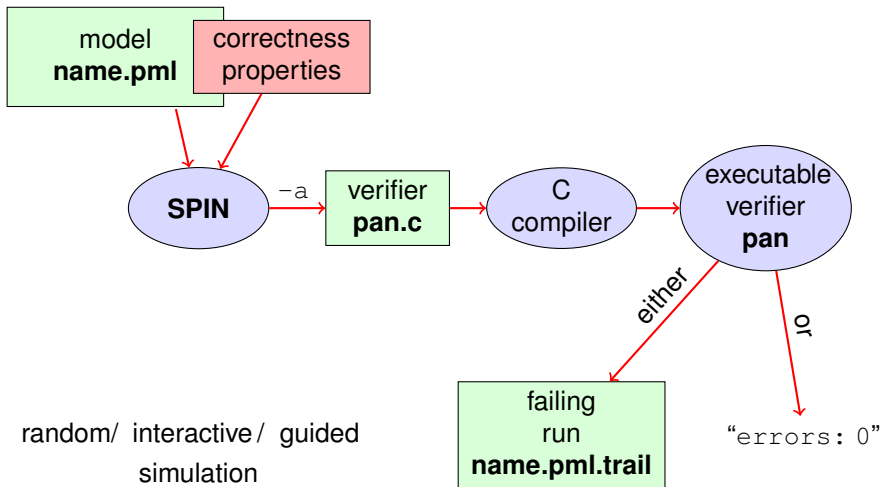


Plain Simulation with SPIN



- run example, random and interactive
`interleave.pml, zero.pml`

Model Checking with SPIN



Meaning of Correctness wrt. Properties

Given PROMELA model M , and correctness properties C_1, \dots, C_n .

- Be R_M the set of **all possible runs** of M .
- For each correctness property C_i ,
 R_{M,C_i} is the set of all **runs** of M **satisfying** C_i .
($R_{M,C_i} \subseteq R_M$)
- M is **correct** wrt. C_1, \dots, C_n iff $(R_{M,C_1} \cap \dots \cap R_{M,C_n}) = R_M$.
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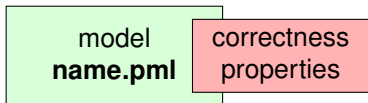
But how to write Correctness Properties?

Stating Correctness Properties

model
name.pml

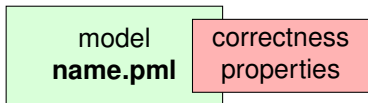
correctness
properties

Stating Correctness Properties



Correctness properties can be stated (syntactically) **within** or **outside** the model.

Stating Correctness Properties

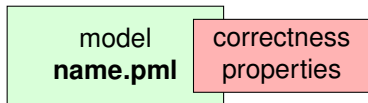


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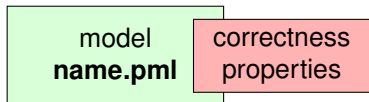


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- meta labels
 - end labels
 - accept labels
 - progress labels

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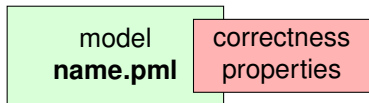
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- never claims
- temporal logic formulas

Stating Correctness Properties



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stating properties within the model, using

- *assertion statements* (today)
- meta labels
 - *end labels* (today)
 - `accept` labels
 - `progress` labels

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Definition (Assertion Statements)

Assertion statements in PROMELA are statements of the form

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stmt2;  
...
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```
...  
stmt1;  
assert (max == a);  
stmt2;  
...
```

```
...  
if  
:: b1 -> stmt3;  
           assert (x < y)  
:: b2 -> stmt4  
...
```

Meaning of **Boolean** Assertion Statements

`assert` (*expr*)

- has **no effect** if *expr* evaluates to **true**
- triggers an **error message** if *expr* evaluates to **false**

This holds in both, simulation and model checking mode.

Meaning of **General** Assertion Statements

`assert (expr)`

- has no effect if *expr* evaluates to **non-zero value**
- triggers an error message if *expr* evaluates to **0**

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Meaning of **General** Assertion Statements

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Recall:

`bool true false` is syntactic sugar for

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This holds in both, simulation and model checking mode.

Recall:

`bool true false` is syntactic sugar for
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⇒ general case covers Boolean case

Instead of using 'printf's for Debugging ...

