

PdF:  
Exploiting LP Infeasibility Certificates  
for Efficient and Trustworthy NN Verification

## Background

Neural networks are State-of-the-Art in numerous machine learning tasks ranging from image classification to beating world-class human players in the games of Chess and Go. These achievements have led to the implementation of neural networks in safety-critical domains like aircraft controllers [3] and autonomous driving. In these areas, failures can have dramatic consequences. Therefore, provable guarantees about the behavior of the corresponding neural networks are necessary. However, we can only provide guarantees for Neural Networks in practice, if the techniques providing these guarantees are, both, trustworthy and scalable.

## Idea

Prior work has shown how neural network verification tools can be extended to provide proof certificates for their verification results [2]. On the one hand, proof production can be used to build formally verified proof checkers which can be used to increase the trust in the verification results provided by a solver [1]. On the other hand, proof production also opens the door to Conflict Driven Clause Learning [5]: During the exhaustive exploration of a neural network's input space, partial proof certificates are potentially reusable in different input regions which can speed up neural network verification. While there exists some initial work towards CDCL for NN verification [4], efficiently exploiting infeasibility certificates for NN verification turns out to be more challenging than its propositional counterpart. A major reason for this lies in the cost of computing small, ideally irreducible, infeasible subsets.

## Project Plan

Following an in-depth literature research on pre-existing approaches, this project can be taken in two directions: We could either come up with a more efficient approach to use infeasibility certificates for Conflict Driven Clause Learning, or we could explore how infeasibility certificates can help to reduce the workload of verified proof-checkers to make verified proof-checking more computationally feasible.

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## References

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