```
/* after choosing a,b from {1,2,3} */  
if  
  :: a >= b -> max = a;  
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fi;  
printf("the maximum of %d and %d is %d\n",  
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Command Line Execution

(simulate, inject faults, add assertion, simulate again)

```
> spin max.pml
```

... we can employ **Assertions**

quoting from file **max.pml**:

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Now, we have a first example with a formulated **correctness property**.

... we can employ **Assertions**

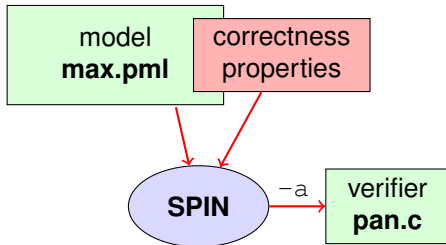
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Now, we have a first example with a formulated **correctness property**.

We can do **model checking**, for the first time!

Generate Verifier in C



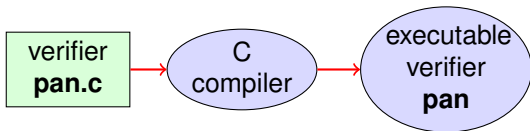
Command Line Execution

Generate Verifier in C

```
> spin -a max.pml
```

SPIN generates **Verifier** in C, called **pan.c**
(plus helper files)

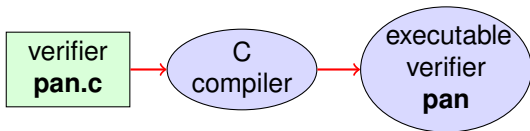
Compile To Executable Verifier



Command Line Execution

compile to executable verifier

```
> gcc -o pan pan.c
```

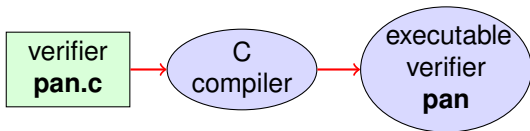


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C compiler generates **executable verifier pan**



Command Line Execution

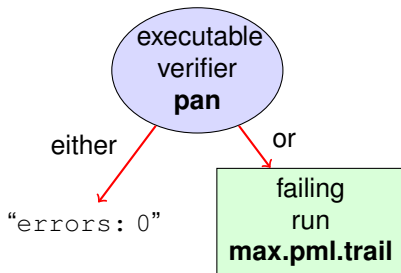
compile to executable verifier

```
> gcc -o pan pan.c
```

C compiler generates **executable verifier pan**

pan: historically “**protocol analyzer**”, now “**process analyzer**”

Run Verifier (= Model Check)

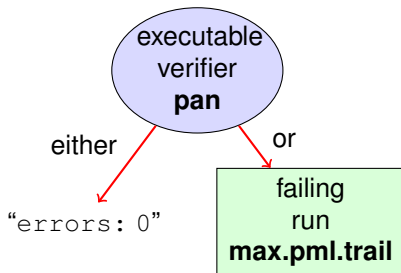


Command Line Execution

run verifier pan

> *./pan*

Run Verifier (= Model Check)



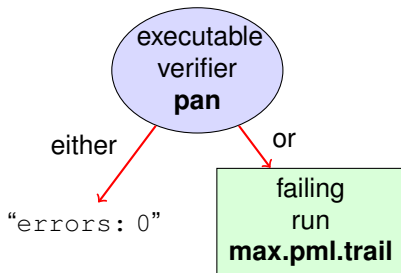
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- prints "errors: 0"

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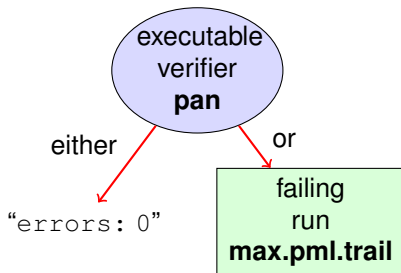
Command Line Execution

```
run verifier pan
```

```
> ./pan
```

- prints "errors: 0" ⇒ Correctness Property verified!

Run Verifier (= Model Check)



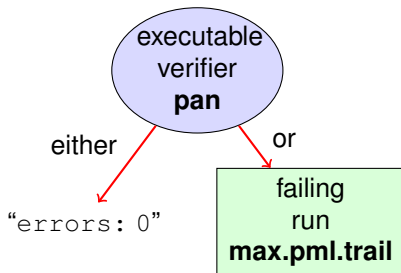
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- prints "errors: 0", or
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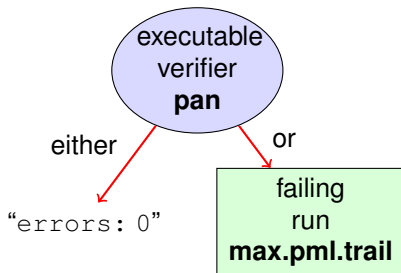
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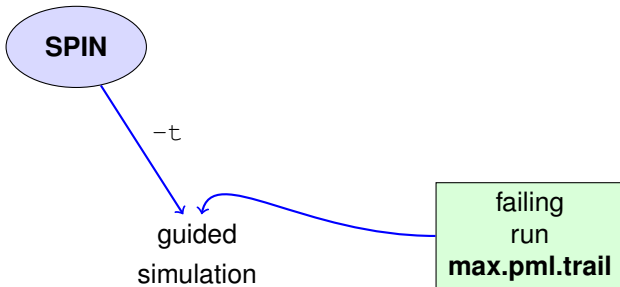
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run verifier pan
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```
> ./pan
```

- prints “errors: 0”, or
- prints “errors: n ” ($n > 0$) \Rightarrow counter example found!
records failing run in **max.pml.trail**

Guided Simulation

To **examine failing run**: employ **simulation mode**, “guided” by trail file.



Command Line Execution

inject a fault, re-run verification, and then:

```
> spin -t -p -l max.pml
```

Output of Guided Simulation

can look like:

```
Starting P with pid 0
1: proc 0 (P) line 8 "max.pml" (state 1) [a = 1]
      P(0):a = 1
2: proc 0 (P) line 14 "max.pml" (state 7) [b = 2]
      P(0):b = 2
3: proc 0 (P) line 23 "max.pml" (state 13) [((a<=b))]
3: proc 0 (P) line 23 "max.pml" (state 14) [max = a]
      P(0):max = 1
spin: line 25 "max.pml", Error: assertion violated
spin: text of failed assertion:
      assert(( (a>b) -> ((max==a) : ((max==b)) ))
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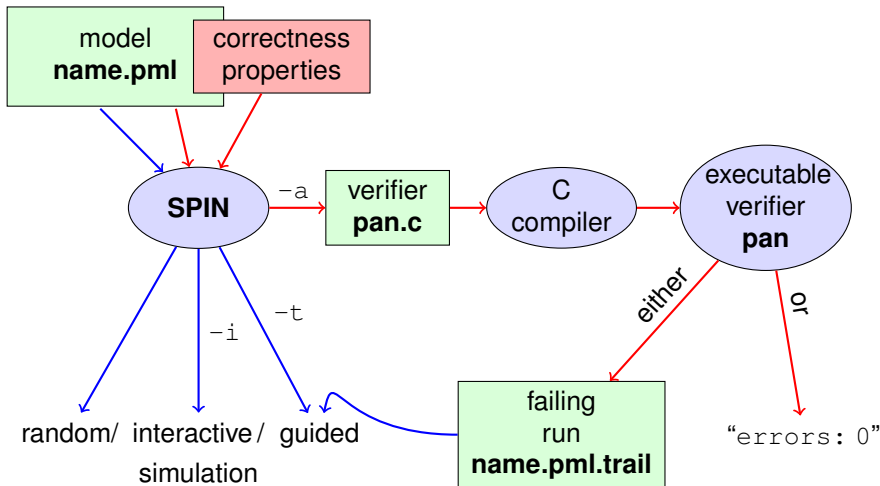
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assignments in the run

values of variables whenever updated

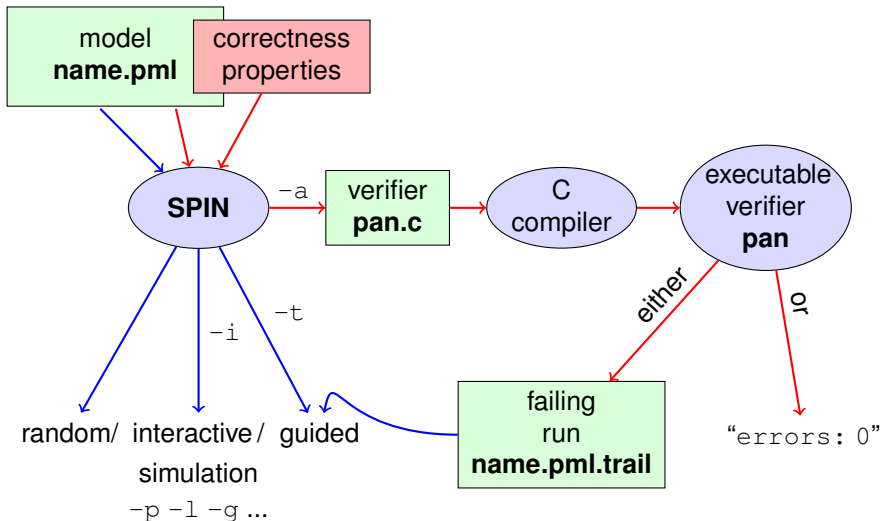
What did we do so far?

following whole cycle (most primitive example, assertions only)



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following whole cycle (most primitive example, assertions only)



Further Examples: Integer Division

```
int dividend = 15;
int divisor  = 4;
int quotient, remainder;

quotient = 0;
remainder = dividend;
do
  :: remainder > divisor ->
    quotient++;
    remainder = remainder - divisor
  :: else ->
    break
od;
printf("%d divided by %d = %d, remainder = %d\n",
       dividend, divisor, quotient, remainder);
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```

simulate, put assertions, verify, change values, ...

Further Examples: Greatest Common Divisor

```
int x = 15, y = 20;
int a, b;
a = x; b = y;
do
  :: a > b -> a = a - b
  :: b > a -> b = b - a
  :: a == b -> break
od;
printf("The GCD of %d and %d = %d\n", x, y, a)
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⇒ **typical for model checking**

Typical Command Lines

typical command line sequences:

random simulation

```
spin name.pml
```

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typical command line sequences:

random simulation

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interactive simulation

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spin -i name.pml
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spin -a name.pml  
gcc -o pan pan.c  
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spin name.pml
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interactive simulation

```
spin -i name.pml
```

model checking

```
spin -a name.pml  
gcc -o pan pan.c  
./pan
```

and in case of error

```
spin -t -p -l -g name.pml
```

Ben-Ari produced **Spin Reference Card**, summarizing

- **typical command line sequences**
- **options for**
 - **SPIN**
 - gcc
 - pan
- **PROMELA**
 - datatypes
 - operators
 - statements
 - guarded commands
 - processes
 - channels
- **temporal logic syntax**

Why SPIN?

- SPIN targets software, instead of hardware verification
- based on standard theory of ω -automata and linear temporal logic
- 2001 ACM Software Systems Award (other winning software systems include: Unix, TCP/IP, WWW, Tcl/Tk, Java)
- used for safety critical applications
- distributed freely as research tool, well-documented, actively maintained, large user-base in academia and in industry
- annual SPIN user workshops series held since 1995

Why SPIN? (Cont'd)

- PROMELA and SPIN are rather simple to use
- good to understand a few system really well, rather than many systems poorly
- availability of good course book (Ben-Ari)
- availability of front end JSPIN (also Ben-Ari)

What is JSPIN?

- graphical user interface for SPIN
- developed for pedagogical purposes
- written in Java
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- **makes back-end calls transparent**

Command Line Execution

calling JSPIN

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> java -jar /usr/local/jSpin/jSpin.jar
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(with path adjusted to your setting)

or use shell script:

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play around with similar examples ...

Catching A Different Type of Error

quoting from file **max2.pml**:

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/* after choosing a,b from {1,2,3} */  
if  
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Note: no **assert** in **max2.pml**.

Catching A Different Type of Error

Further inspection of **pan** output:

```
...  
pan: invalid end state (at depth 1)  
pan: wrote max2.pml.trail  
...
```

Legal and Illegal Blocking

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in **max1.pml**, no process can take over.

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- P 's textual end
- each location marked with an **end label**: “endxxx:”

End labels are not useful in **max1.pml**, but elsewhere, they are.

Example: `end.pml`

Literature for this Lecture

Ben-Ari Chapter 2, Sections 4.7.1, 4.7.2